## EUROPEAN STANDARD NORME EUROPÉENNE EUROPÄISCHE NORM

# FINAL DRAFT prEN 1991-1-4

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Will supersede ENV 1991-2-4:1995

## English version

## Eurocode 1: Actions on structures - General actions - Part 1-4: Wind actions

Eurocode 1 - Actions sur les structures - Partie 1-4 : Actions générales - Actions du vent Eurocode 1: Einwirkungen auf Tragwerke - Teil 1-4: Allgemeine Einwirkungen - Windlasten

This draft European Standard is submitted to CEN members for formal vote. It has been drawn up by the Technical Committee CEN/TC 250.

If this draft becomes a European Standard, CEN members are bound to comply with the CEN/CENELEC Internal Regulations which stipulate the conditions for giving this European Standard the status of a national standard without any alteration.

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EUROPEAN COMMITTEE FOR STANDARDIZATION COMITÉ EUROPÉEN DE NORMALISATION EUROPÄISCHES KOMITEE FÜR NORMUNG

Management Centre: rue de Stassart, 36 B-1050 Brussels

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## **Foreword**

This European Standard has been prepared by Technical Committee CEN/TC250 "Structural Eurocodes", the Secretariat for which is held by BSI.

This document is currently submitted to the formal vote.

This European Standard supersedes ENV 1991-2-4: 1995.

The Annexes A, B, C, D, E and F are informative.

## **Background of the Eurocode programme**

In 1975, the Commission of the European Community decided on an action programme in the field of construction, based on article 95 of the Treaty. The objective of the programme was the elimination of technical obstacles to trade and the harmonisation of technical specifications.

Within this action programme, the Commission took the initiative to establish a set of harmonised technical rules for the design of construction works which, in a first stage, would serve as an alternative to the national rules in force in the Member States and, ultimately, would replace them.

For fifteen years, the Commission, with the help of a Steering Committee with Representatives of Member States, conducted the development of the Eurocodes programme, which led to the first generation of European codes in the 1980s.

In 1989, the Commission and the Member States of the EU and EFTA decided, on the basis of an agreement between the Commission and CEN, to transfer the preparation and the publication of the Eurocodes to the CEN through a series of Mandates, in order to provide them with a future status of European Standard (EN). This links de facto the Eurocodes with the provisions of all the Council's Directives and/or Commission's Decisions dealing with European standards (e.g. the Council Directive 89/106/EEC on construction products - CPD - and Council Directives 93/37/EEC, 92/50/EEC and 89/440/EEC on public works and services and equivalent EFTA Directives initiated in pursuit of setting up the internal market).

<sup>&</sup>lt;sup>1</sup> Agreement between the Commission of the European Communities and the European Committee for Standardisation (CEN) concerning the work on EUROCODES for the design of building and civil engineering works (BC/CEN/03/89).

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The Structural Eurocode programme comprises the following standards generally consisting of a number of Parts:

EN 1990	Eurocode :	Basis of Structural Design
EN 1991	Eurocode 1:	Actions on structures
EN 1992	Eurocode 2:	Design of concrete structures
EN 1993	Eurocode 3:	Design of steel structures
EN 1994	Eurocode 4:	Design of composite steel and concrete structures
EN 1995	Eurocode 5:	Design of timber structures
EN 1995 EN 1996	Eurocode 5: Eurocode 6:	Design of timber structures  Design of masonry structures
EN 1996	Eurocode 6:	Design of masonry structures
EN 1996 EN 1997	Eurocode 6: Eurocode 7:	Design of masonry structures  Geotechnical design

Eurocode standards recognise the responsibility of regulatory authorities in each Member State and have safeguarded their right to determine values related to regulatory safety matters at national level where these continue to vary from State to State.

## Status and field of application of Eurocodes

The Member States of the EU and EFTA recognise that Eurocodes serve as reference documents for the following purposes :

- as a means to prove compliance of building and civil engineering works with the essential requirements of Council Directive 89/106/EEC, particularly Essential Requirement N°1 – Mechanical resistance and stability – and Essential Requirement N°2 –Safety in case of fire;
- as a basis for specifying contracts for construction works and related engineering services;
- as a framework for drawing up harmonised technical specifications for construction products (ENs and ETAs)

The Eurocodes, as far as they concern the construction works themselves, have a direct relationship with the Interpretative Documents<sup>2</sup> referred to in Article 12 of the CPD, although they are of a different nature from harmonised product standards<sup>3</sup>. Therefore, technical aspects arising from the Eurocodes work need to be adequately considered by CEN Technical Committees and/or EOTA Working Groups working on product standards with a view to achieving full compatibility of these technical specifications with the Eurocodes.

The Eurocode standards provide common structural design rules for everyday use for the design of whole structures and component products of both a traditional and an innovative nature. Unusual forms of construction or

a) give concrete form to the essential requirements by harmonising the terminology and the technical bases and indicating classes or levels for each requirement where necessary:

The Eurocodes, de facto, play a similar role in the field of the ER 1 and a part of ER 2.

<sup>&</sup>lt;sup>2</sup> According to Art. 3.3 of the CPD, the essential requirements (ERs) shall be given concrete form in interpretative documents for the creation of the necessary links between the essential requirements and the mandates for harmonised ENs and ETAGs/ETAs.

<sup>&</sup>lt;sup>3</sup> According to Art. 12 of the CPD the interpretative documents shall:

b) indicate methods of correlating these classes or levels of requirement with the technical specifications, e.g. methods of calculation and of proof technical rules for project design, etc.;

c) serve as a reference for the establishment of harmonised standards and guidelines for European technical approvals.

design conditions are not specifically covered and additional expert consideration will be required by the designer in such cases.

## **National Standards implementing Eurocodes**

The National Standards implementing Eurocodes will comprise the full text of the Eurocode (including any annexes), as published by CEN, which may be preceded by a National title page and National foreword, and may be followed by a National annex.

The National annex may only contain information on those parameters which are left open in the Eurocode for national choice, known as Nationally Determined Parameters, to be used for the design of buildings and civil engineering works to be constructed in the country concerned, *i.e.* :

- values and/or classes where alternatives are given in the Eurocode,
- values to be used where a symbol only is given in the Eurocode,
- country specific data (geographical, climatic, etc.), e.g. wind map,
- the procedure to be used where alternative procedures are given in the Eurocode.

It may also contain

- decisions on the use of informative annexes, and
- references to non-contradictory complementary information to assist the user to apply the Eurocode.

## Links between Eurocodes and harmonised technical specifications (ENs and ETAs) for products

There is a need for consistency between the harmonised technical specifications for construction products and the technical rules for works<sup>4</sup>. Furthermore, all the information accompanying the CE Marking of the construction products which refer to Eurocodes should clearly mention which Nationally Determined Parameters have been taken into account.

## Additional information specific for EN 1991-1-4

EN 1991-1-4 gives design guidance and actions for the structural design of buildings and civil engineering works for wind.

EN 1991-1-4 is intended for the use by clients, designers, contractors and relevant authorities.

EN 1991-1-4 is intended to be used with EN 1990, the other Parts of EN 1991 and EN 1992-1999 for the design of structures.

## National annex for EN 1991-1-4

This standard gives alternative procedures, values and recommendations for classes with notes indicating where National choice may be made. Therefore the National Standard implementing EN 1991-1-4 should have a National Annex containing Nationally Determined Parameters to be used for the design of buildings and civil engineering works to be constructed in the relevant country.

National choice is allowed for EN 1991-1-4 through clauses:

1.1 (12)

 $<sup>^{4}</sup>$  see Art.3.3 and Art.12 of the CPD, as well as clauses 4.2, 4.3.1, 4.3.2 and 5.2 of ID 1.

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4.1 (1)
4.2 (1)P Note 2
4.2 (2)P Notes 1, 2, 3 and 5
4.3.1 (1) Notes 1 and 2
4.3.2 (1)
4.3.2 (2)
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#### 1 General

## 1.1 Scope

- (1) EN 1991-1-4 gives guidance on the determination of natural wind actions for the structural design of building and civil engineering works for each of the loaded areas under consideration. This includes the whole structure or parts of the structure or elements attached to the structure, e. g. components, cladding units and their fixings, safety and noise barriers.
- (2) This Part is applicable to:
- Buildings and civil engineering works with heights up to 200 m. See also (11) and (12).
- Bridges having no span greater than 200 m, provided that they satisfy the criteria for dynamic response, see (12) and 8.2.
- (3) This part is intended to predict characteristic wind actions on land-based structures, their components and appendages.
- (4) Certain aspects necessary to determine wind actions on a structure are dependent on the location and on the availability and quality of meteorological data, the type of terrain, etc. These need to be provided in the National Annex and Annex A, through National choice by notes in the text as indicated. Default values and methods are given in the main text, where the National Annex does not provide information.
- (5) Annex A gives illustrations of the terrain categories and provides rules for the effects of orography including displacement height, roughness change, influence of landscape and influence of neighbouring structures.
- (6) Annex B and C give alternative procedures for calculating the structural factor  $c_s c_d$ .
- (7) Annex D gives  $c_s c_d$  factors for different types of structures.
- (8) Annex E gives rules for vortex induced response and some guidance on other aeroelastic effects.
- (9) Annex F gives dynamic characteristics of structures with linear behaviour
- (10) This part does not give guidance on local thermal effects on the characteristic wind, e.g. strong arctic thermal surface inversion or funnelling or tornadoes.
- (11) Guyed masts and lattice towers are treated in EN 1993-7-1 and lighting columns in EN 40
- (12) This part does not give guidance on the following aspects:
- torsional vibrations, e.g. tall buildings with a central core
- bridge deck vibrations from transverse wind turbulence
- cable supported bridges
- vibrations where more than the fundamental mode needs to be considered

NOTE The National Annex may provide guidance on these aspects as non contradictory complementary information.

#### 1.2 Normative references

The following normative documents contain provisions which, through references in this text, constitute provisions of this European standard. For dated references, subsequent amendments to, or revisions of any of these publications do not apply. However, parties to agreements based on this European standard are encouraged to investigate the possibility of applying the most recent editions of the normative documents indicated below. For undated references the latest edition of the normative document referred to applies.

EN 1990 Eurocode: Basis of structural design

EN 1991-1-3 Eurocode 1: Actions on structures: Part 1-3: Snow loads

EN 1991-1-6 Eurocode 1: Actions on structures: Part 1-6: Actions during execution

EN 1991-2 Eurocode 1: Actions on structures: Part 2: Traffic loads on bridges

## 1.3 Assumptions

(1)PThe general assumptions given in EN 1990, 1.3 apply.

## 1.4 Distinction between Principles and Application Rules

(1)PThe rules in EN 1990, 1.4 apply.

## 1.5 Design assisted by testing and measurements

- (1) With the approval of the appropriate Authority, wind tunnel tests and proven and/or properly validated numerical methods may be used to obtain load and response information, using appropriate models of the structure and of the natural wind.
- (2) With the approval of the appropriate Authority, load and response information and terrain parameters may be obtained by appropriate full scale data.

## 1.6 Definitions

For the purposes of this European Standard, the definitions given in ISO 2394, ISO 3898 and ISO 8930 and the following apply. Additionally for the purposes of this Standard a basic list of definitions is provided in EN 1990,1.5.

## 1.6.1

#### fundamental basic wind velocity

the 10 minute mean wind velocity with an annual risk of being exceeded of 0, 02, irrespective of wind direction, at a height of 10 m above flat open country terrain and accounting for altitude effects (if required)

## 1.6.2

## basic wind velocity

the fundamental basic wind velocity modified to account for the direction of the wind being considered and the season (if required)

## 1.6.3

#### mean wind velocity

the basic wind velocity modified to account for the effect of terrain roughness and orography

#### 1.6.4

## pressure coefficient

external pressure coefficients give the effect of the wind on the external surfaces of buildings; internal pressure coefficients give the effect of the wind on the internal surfaces of buildings.

The external pressure coefficients are divided into overall coefficients and local coefficients. Local coefficients give the pressure coefficients for loaded areas of 1 m<sup>2</sup> or less e.g. for the design of small elements and fixings; overall coefficients give the pressure coefficients for loaded areas larger than 10 m<sup>2</sup>.

Net pressure coefficients give the resulting effect of the wind on a structure, structural element or component per unit area.

#### 1.6.5

#### force coefficient

force coefficients give the overall effect of the wind on a structure, structural element or component as a whole, including friction, if not specifically excluded

#### 1.6.6

#### background response factor

the background factor allowing for the lack of full correlation of the pressure on the structure surface

#### 1.6.7

## resonance response factor

the resonance response factor allowing for turbulence in resonance with the vibration mode

## 1.7 Symbols

(1) For the purposes of this European standard, the following symbols apply

NOTE The notation used is based on ISO 3898:1999. In this Part the symbol dot in expressions indicates the multiplication sign. This notation has been employed to avoid confusion with functional expressions.

(2) A basic list of notations is provided in EN 1990, 1.6 and the additional notations below are specific to EN 1991-1-4.

Latin upper case letters

<i>A</i> ar	ea
-------------	----

 $A_{\rm fr}$  area swept by the wind

A<sub>ref</sub> reference area

B<sup>2</sup> background response partC wind load factor for bridges

E Young's modulus

 $F_{\rm fr}$  resultant friction force

*F*<sub>i</sub> vortex exciting force at point j of the structure

F<sub>w</sub> resultant wind force

H height of a topographic feature

 $I_{\nu}$  turbulence intensity

K mode shape factor; shape parameter  $K_{iv}$  interference factor for vortex shedding

 $K_{rd}$  reduction factor for parapets

 $K_{\rm w}$  correlation length factor

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 $K_{x}$  non dimensional coefficient

L length of the span of a bridge deck; turbulent length scale

 $L_{\rm d}$  actual length of a downwind slope  $L_{\rm e}$  effective length of an upwind slope

L<sub>i</sub> correlation length

L<sub>u</sub> actual length of an upwind slope

N number of cycles caused by vortex shedding

 $N_{\rm g}$  number of loads for gust response

*R*<sup>2</sup> resonant response part

Re Reynolds number

 $R_h$ ,  $R_b$  aerodynamic admittance

S wind action

Sc Scruton number

S<sub>L</sub> non dimensional power spectral density function

St Strouhal number

 $W_{\rm s}$  weight of the structural parts contributing to the stiffness of a chimney

 $W_{\rm t}$  total weight of a chimney

#### Latin lower case letters

a<sub>G</sub> factor of galloping instability

a<sub>IG</sub> combined stability parameter for interference galloping

b width of the structure

 $egin{array}{lll} c_{
m alt} & & {
m altitude\ factor} \ & & {
m dynamic\ factor} \ & & {
m directional\ factor} \ & & {
m c_{f}} & & {
m force\ coefficient} \ \end{array}$ 

 $c_{\text{f,o}}$  force coefficient of structures or structural elements without free-end flow

 $egin{array}{ll} c_{
m f,l} & ext{lift force coefficient} \\ c_{
m fr} & ext{friction coefficient} \\ \end{array}$ 

 $c_{\text{lat}}$  aerodynamic exciting coefficient

 $egin{array}{lll} c_{
m M} & {
m moment coefficient} \ c_{
m p} & {
m pressure coefficient} \ c_{
m prob} & {
m probability factor} \ c_{
m r} & {
m roughness factor} \ c_{
m o} & {
m orography factor} \ \end{array}$ 

c<sub>s</sub> size factor

c<sub>season</sub> seasonal factor

d depth of the structure

e eccentricity of a force or edge distance

f<sub>L</sub> non dimensional frequency

h height of the structure
h<sub>dis</sub> displacement height
k equivalent roughness

 $k_{
m p}$  peak factor  $k_{
m r}$  terrain factor  $k_{
m e}$  torsional stiffness

I length of a horizontal structure

m mass per unit length

 $m_1$  equivalent mass per unit length

 $n_{\rm i}$  natural frequency of the structure of the mode i  $n_{\rm 1,x}$  fundamental frequency of along wind vibration  $n_{\rm 1,y}$  fundamental frequency of cross-wind vibration

 $n_0$  ovalling frequency

p annual probability of exceedence

*q*<sub>b</sub> reference mean (basic) velocity pressure

 $q_p$  peak velocity pressure

*r* radius

s factor; coordinate

t averaging time of the reference wind speed, plate thickness

 $v_{\rm CG}$  onset wind velocity for galloping

 $v_{\text{CIG}}$  critical wind velocity for interference galloping

 $v_{\rm crit}$  critical wind velocity of vortex shedding

 $v_{\rm div}$  divergence wind velocity

 $v_{\rm m}$  mean wind velocity

 $v_{\rm b,0}$  fundamental value of the basic wind velocity

v<sub>b</sub> basic wind velocityw wind pressure

x horizontal distance of the site from the top of a crest

*x-direction* horizontal direction, perpendicular to the span

*y-direction* horizontal direction along the span

 $y_{\text{max}}$  maximum cross-wind amplitude at critical wind speed

z height above ground

 $egin{array}{ll} z_{\text{ave}} & \text{average height} \\ \hline z-direction & \text{vertical direction} \\ z_0 & \text{roughness length} \\ \end{array}$ 

 $z_e$ ,  $z_i$  reference height for external wind action, internal pressure  $z_g$  distance from the ground to the considered component

z<sub>max</sub> maximum height

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## $z_{\min}$ minimum height

## Greek upper case letters

 $\Phi$  upwind slope

 $\Phi_{1,x}$  fundamental alongwind modal shape

 $\theta$  torsional angle

## Greek lower case letters

$lpha_{G}$	galloping instability parameter
$lpha_{IG}$	combined stability parameter of interference galloping
δ	logarithmic decrement of damping
$\delta_{a}$	aerodynamic logarithmic decrement of damping
$\delta_{ extsf{d}}$	logarithmic decrement of damping due to special devices
$\delta_{\! extsf{s}}$	structural logarithmic decrement of damping
$\mathcal{E}$	coefficient
$\mathcal{E}_0$	bandwidth factor
$arepsilon_1$	frequency factor
$\eta$	variable
$\varphi$	solidity ratio, blockage of canopy
λ	slenderness ratio
$\mu$	opening ratio, permeability of a skin
ν	up-crossing frequency, Poisson ratio, kinematic viscosity
$\rho$	air density
$\sigma_{\!\scriptscriptstyle \sf V}$	standard deviation of the turbulence
$\sigma_{\!a,x}$	standard deviation of alongwind acceleration
$\psi_{mc}$	reduction factor for multibay canopies
$\psi_{r}$	reduction factor of force coefficient for square sections with rounded corners
$\psi_{\lambda}$	reduction factor of force coefficient for structural elements with end-effects
$\psi_{\lambdalpha}$	end-effect factor for circular cylinders
$\psi_{S}$	shelter factor for walls and fences
$\psi_{sc}$	reduction factor of force coefficient for scaffoldings effected by solid building face
ζ	exponent of mode shape

## Indices

crit critical

e external, exposure

tr	friction
i	internal, mode number
j	current number of incremental area or point of a structure
m	mean
p	peak, parapet
ref	reference
V	wind velocity
Х	alongwind direction

cross-wind direction

vertical direction

y z

## 2 Design situations

- (1)P The relevant wind actions shall be determined for each design situation identified in accordance with EN 1990, 3.2.
- (2) In accordance with EN 1990, 3.2 (3)P other actions (such as snow, traffic or ice) which will modify the effects due to wind should be taken into account.

NOTE See also EN 1991-1-3, EN 1991-2 and ISO FDIS12494

(3) In accordance with EN 1990, 3.2 (3)P, the changes to the structure during stages of execution (such as different stages of the form of the structure, dynamic characteristics, etc.), which may modify the effects due to wind, should be taken into account.

NOTE See also EN 1991-1-6

(4) Where in design windows and doors are assumed to be shut under storm conditions, the effect of these being open should be treated as an accidental design situation.

NOTE See also EN 1990, 3.2 (2) (P)

(5) Fatigue due to the effects of wind actions should be considered for susceptible structures.

NOTE The number of load cycles may be obtained from Annex B, C and E.

## 3 Modelling of wind actions

## 3.1 Nature

(1) Wind actions fluctuate with time and act directly as pressures on the external surfaces of enclosed structures and, because of porosity of the external surface, also act indirectly on the internal surfaces. They may also act directly on the internal surface of open structures. Pressures act on areas of the surface resulting in forces normal to the surface of the structure or of individual cladding components. Additionally, when large areas of structures are swept by the wind, friction forces acting tangentially to the surface may be significant.

## 3.2 Representations of wind actions

(1) The wind action is represented by a simplified set of pressures or forces whose effects are equivalent to the extreme effects of the turbulent wind.

#### 3.3 Classification of wind actions

(1) Unless otherwise specified, wind actions should be classified as variable fixed actions, see EN 1990, 4.1.1.

## 3.4 Characteristic values

(1) The wind actions calculated using EN 1991-1-4 are characteristic values (See EN 1990, 4.1.2). They are determined from the basic values of wind velocity or the velocity pressure. In accordance with EN 1990 4.1.2 (7)P the basic values are characteristic values having annual probabilities of exceedence of 0,02, which is equivalent to a mean return period of 50 years.

NOTE All coefficients or models, to derive wind actions from basic values, are chosen so that the probability of the calculated wind actions does not exceed the probability of these basic values.

#### 3.5 Models

(1) The effect of the wind on the structure (i.e. the response of the structure), depends on the size, shape and dynamic properties of the structure. This Part covers dynamic response due to along-wind turbulence in resonance with the along-wind vibrations of a fundamental flexural mode shape with constant sign.

The response of structures should be calculated according to Section 5 from the peak velocity pressure,  $q_p$ , at the reference height in the undisturbed wind field, the force and pressure coefficients and the structural factor  $c_s c_d$  (see Section 6).  $q_p$  depends on the wind climate, the terrain roughness and orography, and the reference height.  $q_p$  is equal to the mean velocity pressure plus a contribution from short-term pressure fluctuations.

(2) Aeroelastic response should be considered for flexible structures such as cables, masts, chimneys and bridges.

NOTE Simplified guidance on aeroelastic response is given in Annex E.

## 4 Wind velocity and velocity pressure

#### 4.1 Basis for calculation

(1) The wind velocity and the velocity pressure are composed of a mean and a fluctuating component.

The mean wind velocity  $v_m$  should be determined from the basic wind velocity  $v_b$  which depends on the wind climate as described in 4.2, and the height variation of the wind determined from the terrain roughness and orography as described in 4.3. The peak velocity pressure is determined in 4.5.

The fluctuating component of the wind is represented by the turbulence intensity defined in 4.4.

NOTE The National Annex may provide National climatic information from which the mean wind velocity  $v_m$ , the peak velocity pressure  $q_0$  and additional values may be directly obtained for the terrain categories considered.

#### 4.2 Basic values

(1)P The fundamental value of the basic wind velocity,  $v_{b,0}$ , is the characteristic 10 minutes mean wind velocity, irrespective of wind direction and time of year, at 10 m above ground level in open country terrain with low vegetation such as grass and isolated obstacles with separations of at least 20 obstacle heights.

- NOTE 1 This terrain corresponds to terrain category II in Table 4.1.
- NOTE 2 The value of the basic wind velocity,  $v_{b,0}$ , may be given in the National Annex.
- (2)P The basic wind velocity shall be calculated from Expression (4.1).

$$V_{b} = C_{dir} \cdot C_{season} \cdot V_{b,0} \tag{4.1}$$

where:

 $v_{\rm b}$  is the basic wind velocity, defined as a function of wind direction and time of year at 10 m above ground of terrain category II

 $v_{\rm b,0}$  is the fundamental value of the basic wind velocity, see (1)P

 $c_{\text{dir}}$  is the directional factor, see Note 2.

 $c_{\text{season}}$  is the season factor, see Note 3.

- NOTE 1 Where the influence of altitude on the basic wind velocity  $v_b$  is not included in the specified fundamental value  $v_{b,0}$  the National Annex may give a procedure to take it into account.
- NOTE 2 The value of the directional factor,  $c_{dir}$ , for various wind directions may be found in the National Annex. The recommended value is 1,0.
- NOTE 3 The value of the season factor,  $c_{\text{season}}$ , may be given in the National Annex. The recommended value is 1,0.
- NOTE 4 The 10 minutes mean wind velocity having the probability p for an annual exceedence is determined by multiplying the basic wind velocity  $v_b$  in 4.2 (2)P by the probability factor,  $c_{prob}$  given by Expression (4.2). See also EN 1991-1-6.

$$c_{\text{prob}} = \left(\frac{1 - K \cdot \ln(-\ln(1-p))}{1 - K \cdot \ln(-\ln(0.98))}\right)^{n}$$
(4.2)

where:

K is the shape parameter depending on the coefficient of variation of the extreme-value distribution.

n is the exponent.

NOTE 5 The values for K and n may be given in the National Annex. The recommended values are 0,2 for K and 0,5 for n.

(3) For temporary structures and for all structures in the execution phase, the seasonal factor  $c_{\text{season}}$  may be used. For transportable structures, which may be used at any time in the year,  $c_{\text{season}}$  should be taken equal to 1,0.

NOTE See also EN 1991-1-6.

#### 4.3 Mean wind

## 4.3.1 Variation with height

(1) The mean wind velocity  $v_m(z)$  at a height z above the terrain depends on the terrain roughness and orography and on the basic wind velocity,  $v_b$ , and should be determined using Expression (4.3)

$$V_{\rm m}(z) = c_{\rm r}(z) \cdot c_{\rm o}(z) \cdot V_{\rm b} \tag{4.3}$$

where:

- $c_r(z)$  is the roughness factor, given in 4.3.2
- $c_0(z)$  is the orography factor, taken as 1,0 unless otherwise specified in 4.3.3

NOTE 1 Information on  $c_0$  may be given in the National Annex. If the orography is accounted for in the basic wind velocity, the recommended value is 1,0.

NOTE 2 Design charts or tables for  $v_m(z)$  may be given in the National Annex.

The influence of neighbouring structures on the wind velocity should be considered (see 4.3.4).

## 4.3.2 Terrain roughness

- (1) The roughness factor,  $c_r(z)$ , accounts for the variability of the mean wind velocity at the site of the structure due to:
- the height above ground level
- the ground roughness of the terrain upwind of the structure in the wind direction considered

NOTE The procedure for determining  $c_r(z)$  may be given in the National Annex. The recommended procedure for the determination of the roughness factor at height z is given by Expression (4.4) and is based on a logarithmic velocity profile.

$$c_{r}(z) = k_{r} \cdot \ln \left(\frac{z}{z_{0}}\right) \qquad \text{for} \qquad z_{\min} \leq z \leq z_{\max}$$

$$c_{r}(z) = c_{r}(z_{\min}) \qquad \text{for} \qquad z \leq z_{\min}$$

$$(4.4)$$

where:

 $z_0$  is the roughness length

 $k_r$  terrain factor depending on the roughness length  $z_0$  calculated using

$$k_{\Gamma} = 0.19 \cdot \left(\frac{z_0}{z_{0,|I|}}\right)^{0.07}$$
 (4.5)

where:

 $z_{0,II} = 0.05$  m (terrain category II, Table 4.1)

 $z_{\min}$  is the minimum height defined in Table 4.1

z<sub>max</sub> is to be taken as 200 m, unless otherwise specified in the National Annex

 $z_0$ ,  $z_{min}$  depend on the terrain category. Recommended values are given in Table 4.1 depending on five representative terrain categories.

Expression (4.4) is valid when the upstream distance with uniform terrain roughness is long enough to stabilise the profile sufficiently. See (2).

Table 4.1 — Terrain categories and terrain parameters

Terrain category		<b>z</b> <sub>0</sub>	<b>Z</b> <sub>min</sub>
			m
0	Sea or coastal area exposed to the open sea	0,003	1
I	Lakes or flat and horizontal area with negligible vegetation and without obstacles	0,01	1
II	Area with low vegetation such as grass and isolated obstacles (trees, buildings) with separations of at least 20 obstacle heights	0,05	2
III	Area with regular cover of vegetation or buildings or with isolated obstacles with separations of maximum 20 obstacle heights (such as villages, suburban terrain, permanent forest)	0,3	5
IV	Area in which at least 15 % of the surface is covered with buildings and their average height exceeds 15 m	1,0	10
The terrain categories are illustrated in Annex A.1.			

(2) The terrain roughness to be used for a given wind direction depends on the ground roughness and the distance with uniform terrain roughness in an angular sector around the wind direction. Small areas (less than 10% of the area under consideration) with deviating roughness may be ignored. See Figure 4.1.

NOTE The National Annex may give definitions of the angular sector and of the upstream distance. The recommended value of the angular sector may be taken as the 30° angular sector within ±15° from the wind direction. The recommended value for the upstream distance may be obtained from Annex A.2.

deviating roughness

### Figure 4.1 — Assessment of terrain roughness

- (3) When a pressure or force coefficient is defined for a nominal angular sector, the lowest roughness length within any 30° angular wind sector should be used.
- (4) When there is choice between two or more terrain categories in the definition of a given area, then the area with the lowest roughness length should be used.

## 4.3.3 Terrain orography

(1) Where orography (e.g. hills, cliffs etc.) increases wind velocities by more than 5% the effects should be taken into account using the orography factor  $c_0$ .

NOTE The procedure to be used for determining  $c_0$  may be given in the National Annex. The recommended procedure is given in Annex A.3.

(2) The effects of orography may be neglected when the average slope of the upwind terrain is less than 3°. The upwind terrain may be considered up to a distance of 10 times the height of the isolated orographic feature.

## 4.3.4 Large and considerably higher neighbouring structures

(1) If the structure is to be located close to another structure, that is at least twice as high as the average height of its neighbouring structures, then it could be exposed (dependent on the properties of the structure) to increased wind velocities for certain wind directions. Such cases should be taken into account.

NOTE The National Annex may give a procedure to take account of this effect. A recommended conservative first approximation is given in Annex A.4.

## 4.3.5 Closely spaced buildings and obstacles

(1) The effect of closely spaced buildings and other obstacles may be taken into account.

NOTE The National Annex may give a procedure. A recommended first approximation is given in Annex A.5. In rough terrain closely spaced buildings modify the mean wind flow near the ground, as if the ground level was raised to a height called displacement height  $h_{\rm dis}$ .

#### 4.4 Wind turbulence

(1) The turbulence intensity  $I_v(z)$  at height z is defined as the standard deviation of the turbulence divided by the mean wind velocity.

NOTE 1 The turbulent component of wind velocity has a mean value of 0 and a standard deviation  $\sigma_V$ . The standard deviation of the turbulence  $\sigma_V$  may be determined using Expression (4.6).

$$\sigma_{\rm v} = k_{\rm r} \cdot v_{\rm h} \cdot k_{\rm l} \tag{4.6}$$

For the terrain factor  $k_r$  see Expression (4.5), for the basic wind velocity  $v_b$  see Expression (4.1) and for turbulence factor  $k_l$  see Note 2.

NOTE 2 The recommended rules for the determination of  $I_v(z)$  are given in Expression (4.7)

$$I_{v}(z) = \frac{\sigma_{v}}{v_{m}(z)} = \frac{k_{l}}{c_{o}(z) \cdot \ln(z/z_{0})} \quad \text{for} \qquad z_{min} \le z \le z_{max}$$

$$I_{v}(z) = I_{v}(z_{min}) \quad \text{for} \quad z < z_{min}$$

$$(4.7)$$

where:

 $k_1$  is the turbulence factor. The value of  $k_1$  may be given in the National Annex. The recommended value is  $k_1 = 1,0$ .

c<sub>o</sub> is the orography factor as described in 4.3.3

 $z_0$  is the roughness length, given in Table 4.1

## 4.5 Peak velocity pressure

(1) The peak velocity pressure  $q_p(z)$  at height z, which includes mean and short-term velocity fluctuations, should be determined.

NOTE 1 The National Annex may give rules for the determination of  $q_p(z)$ . The recommended rule is given in Expression (4.8).

$$q_{p}(z) = [1 + 7 \cdot I_{v}(z)] \cdot \frac{1}{2} \cdot \rho \cdot V_{m}^{2}(z) = c_{e}(z) \cdot q_{b}$$
 (4.8)

where:

 $\rho$  is the air density, which depends on the altitude, temperature and barometric pressure to be expected in the region during wind storms

 $c_{\rm e}(z)$  is the exposure factor given in Expression (4.9)

$$C_{\rm e}(z) = \frac{q_{\rm p}(z)}{q_{\rm b}} \tag{4.9}$$

 $q_b$  is the basic velocity pressure given in Expression (4.10)

$$q_{\rm b} = \frac{1}{2} \cdot \rho \cdot V_{\rm b}^2 \tag{4.10}$$

The value 7 in Expression (4.8) is based on a peak factor equal to 3,5 and is consistent with the values of the pressure and force coefficients in Section 7.

For flat terrain where  $c_0(z)$  = 1,0 (see 4.3.3), the exposure factor  $c_e(z)$  is illustrated in Figure 4.2 as a function of height above terrain and a function of terrain category as defined in Table 4.1.

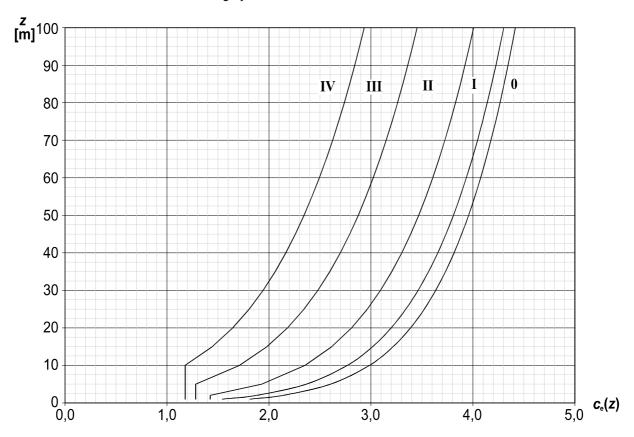


Figure 4.2 — Illustrations of the exposure factor  $c_e(z)$  for  $c_0$ =1,0,  $k_i$ =1,0

NOTE 2 The values for  $\rho$  may be given in the National Annex. The recommended value is 1,25 kg/m<sup>3</sup>.

## 5 Wind actions

#### 5.1 General

(1)P Wind actions on structures and structural elements shall be determined taking account of both external and internal wind pressures.

NOTE A summary of calculation procedures for the determination of wind actions is given in Table 5.1.

Table 5.1 —Calculation procedures for the determination of wind actions

Parameter	Subject Reference
peak velocity pressure $q_{ m p}$	
basic wind velocity $v_{ m b}$	4.2 (2)P
reference height $z_{\rm e}$	Section 7
terrain category	Table 4.1
characteristic peak velocity pressure $q_{ m p}$	4.5 (1)
turbulence intensity $I_{\rm v}$	4.4
mean wind velocity $v_{ m m}$	4.3.1
orography coefficient $c_{\circ}(z)$	4.3.3
roughness coefficient $c_{\rm r}(z)$	4.3.2
Wind pressures, e.g. for cladding, fixings and structural parts	
internal pressure coefficient $c_{ m pi}$	Section 7
external pressure coefficient $c_{ m pe}$	Section 7
external wind pressure: $w_{ m e} = q_{ ho} \; c_{ m pe}$	5.2 (1)
internal wind pressure: $w_i = q_p c_{pi}$	5.2 (2)
Wind forces on structures, e.g. for overall wind effects	
structural factor: $c_{ m s}c_{ m d}$	6
wind force $F_{W}$ calculated from force coefficients	5.3 (2)
wind force $F_{ m W}$ calculated from pressure coefficients	5.3 (3)

## 5.2 Wind pressure on surfaces

(1) The wind pressure acting on the external surfaces,  $w_e$ , should be obtained from Expression (5.1).

$$W_{\rm e} = q_{\rm p}(z_{\rm e}) \cdot c_{\rm pe} \tag{5.1}$$

where:

 $q_{\rm p}(z_{\rm e})$  is the peak velocity pressure

z<sub>e</sub> is the reference height for the external pressure given in Section 7

 $c_{\rm pe}$  is the pressure coefficient for the external pressure, see Section 7.

NOTE  $q_p(z)$  is defined in 4.5

(2) The wind pressure acting on the internal surfaces of a structure,  $w_i$ , should be obtained from Expression (5.2)

$$W_{i} = q_{p}(z_{i}) \cdot c_{pi} \tag{5.2}$$

where:

- $q_p(z_i)$  is the peak velocity pressure
- z<sub>i</sub> is the reference height for the internal pressure given in Section 7
- $c_{pi}$  is the pressure coefficient for the internal pressure given in Section 7

NOTE  $q_p(z)$  is defined in 4.5

(3) The net pressure on a wall, roof or element is the difference between the pressures on the opposite surfaces taking due account of their signs. Pressure, directed towards the surface is taken as positive, and suction, directed away from the surface as negative. Examples are given in Figure 5.1.

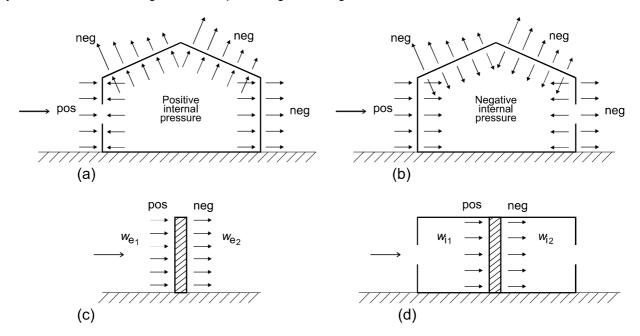


Figure 5.1 — Pressure on surfaces

#### 5.3 Wind forces

- (1) The wind forces for the whole structure or a structural component should be determined:
- by calculating forces using force coefficients (see (2)) or
- by calculating forces from surface pressures (see (3))
- (2) The wind force  $F_w$  acting on a structure or a structural component may be determined directly by using Expression (5.3)

$$F_{\rm w} = c_{\rm s} c_{\rm d} \cdot c_{\rm f} \cdot q_{\rm p}(z_{\rm e}) \cdot A_{\rm ref} \tag{5.3}$$

or by vectorial summation over the individual structural elements (as shown in 7.2.2) by using Expression (5.4)

$$F_{\rm w} = c_{\rm s} c_{\rm d} \cdot \sum_{\rm elements} c_{\rm f} \cdot q_{\rm p}(z_{\rm e}) \cdot A_{\rm ref} \tag{5.4}$$

where:

 $c_{\rm s}c_{\rm d}$  is the structural factor as defined in Section 6

c<sub>f</sub> is the force coefficient for the structure or structural element, given in Section 7 or Section 8

 $q_p(z_e)$  is the peak velocity pressure (defined in 4.5) at reference height  $z_e$  (defined in Section 7 or Section 8)

A<sub>ref</sub> is the reference area of the structure or structural element, given in Section 7 or Section 8

NOTE Section 7 gives  $c_f$  values for structures or structural elements such as prisms, cylinders, roofs, signboards, plates and lattice structures etc. These values include friction effects. Section 8 gives  $c_f$  values for bridges.

(3) The wind force,  $F_{\rm w}$  acting on a structure or a structural element may be determined by vectorial summation of the forces  $F_{\rm w,e}$ ,  $F_{\rm w,i}$  and  $F_{\rm fr}$  calculated from the external and internal pressures using Expressions (5.5) and (5.6) and the frictional forces resulting from the friction of the wind parallel to the external surfaces, calculated using Expression (5.7).

external forces:

$$F_{\rm w,e} = c_{\rm s} c_{\rm d} \cdot \sum_{\rm surfaces} w_{\rm e} \cdot A_{\rm ref} \tag{5.5}$$

internal forces:

$$F_{w,i} = \sum_{\text{surfaces}} w_i \cdot A_{\text{ref}} \tag{5.6}$$

friction forces:

$$F_{\rm fr} = c_{\rm fr} \cdot q_{\rm p}(z_{\rm e}) \cdot A_{\rm fr} \tag{5.7}$$

where:

 $c_{\rm s}c_{\rm d}$  is the structural factor as defined in Section 6

 $w_e$  is the external pressure on the individual surface at height  $z_e$ , given in Expression (5.1)

 $w_i$  is the internal pressure on the individual surface at height  $z_i$ , given in Expression (5.2)

A<sub>ref</sub> is the reference area of the individual surface

 $c_{\rm fr}$  is the friction coefficient derived from 7.5

 $A_{\rm fr}$  is the area of external surface parallel to the wind, given in 7.5.

NOTE 1 For elements (e.g. walls, roofs), the wind force becomes equal to the difference between the external and internal resulting forces.

NOTE 2 Friction forces F<sub>fr</sub> act in the direction of the wind components parallel to external surfaces.

(4) The effects of wind friction on the surface can be disregarded when the total area of all surfaces parallel with (or at a small angle to) the wind is equal to or less than 4 times the total area of all external surfaces perpendicular to the wind (windward and leeward).

(5) In the summation of the wind forces acting on building structures, the lack of correlation of wind pressures between the windward and leeward sides may be taken into account.

NOTE The National Annex may determine whether this lack of correlation may be applied generally or be restricted to walls as applied in 7.2.2 (3). It is recommended to consider the lack of correlation only for walls (see 7.2.2 (3)).

## 6 Structural factor c<sub>s</sub>c<sub>d</sub>

#### 6.1 General

(1) The structural factor  $c_s c_d$  should take into account the effect on wind actions from the non-simultaneous occurrence of peak wind pressures on the surface together with the effect of the vibrations of the structure due to turbulence.

NOTE The structural factor  $c_s c_d$  may be separated into a size factor  $c_s$  and a dynamic factor  $c_d$ , based on 6.3. Information on whether the structural factor  $c_s c_d$  should be separated or not may be given in the National Annex.

## 6.2 Determination of $c_s c_d$

- (1)  $c_s c_d$  should be determined as follows:
- a) For buildings with a height less than 15 m the value of  $c_{\rm s}c_{\rm d}$  may be taken as 1.
- b) For facade and roof elements having a natural frequency greater than 5 Hz, the value of  $c_{\rm s}c_{\rm d}$  may be taken as
- c) For framed buildings which have structural walls and which are less than 100 m high and whose height is less than 4 times the in-wind depth, the value of  $c_s c_d$  may be taken as 1.
- d) For chimneys with circular cross-sections whose height is less than 60 m and 6,5 times the diameter, the value of  $c_s c_d$  may be taken as 1.
- e) Alternatively, for cases a), b), c) and d) above, values of  $c_s c_d$  may be derived from 6.3.1.
- f) For civil engineering works (other than bridges, which are considered in Section 8), and chimneys and buildings outside the limitations given in c) and d) above,  $c_s c_d$  should be derived either from 6.3 or taken from Annex D.
  - NOTE 1 Natural frequencies of facade and roof elements may be calculated using Annex F (glazing spans smaller than 3 m usually lead to natural frequencies greater than 5 Hz)
  - NOTE 2 The figures in Annex D give values of  $c_s c_d$  for various types of structures. The figures give envelopes of safe values calculated from models complying with the requirements in 6.3.1.

### 6.3 Detailed procedure

## 6.3.1 Structural factor $c_s c_d$

(1) The detailed procedure for calculating the structural factor  $c_s c_d$  is given in Expression (6.1). This procedure can only be used if the conditions given in 6.3.1 (2) apply.

$$c_{s}c_{d} = \frac{1 + 2 \cdot k_{p} \cdot I_{v}(z_{e}) \cdot \sqrt{B^{2} + R^{2}}}{1 + 7 \cdot I_{v}(z_{e})}$$
(6.1)

where:

- $z_e$  is the reference height, see Figure 6.1. For structures where Figure 6.1 does not apply  $z_e$  may be equal to h, the height of the structure.
- $k_p$  is the peak factor defined as the ratio of the maximum value of the fluctuating part of the response to its standard deviation
- $I_{\rm v}$  is the turbulence intensity defined in 4.4

- $B^2$  is the background factor, allowing for the lack of full correlation of the pressure on the structure surface
- $R^2$  is the resonance response factor, allowing for turbulence in resonance with the vibration mode

NOTE 1 The size factor  $c_s$  takes into account the reduction effect on the wind action due to the non-simultaneity of occurrence of the peak wind pressures on the surface and may be obtained from Expression (6.2):

$$c_{s} = \frac{1 + 7 \cdot I_{v}(z_{e}) \cdot \sqrt{B^{2}}}{1 + 7 \cdot I_{v}(z_{e})}$$
(6.2)

NOTE 2 The dynamic factor  $c_d$  takes into account the increasing effect from vibrations due to turbulence in resonance with the structure and may be obtained from Expression (6.3):

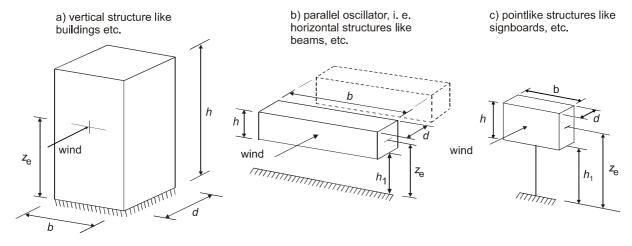
$$c_{d} = \frac{1 + 2 \cdot k_{p} \cdot I_{v}(z_{e}) \cdot \sqrt{B^{2} + R^{2}}}{1 + 7 \cdot I_{v}(z_{e}) \cdot \sqrt{B^{2}}}$$
(6.3)

NOTE 3 The procedure to be used to determine  $k_p$ , B and R may be given in the National Annex. A recommended procedure is given in Annex B. An alternative procedure is given in Annex C. As an indication to the users the differences in  $c_s c_d$  using Annex C compared to Annex B does not exceed approximately 5%.

(2)P Expression (6.1) shall only be used if all of the following requirements are met:

- the structure corresponds to one of the general shapes shown in Figure 6.1,
- only the along-wind vibration in the fundamental mode is significant, and this mode shape has a constant sign.

NOTE The contribution to the response from the second or higher alongwind vibration modes is negligible.



NOTE Limitations are also given in 1.1 (2)

$$z_{e} = 0.6 \cdot h \ge z_{min}$$
  $z_{e} = h_{1} + \frac{h}{2} \ge z_{min}$   $z_{e} = h_{1} + \frac{h}{2} \ge z_{min}$ 

Figure 6.1 — General shapes of structures covered by the design procedure. The structural dimensions and the reference height used are also shown.

### 6.3.2 Serviceability assessments

(1) For serviceability assessments, the maximum along-wind displacement and the standard deviation of the characteristic along-wind acceleration of the structure at height z should be used. For the maximum along-wind displacement the equivalent static wind force defined in 5.2 should be used.

NOTE The National Annex may give a method for determining the along-wind displacement and the standard deviation of the along-wind acceleration. The recommended method is given in Annex B. An alternative method is given in Annex C.

## 6.3.3 Wake buffeting

- (1) For slender buildings (h/d > 4) and chimneys (h/d > 6.5) in tandem or grouped arrangement, the effect of increased turbulence in the wake of nearby structures (wake buffeting) should be taken into account.
- (2) Wake buffeting effects may be assumed to be negligible if at least one of the following conditions applies:
- The distance between two buildings or chimneys is larger than 25 times the cross wind dimension of the upstream building or chimney.
- The natural frequency of the downstream building or chimney is higher than 1 Hz.

NOTE If 6.3.3 (2) is not fulfilled wind tunnel tests or specialist advice is recommended.

## 7 Pressure and force coefficients

#### 7.1 General

- (1) This section should be used to determine the appropriate aerodynamic coefficients for structures. Depending on the structure the appropriate aerodynamic coefficient will be:
- Internal and external pressure coefficients, see 7.1.1 (1),
- Net pressure coefficients, see 7.1.1 (2),
- Friction coefficients, see 7.1.1 (3),
- Force coefficients, see 7.1.1 (4).

## 7.1.1 Choice of aerodynamic coefficient

- (1) Pressure coefficients should be determined for:
- Buildings, using 7.2 for both internal and external pressures, and for
- Circular cylinders, using 7.2.9 for the internal pressures and 7.9.1 for the external pressures
  - NOTE 1 External pressure coefficients give the effect of the wind on the external surfaces of buildings; internal pressure coefficients give the effect of the wind on the internal surfaces of buildings.
  - NOTE 2 The external pressure coefficients are divided into overall coefficients and local coefficients. Local coefficients give the pressure coefficients for loaded areas of 1  $\text{m}^2$ . They may be used for the design of small elements and fixings. Overall coefficients give the pressure coefficients for loaded areas of 10  $\text{m}^2$ . They may be used for loaded areas larger than 10  $\text{m}^2$ .
- (2) Net pressure coefficients should be determined for:
- Canopy roofs, using 7.3
- Free-standing walls, parapets and fences using 7.4
  - NOTE Net pressure coefficients give the resulting effect of the wind on a structure, structural element or component per unit area.
- (3) Friction coefficients should be determined for walls and surfaces defined in 5.2 (3), using 7.5.
- (4) Force coefficients should be determined for:
- Signboards, using 7.4.3,
- Structural elements with rectangular cross section, using 7.6,
- Structural elements with sharp edged section, using 7.7,
- Structural elements with regular polygonal section, using 7.8,
- Circular cylinders, using 7.9.2 and 7.9.3,
- Spheres, using 7.10,

- Lattice structures and scaffoldings, using 7.11,
- Flags, using 7.12.

A reduction factor depending on the effective slenderness of the structure may be applied, using 7.13.

NOTE Force coefficients give the overall effect of the wind on a structure, structural element or component as a whole, including friction, if not specifically excluded.

## 7.1.2 Asymmetric and counteracting pressures and forces

- (1) If instantaneous fluctuations of wind over surfaces can give rise to significant asymmetry of loading and the structural form is likely to be sensitive to such loading (e.g. torsion in nominally symmetric single core buildings) then their effect should be taken into account.
- (2) For buildings, free-standing canopies and signboards, 7.2, 7.3 and 7.4 should be applied.

NOTE The National Annex may give procedures for other structures. The recommended procedures are:

a) For rectangular structures that are susceptible to torsional effects the pressure distribution given in Figure 7.1 should be applied for the representation of the torsional effects due to an inclined wind or due to lack of correlation between wind forces acting at different places on the structure.

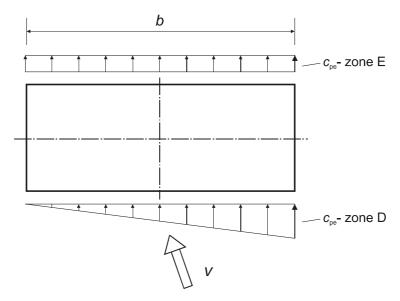


Figure 7.1 — Pressure distribution used to take torsional effects into account. The zones and values for  $c_{pe}$  are given in Table 7.1 and Figure 7.5.

b) For other cases an allowance for asymmetry of loading should be made by completely removing the design wind action from those parts of the structure where its action will produce a beneficial effect.

## 7.1.3 Effects of ice and snow

(1) If ice or snow alters the geometry of a structure so that it changes the reference area or shape, this should be taken into account.

NOTE Further information may be given in the National Annex.

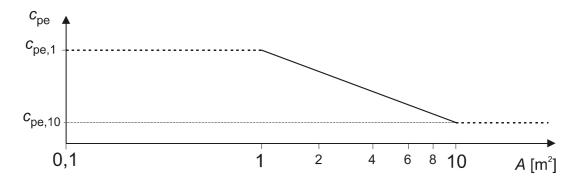
## 7.2 Pressure coefficients for buildings

#### 7.2.1 General

(1) The external pressure coefficients  $c_{\rm pe}$  for buildings and parts of buildings depend on the size of the loaded area A, which is the area of the structure, that produces the wind action in the section to be calculated. The external pressure coefficients are given for loaded areas A of 1 m<sup>2</sup> and 10 m<sup>2</sup> in the tables for the appropriate building configurations as  $c_{\rm pe,1}$ , for local coefficients, and  $c_{\rm pe,10}$ , for overall coefficients, respectively.

NOTE 1 Values for  $c_{\rm pe,1}$  are intended for the design of small elements and fixings with an area per element of 1 m<sup>2</sup> or less such as cladding elements and roofing elements. Values for  $c_{\rm pe,10}$  may be used for the design of the overall load bearing structure of buildings.

NOTE 2 The National Annex may give a procedure for calculating external pressure coefficients for loaded areas above 1  $\text{m}^2$  based on external pressure coefficients  $c_{\text{pe},1}$  and  $c_{\text{pe},10}$ . The recommended procedure for loaded areas up to 10  $\text{m}^2$  is given in Figure 7.2.



The figure is based on the following: for 1 m<sup>2</sup> < A < 10 m<sup>2</sup>  $c_{pe} = c_{pe,1} - (c_{pe,1} - c_{pe,10}) \log_{10} A$ 

Figure 7.2 — Recommended procedure for determining the external pressure coefficient  $c_{\rm pe}$  for buildings with a loaded area A between 1 m<sup>2</sup> and 10 m<sup>2</sup>

- (2) The values  $c_{\text{pe},10}$  and  $c_{\text{pe},1}$  in Tables 7.2 to 7.5 should be used for the orthogonal wind directions 0°, 90°, 180°. These values represent the most unfavourable values obtained in a range of wind direction  $\Theta = \pm 45^{\circ}$  either side of the relevant orthogonal direction.
- (3) For protruding roof corners the pressure on the underside of the roof overhang is equal to the pressure for the zone of the vertical wall directly connected to the protruding roof; the pressure at the top side of the roof overhang is equal to the pressure of the zone, defined for the roof.

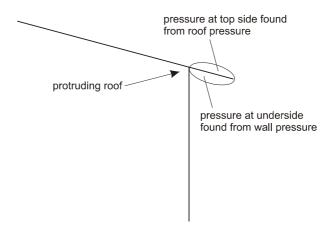
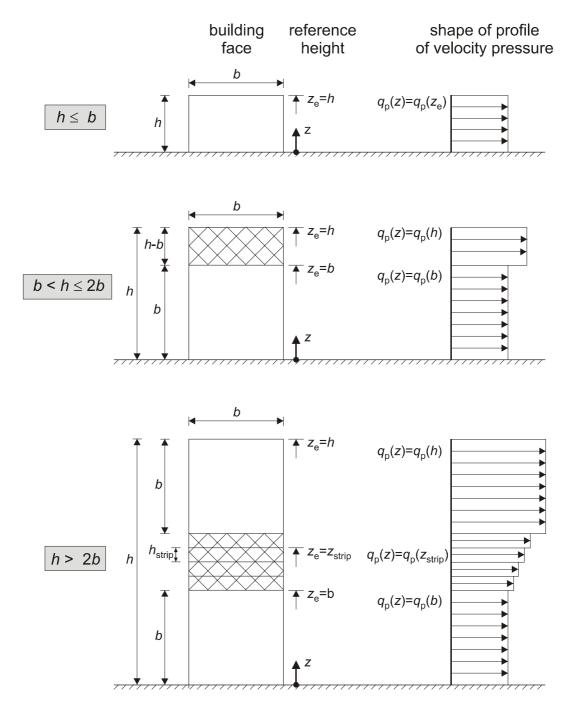


Figure 7.3 — Illustration of relevant pressures for protruding roofs

## 7.2.2 Vertical walls of rectangular plan buildings

- (1) The reference heights,  $z_e$ , for windward walls of rectangular plan buildings (zone D, see Figure 7.5) depend on the aspect ratio h/b and are always the upper heights of the different parts of the walls. They are given in Figure 7.4 for the following three cases:
- A building, whose height h is less than b should be considered to be one part.
- A building, whose height h is greater than b, but less than 2b, may be considered to be two parts, comprising: a lower part extending upwards from the ground by a height equal to b and an upper part consisting of the remainder.
- A building, whose height h is greater than 2b may be considered to be in multiple parts, comprising: a lower part extending upwards from the ground by a height equal to b; an upper part extending downwards from the top by a height equal to b and a middle region, between the upper and lower parts, which may be divided into horizontal strips with a height h<sub>strip</sub> as shown in Figure 7.4.

NOTE The rules for the velocity pressure distribution for leeward wall and sidewalls (zones A, B, C and E, see Figure 7.5) may be given in the National Annex or be defined for the individual project. The recommended procedure is to take the reference height as the height of the building.



NOTE The velocity pressure should be assumed to be uniform over each horizontal strip considered.

Figure 7.4 — Reference height,  $z_e$ , depending on h and b, and corresponding velocity pressure profile

(2) The external pressure coefficients  $c_{\rm pe,10}$  and  $c_{\rm pe,1}$  for zone A, B, C, D and E are defined in Figure 7.5.

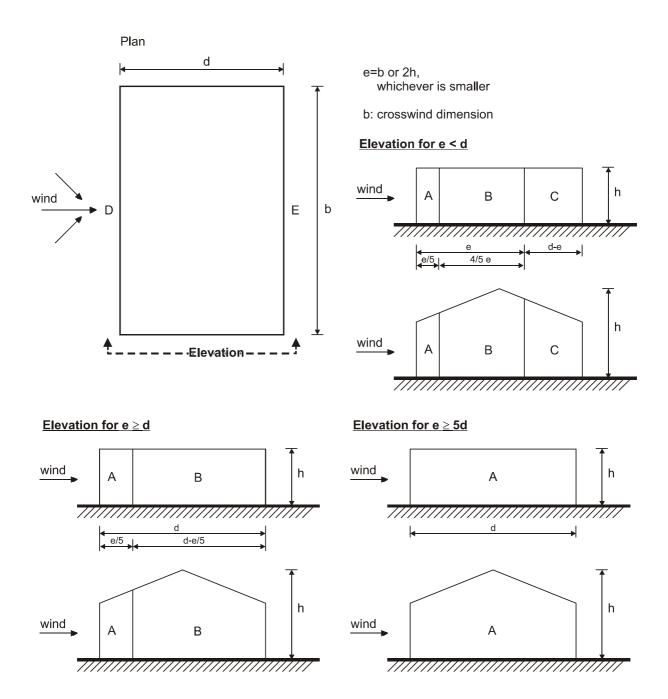


Figure 7.5 — Key for vertical walls

NOTE 1 The values of  $c_{\text{pe},10}$  and  $c_{\text{pe},1}$  may be given in the National Annex. The recommended values are given in Table 7.1, depending on the ratio h/d. For intermediate values of h/d, linear interpolation may be applied. The values of Table 7.1 also apply to walls of buildings with inclined roofs, such as duopitch and monopitch roofs.

Table 7.1 — Recommended values of external pressure coefficients for vertical walls of
rectangular plan buildings

Zone	Α		В		С		D		E	
h/d	<b>C</b> pe,10	<b>C</b> pe,1	<b>C</b> pe,10	<b>C</b> pe,1	<b>C</b> pe,10	<b>C</b> pe,1	<b>C</b> pe,10	C <sub>pe,1</sub>	C <sub>pe,10</sub>	<b>C</b> pe,1
5	-1,2	-1,4	-0,8	-1,1	-0,5		+0,8	+1,0	-0,7	
1	-1,2	-1,4	-0,8	-1,1	-0	-0,5		+1,0	-0,5	
≤ 0,25	-1,2	-1,4	-0,8	-1,1	-0	),5	+0,7	+1,0	-0	,3

NOTE 2 For buildings with h/d > 5, the total wind loading may be based on the provisions given in Sections 7.6 to 7.8 and 7.9.2.

(3) In cases where the wind force on building structures is determined by application of the pressure coefficients  $c_{\rm pe}$  on windward and leeward side (zones D and E) of the building simultaneously, the lack of correlation of wind pressures between the windward and leeward side may have to be taken into account.

NOTE The lack of correlation of wind pressures between the windward and leeward side may be considered as follows. For buildings with  $h/d \ge 5$  the resulting force is multiplied by 1. For buildings with  $h/d \le 1$ , the resulting force is multiplied by 0,85. For intermediate values of h/d, linear interpolation may be applied.

### 7.2.3 Flat roofs

- (1) Flat roofs are defined as having a slope ( $\alpha$ ) of –5°<  $\alpha$  < 5°
- (2) The roof should be divided into zones as shown in Figure 7.6.
- (3) The reference height for flat roof and roofs with curved or mansard eaves should be taken as h. The reference height for flat roofs with parapets should be taken as  $h + h_0$ , see Figure 7.6.
- (4) Pressure coefficients for each zone are given in Table 7.2.
- (5) The resulting pressure coefficient on the parapet should be determined using 7.4.

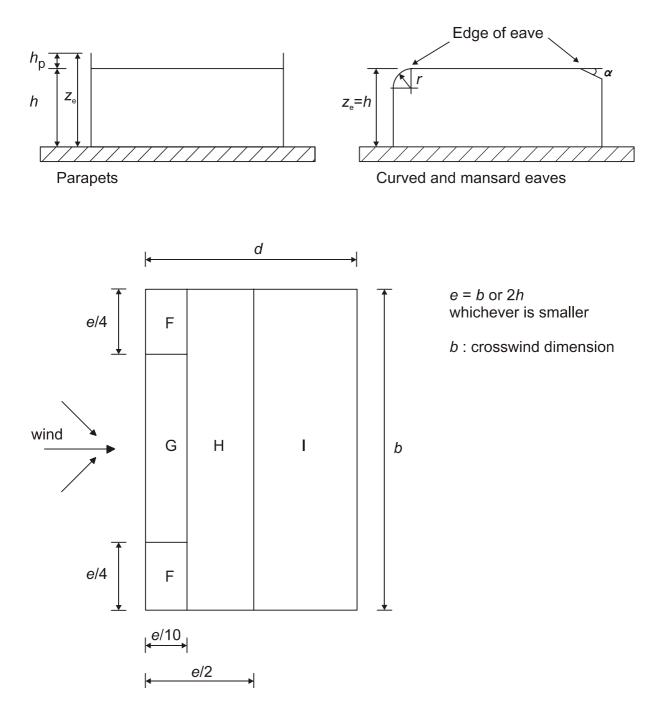


Figure 7.6 — Key for flat roofs

Table 7.2 — External pressure coefficients for flat roofs

					7	Zone			
Roof	type	ı	=	(	3		Н	I	
		<b>c</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>						
Sharp eaves		-1,8	-2,5	-1,2	-2,0	-0,7	-1,2	+0	,2
Charp caves	T	1,0	2,0	1,2	2,0	0,1	.,_	-0	,2
	h <sub>p</sub> /h=0,025	-1,6	-2,2	-1,1	-1,8	-0,7	-1,2	+0	,2
	р 2,22	.,-	_,_	.,.	,,,	-,-		-0,2	
With	h <sub>p</sub> /h=0,05	-1,4	-2,0	-0,9	-1,6	-0,7	-1,2	+0	
Parapets	, ·	,	,	,	,			-0	
	h <sub>p</sub> /h=0,10	-1,2	-1,8	-0,8	-1,4	-0,7	-1,2	+0	
	·							-0,2	
	<i>r</i> / <i>h</i> = 0,05	-1,0	-1,5	-1,2	-1,8	-0,4		+0	
								-0,2	
Curved	<i>r</i> / <i>h</i> = 0,10	-0,7	-1,2	-0,8	-1,4	-(	0,3	+0	
Eaves								-0	
	<i>r/h</i> = 0,20	-0,5	-0,8	-0,5	-0,8	-(	0,3	+0	
								-0	,2
	α = 30°	-1,0	-1,5	-1,0	-1,5	-(	0,3	+0	
		,		,	,			-0	,2
Mansard	$\alpha = 45^{\circ}$	-1,2	-1,8	-1,3	-1,9	-(	0,4	+0	
Eaves		,-	,-	,-	,-	-0,-		-0	,2
	$\alpha = 60^{\circ}$	-1,3	-1,9	-1,3	-1,9	_(	),5	+0	,2
	<i>α</i> = 60°	1,0	1,0	.,0	.,0	)	,,,	-0	,2

NOTE 1 For roofs with parapets or curved eaves, linear interpolation may be used for intermediate values of  $h_p/h$  and r/h.

NOTE 2 For roofs with mansard eaves, linear interpolation between  $\alpha$  = 30°, 45° and  $\alpha$  = 60° may be used. For  $\alpha$  > 60° linear interpolation between the values for  $\alpha$  = 60° and the values for flat roofs with sharp eaves may be used.

NOTE 3 In Zone I, where positive and negative values are given, both values shall be considered.

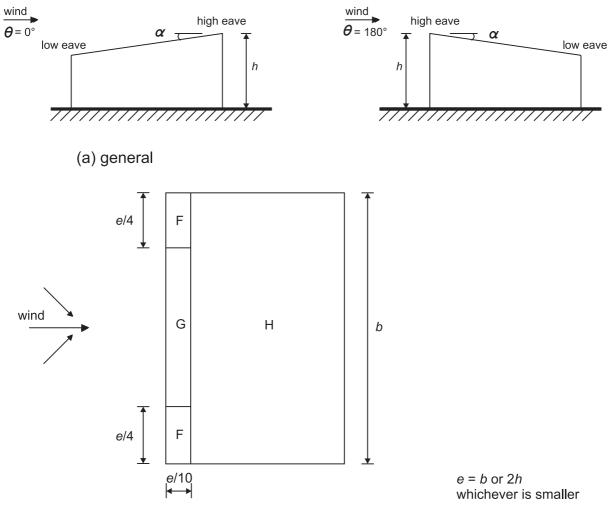
NOTE 4 For the mansard eave itself, the external pressure coefficients are given in Table 7.4 "External pressure coefficients for duopitch roofs: wind direction  $0^{\circ}$ ", Zone F and G, depending on the pitch angle of the mansard eave.

NOTE 5 For the curved eave itself, the external pressure coefficients are given by linear interpolation along the curve, between values on the wall and on the roof.

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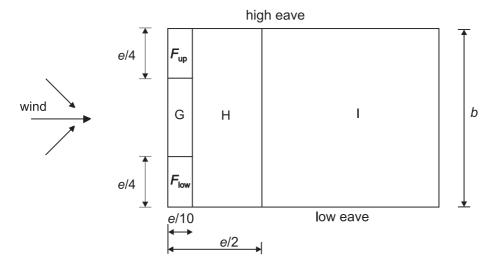
# 7.2.4 Monopitch roofs

- (1) The roof, including protruding parts, should be divided into zones as shown in Figure 7.7.
- (2) The reference height  $z_{\rm e}$  should be taken equal to h.
- (3) The pressure coefficients for each zone that should be used are given in Table 7.3.



(b) wind directions  $\theta$  = 0° and  $\theta$  = 180°

b: crosswind dimension



(c) wind direction  $\theta$ = 90°

Figure 7.7 — Key for monopitch roofs

Table 7.3a — External pressure coefficients for monopitch roofs

	Z	Zone fo	r wind c	lirectio	on <i>⊚</i> = 0	0	Zo	ne for	wind di	irection	<i>⊕</i> = 180	)°
Pitch Angle α	F	=	G	G		н		F		G		
79.0 3	C <sub>pe,10</sub>	C <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	C <sub>pe,10</sub>	<i>C</i> <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	C <sub>pe,10</sub>	C <sub>pe,1</sub>	C <sub>pe,10</sub>	C <sub>pe,1</sub>
5°	-1,7	-2,5	-1,2	-2,0	-0,6 -1,2		-2,3	-2,5	1 2	2.0	-0,8	-1,2
5	+0	),0	+0	,0	+0,0		-2,3		-1,3	-2,0	-0,0	
15°	-0,9	-2,0	-0,8	-1,5	-0,3		2.5	20	1 2	2.0	0.0	1.2
	+0	),2	+0	,2	+ 0,2		-2,5	-2,8	-1,3	-2,0	-0,9	-1,2
30°	-0,5	-1,5	-0,5	-1,5	-0,2		-1,1	-2,3	-0,8	-1,5	-0,	0
30	+0	),7	+0	,7	+0	),4	-1,1	-2,3	-0,6	-1,5	-0,	.0
45°	-0	,0	-0,	0	-0	-0,0		-1,3	0	,5	-0,	7
43	+0	),7	+0	,7	+0,6		-0,6	-1,3	1	,,5	-0,	,7
60°	+(	),7	+0	,7	+0,7		-0,5	-1,0	-0	,5	-0,	5
75°	+(	),8	+0	,8	+0	+0,8		-1,0	-0	,5	-0,	5

Table 7.3b — External pressure coefficients for monopitch roofs

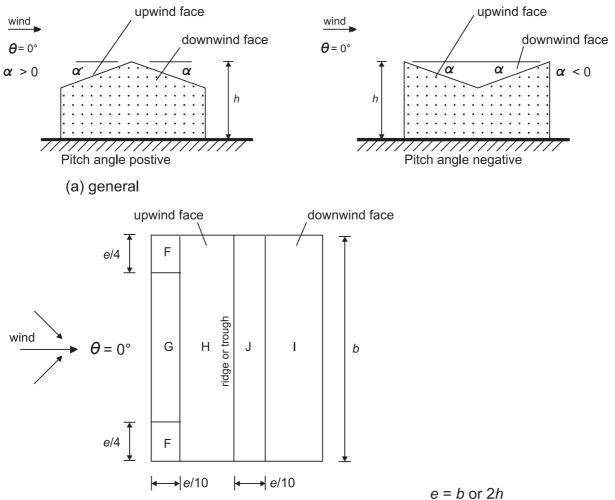
				Zone f	or wind d	lirection	<i>⊕</i> = 90°				
Pitch Angle $\alpha$	F <sub>up</sub>		F <sub>low</sub>		G	G			I		
	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>C</b> pe,1							
5°	-2,1	-2,6	-2,1	-2,4	-1,8	-2,0	-0,6	-1,2	-0,5		
15°	-2,4	-2,9	-1,6	-2,4	-1,9	-2,5	-0,8	-1,2	-0,7	-1,2	
30°	-2,1	-2,9	-1,3	-2,0	-1,5	-2,0	-1,0	-1,3	-0,8	-1,2	
45°	-1,5	-2,4	-1,3	-2,0	-1,4	-2,0	-1,0	-1,3	-0,9	-1,2	
60°	-1,2	-2,0	-1,2	-2,0	-1,2	-2,0	-1,0	-1,3	-0,7	-1,2	
75°	-1,2	-2,0	-1,2	-2,0	-1,2	-2,0	-1,0	-1,3	-0	,5	

NOTE 1 At  $\Theta$  = 0° (see table a)) the pressure changes rapidly between positive and negative values around a pitch angle of  $\alpha$  = +5° to +45°, so both positive and negative values are given. For those roofs, two cases should be considered: one with all positive values, and one with all negative values. No mixing of positive and negative values is allowed on the same face.

NOTE 2 Linear interpolation for intermediate pitch angles may be used between values of the same sign. The values equal to 0.0 are given for interpolation purposes

# 7.2.5 Duopitch roofs

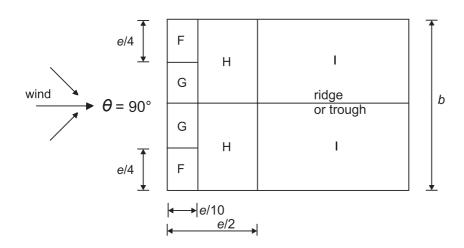
- (1) The roof, including protruding parts, should be divided in zones as shown in Figure 7.8.
- (2) The reference height  $z_e$  should be taken as h.
- (3) The pressure coefficients for each zone that should be used are given in Table 7.4.



(b) wind direction  $\theta = 0^{\circ}$ 

*e* = *b* or 2*h* whichever is smaller

b: crosswind dimension



(c) wind direction  $\theta$ = 90°

Figure 7.8 — Key for duopitch roofs

Table 7.4a — External pressure coefficients for duopitch roofs

Ditala				Zone	for wind	directio	n <i>⊕</i> = 0°							
Pitch Angle $lpha$	!	F	(	3	Н		I							
Aligie a	<b>C</b> <sub>pe,10</sub>	C <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	C <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>	C <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>				
-45°	-(	),6	-0,6		-0,8		-0,7		-0,7		-1,0	-1,5		
-30°	-1,1	-2,0	-0,8	-1,5	-0,	8	-0,	6	-0,8	-1,4				
-15°	-2,5	-2,8	-1,3	-2,0	-0,9	-1,2	-0,	5	-0,7	-1,2				
-5°	0.0	2.5	1.0	10 00 15		+0,2		+0,2						
-5-	-2,3	-2,5	-1,2	-2,0	-0,8	-1,2	-0,6		-0,6					
5°	-1,7	-2,5	-1,2	-2,0	-0,6	-1,2	2.2		+0	,2				
5	+0,0		+0,0		+0,	0	-0,(	0	-0	,6				
15°	-0,9	-2,0	-0,8	-1,5	-0,	3	-0,	4	-1,0	-1,5				
15	+(	0,2	+(	),2	+0,	2	+0,0		+0,0	+0,0				
30°	-0,5	-1,5	-0,5	-1,5	-0,2		-0,	4	-0	,5				
30	+(	0,7	+(	),7	+0,	4	+0,	0	+0,0					
45°	-(	),0	-0	),0	-0,	-0,0		2	-0	,3				
40	+(	0,7	+(	),7	+0,6		+0,	0	+0	,0				
60°	+(	0,7	+(	),7	+0,7		+0,7		+0,7		-0,2	2	-0	,3
75°	+0,8		+(	),8	+0,	8	-0,2		-0,3					

NOTE 1 At  $\Theta$  = 0° the pressure changes rapidly between positive and negative values on the windward face around a pitch angle of  $\alpha$  = -5° to +45°, so both positive and negative values are given. For those roofs, four cases should be considered where the largest or smallest values of all areas F, G and H are combined with the largest or smallest values in areas I and J. No mixing of positive and negative values is allowed on the same face.

NOTE 2 Linear interpolation for intermediate pitch angles of the same sign may be used between values of the same sign. (Do not interpolate between  $\alpha$  = +5° and  $\alpha$  = -5°, but use the data for flat roofs in 7.2.3). The values equal to 0,0 are given for interpolation purposes

Table 7.4b — External pressure coefficients for duopitch roofs

Pitch		Zone for wind direction <i>⊕</i> = 90°											
angle $\alpha$	F	:	(	3		н	I						
angle a	<b>C</b> <sub>pe,10</sub>	c <sub>pe,1</sub>	<b>c</b> <sub>pe,10</sub>	C <sub>pe,1</sub>	<b>c</b> <sub>pe,10</sub>	C <sub>pe,1</sub>	<b>C</b> <sub>pe,10</sub>	<b>c</b> <sub>pe,1</sub>					
-45°	-1,4	-2,0	-1,2	-2,0	-1,0	-1,3	-0,9	-1,2					
-30°	-1,5	-2,1	-1,2	-2,0	-1,0	-1,3	-0,9	-1,2					
-15°	-1,9	-2,5	-1,2	-2,0	-0,8	-1,2	-0,8	-1,2					
-5°	-1,8	-2,5	-1,2	-2,0	-0,7	-1,2	-0,6	-1,2					
5°	-1,6	-2,2	-1,3	-2,0	-0,7	-1,2	-0	,6					
15°	-1,3	-2,0	-1,3	-2,0	-0,6	-1,2	-0	,5					
30°	-1,1	-1,5	-1,4	-2,0	-0,8	-1,2	-0,5						
45°	-1,1	-1,5	-1,4	-2,0	-0,9	-1,2	-0,5						
60°	-1,1	-1,5	-1,2	-2,0	-0,8	-1,0	-0,5						
75°	-1,1	-1,5	-1,2	-2,0	-0,8	-1,0	-0	,5					

# 7.2.6 Hipped roofs

- (1) The roof, including protruding parts, should be divided into zones as shown in Figure 7.9.
- (2) The reference height  $z_e$  should be taken as h.
- (3) The pressure coefficients that should be used are given in Table 7.5.

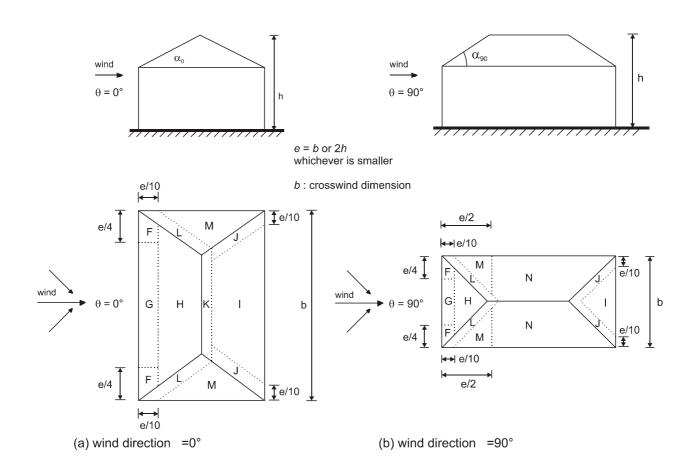


Figure 7.9 — Key for hipped roofs

Table 7.5 — External pressure coefficients for hipped roofs of buildings

Pitch angle					;	Zone	for w	ind c	lirect	ion <i>&amp;</i>	)= 0° a	and $\epsilon$	90°	,					
α₀ for <i>Θ</i> =0°	F	=	(	3	н			I J		ŀ	K L		L	. м		N			
α <sub>90</sub> for <i>Θ</i> =90°	<b>C</b> <sub>pe,10</sub>	<b>C</b> <sub>pe,1</sub>																	
5°	-1,7	-2,5	-1,2	-2,0	-0,6	-1,2	-0	,3	-0	,6	-0	,6	-1,2	-2,0	-0,6	-1,2	-0	,4	
	+0	),0	+(	),0	+0	),0							-,-	_,,	0,0	.,_		, .	
15°	-0,9	-2,0	-0,8	-1,5	-0	,3	-0,5		-1,0	-1,5	-1,2	-2,0	-1,4	-2,0	-0,6	-1,2	0	,3	
13	+0	),2	+(	),2	+0	),2	-0	,,,	-1,0	-1,5	-1,2	-2,0	-1,4	-2,0	-0,0	-1,2	-0	,,,	
30°	-0,5	-1,5	-0,5	-1,5	-0	,2	0.4		-0,4	0.7	-1.2		. =	1 1	2.0	0.0	10		
30	+0	),5	+(	),7	+0	),4	-0	,4	-0,7	-1,2	-0	-0,5	-1,4	-1,4   -2,0	-0,8 -1,2	-1,2	-0,2	,∠	
45°	-0	,0	-0	,0	-0	,0							4.0	0.0	0.0	10		. 0	
40	+0	),7	+(	),7	+0	),6	0	,3	0	,6	0	-0,3	-1,3	-2,0	-0,8	-1,2	0	,2	
60°	+0	),7	+(	),7	+0	),7	-0,3		-0	,6	-0	,3	-1,2	-2,0	-0	,4	-0	,2	
75°	+0	),8	+(	),8	+0	+0,8		,3	-0	,6	-0	,3	-1,2	-2,0	-0	,4	-0	,2	

NOTE 1 At  $\Theta$  = 0° the pressures changes rapidly between positive and negative values on the windward face at pitch angle of  $\alpha$  = +5° to +45°, so both positive and negative values are given. For those roofs, two cases should be considered: one with all positive values, and one with all negative values. No mixing of positive and negative values are allowed.

NOTE 2 Linear interpolation for intermediate pitch angles of the same sign may be used between values of the same sign. The values equal to 0,0 are given for interpolation purposes

NOTE 3 The pitch angle of the windward face always will govern the pressure coefficients.

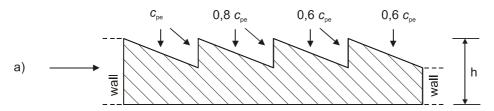
### 7.2.7 Multispan roofs

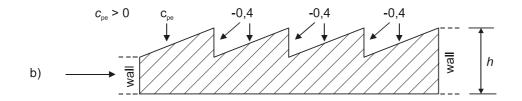
(1) Pressure coefficients for wind directions  $0^{\circ}$ ,  $90^{\circ}$  and  $180^{\circ}$  for each span of a multispan roof may be derived from the pressure coefficient for each individual span.

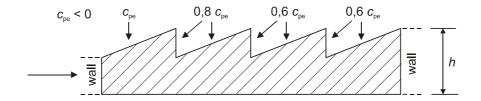
Modifying factors for the pressures (local and global) for wind directions  $0^{\circ}$  and  $180^{\circ}$  on each span should be derived:

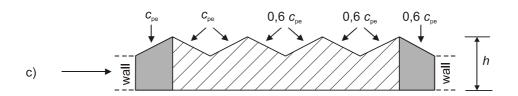
- from 7.2.4 for monopitch roofs, modified for their position according to Figure 7.10 a and b.
- from 7.2.5 for duopitch roofs for  $\alpha$  < 0 modified for their position according to Figure 7.10 c and d.
- (2) The zones F/G/J used should be considered only for the upwind face. The zones H and I should be considered for each span of the multispan roof.

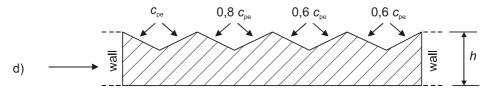
(3) The reference height  $z_e$  should be taken as h.











NOTE 1 In configuration b two cases should be considered depending on the sign of pressure coefficient  $c_{pe}$  on the first roof.

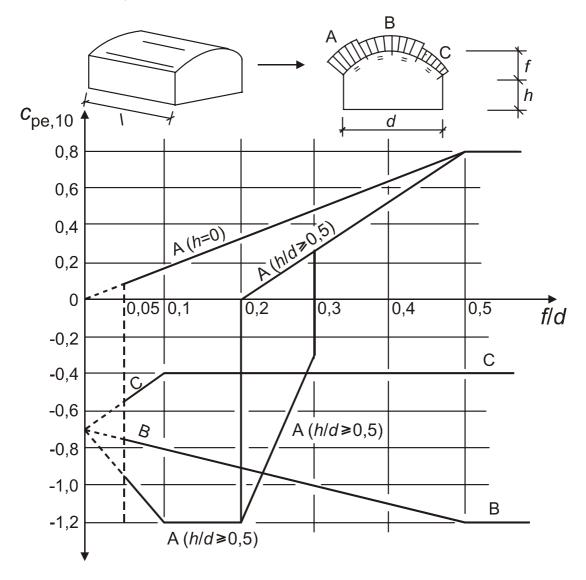
NOTE 2 In configuration c the first  $c_{pe}$  is the  $c_{pe}$  of the monopitch roof, the second and all following  $c_{pe}$  are the  $c_{pe}$  of the troughed duopitch roof.

Figure 7.10 — Key to multispan roofs

### 7.2.8 Vaulted roofs and domes

(1) This section applies to circular cylindrical roofs and domes.

NOTE The values of  $c_{\rm pe,10}$  and  $c_{\rm pe,1}$  to be used for circular cylindrical roofs and domes may be given in the National Annex. The recommended values of  $c_{\rm pe,10}$  are given in Figures 7.11 and 7.12 for different zones. The reference height should be taken as  $z_{\rm e} = h + f$ .

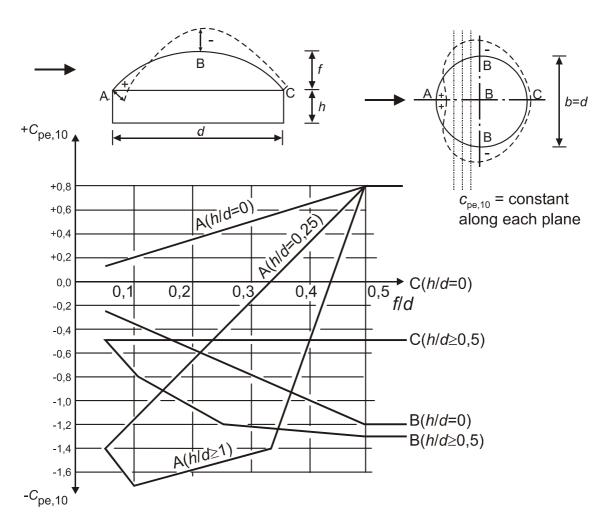


for 0 < h/d < 0.5,  $c_{pe,10}$  is obtained by linear interpolation

for  $0.2 \le f/d \le 0.3$  and  $h/d \ge 0.5$ , two values of  $c_{\text{pe},10}$  have to be considered

the diagram is not applicable for flat roofs

Figure 7.11 — Recommended values of external pressure coefficients  $c_{\rm pe,10}$  for vaulted roofs with rectangular base



 $c_{\rm pe,10}$  is constant along arcs of circles, intersections of the sphere and of planes perpendicular to the wind; it can be determined as a first approximation by linear interpolation between the values in A, B and C along the arcs of circles parallel to the wind. In the same way the values of  $c_{\rm pe,10}$  in A if 0 < h/d < 1 and in B or C if 0 < h/d < 0,5 can be obtained by linear interpolation in the Figure above.

Figure 7.12 — Recommended values of external pressure coefficients  $c_{\rm pe,10}$  for domes with circular base

(2) Pressure coefficients for the walls of rectangular buildings with vaulted roofs should be taken from 7.2.2.

### 7.2.9 Internal pressure

- (1)P Internal and external pressures shall be considered to act at the same time. The worst combination of external and internal pressures shall be considered for every combination of possible openings and other leakage paths.
- (2) The internal pressure coefficient,  $c_{\rm pi}$ , depends on the size and distribution of the openings in the building envelope. When in at least two sides of the buildings (facades or roof) the total area of openings in each side is more than 30 % of the area of that side, the actions on the structure should not be calculated from the rules given in this section but the rules of 7.3 and 7.4 should instead be used.

NOTE The openings of a building include small openings such as: open windows, ventilators, chimneys, etc. as well as background permeability such as air leakage around doors, windows, services and through the building envelope. The background permeability is typically in the range 0,01% to 0, 1% of the face area. Additional information may be given in a National Annex.

(3) Where an external opening, such as a door or a window, would be dominant when open but is considered to be closed in the ultimate limit state, during severe windstorms, the condition with the door or window open should be considered as an accidental design situation in accordance with EN 1990.

NOTE Checking of the accidental design situation is important for tall internal walls (with high risk of hazard) when the wall has to carry the full external wind action because of openings in the building envelope.

(4) A face of a building should be regarded as dominant when the area of openings at that face is at least twice the area of openings and leakages in the remaining faces of the building considered.

NOTE This can also be applied to individual internal volumes within the building.

(5) For a building with a dominant face the internal pressure should be taken as a fraction of the external pressure at the openings of the dominant face. The values given by Expressions (7.2) and (7.3) should be used.

When the area of the openings at the dominant face is twice the area of the openings in the remaining faces,

$$\boldsymbol{c}_{\mathrm{pi}} = 0.75 \cdot \boldsymbol{c}_{\mathrm{pe}} \tag{7.2}$$

When the area of the openings at the dominant face is at least 3 times the area of the openings in the remaining faces,

$$c_{pi} = 0.90 \cdot c_{pe} \tag{7.3}$$

where  $c_{pe}$  is the value for the external pressure coefficient at the openings in the dominant face. When these openings are located in zones with different values of external pressures an area weighted average value of  $c_{pe}$  should be used.

When the area of the openings at the dominant face is between 2 and 3 times the area of the openings in the remaining faces linear interpolation for calculating  $c_{pi}$  may be used.

(6) For buildings without a dominant face, the internal pressure coefficient  $c_{pi}$  should be determined from Figure 7.13, and is a function of the ratio of the height and the depth of the building, h/d, and the opening ratio  $\mu$  for each wind direction  $\theta$ , which should be determined from Expression (7.4).

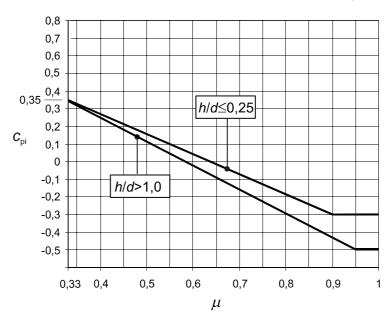


Figure 7.13 — Internal pressure coefficients for uniformly distributed openings

$$\mu = \frac{\sum \text{area of openings where } c_{\text{pe}} \text{ is negative or - 0,0}}{\sum \text{area of all openings}}$$
 (7.4)

NOTE 1 This applies to façades and roof of buildings with and without internal partitions.

NOTE 2 Where it is not possible, or not considered justified, to estimate  $\mu$  for a particular case then  $c_{pi}$  should be taken as the more onerous of +0,2 and -0,3.

- (7) The reference height  $z_i$  for the internal pressures should be equal to the reference height  $z_e$  for the external pressures (see 5.1) on the faces which contribute by their openings to the creation of the internal pressure. If there are several openings the largest value of  $z_e$  should be used to determine  $z_i$ .
- (8) The internal pressure coefficient of open silos and chimneys should be based on Expression (7.5):

$$c_{\text{pi}} = -0.60$$
 (7.5)

The internal pressure coefficient of vented tanks with small openings should be based on Expression (7.6):

$$c_{\rm pi} = -0.40$$
 (7.6)

The reference height  $z_i$  is equal to the height of the structure.

### 7.2.10 Pressure on walls or roofs with more than one skin

- (1) The wind force is to be calculated separately on each skin.
- (2) The permeability  $\mu$  of a skin is defined as the ratio of the total area of the opening to the total area of the skin. A skin is defined as impermeable if the value  $\mu$  is less than 0,1%.
- (3) If only one skin is permeable, then the wind force on the impermeable skin should be determined from the difference between the internal and the external wind pressure as described in Section 5.1. If more than one skin is permeable then the wind force on each skin depends on:
- The relative rigidity of the skins,
- The external and internal pressures,
- The distance between the skins,
- The permeability of the skins,
- The openings at the extremities of the layer between the skins.
  - NOTE 1 The National Annex may give values for the wind effects on external walls and roofs with more than one skin. As a first approximation it is recommended that the wind pressure on the most rigid skin may be taken as the difference between the internal and the external pressures.
  - NOTE 2 The National Annex may give rules for cases where the extremities of the layer between the skins are air tight (Figure 7.14(a)) and where the free distance between the skins is less than 100 mm (the thermal insulation material being included in one skin, when there is no airflow within the insulation). As a first approximation the following recommended rules may be applied:
    - For walls and roofs with an impermeable inside skin and a permeable outside skin with approximately uniformly distributed openings, the wind force on the outside skin may be calculated from  $c_{p,net} = 2/3 \cdot c_{pe}$  for overpressure and  $c_{p,net} = 1/3 \cdot c_{pe}$  for underpressure. The windforce on the inside skin may be calculated from  $c_{p,net} = c_{pe} c_{pi}$ .
    - For walls and roofs with an impermeable inside skin and an impermeable more rigid, outside skin, the wind force on the outside skin may be calculated from  $c_{p,net} = c_{pe} c_{pi}$ .
    - For walls and roofs with a permeable inside skin with approximately uniformly distributed openings and an impermeable outside skin, the wind force on the outside skin may be calculated from  $c_{\text{p,net}} = c_{\text{pe}} c_{\text{pi}}$ , and the wind force on the inside skin from  $c_{\text{p,net}} = 1/3 \cdot c_{\text{pi}}$ .
    - For walls and roofs with an impermeable outside skin and an impermeable, more rigid inside skin, the wind force on the outside skin may be calculated from  $c_{p,net} = c_{pe}$  and the wind force on the inside skin from  $c_{p,net} = c_{pe} c_{pi}$ .

If entries of air put the layer of air into communication with faces of the building other than the face on which the wall is situated (Figure 7.14(b)), these rules are not applicable

1 1		11	
) extremitie	es of the layer betw	veen the skins open	

(a) extremities of the layer between the skins closed

Figure 7.14 — Corner details for external walls with more than one skin.

### 7.3 Canopy roofs

- (1) A canopy roof is defined as the roof of a structure that does not have permanent walls, such as petrol stations, dutch barns, etc.
- (2) The degree of blockage under a canopy roof is shown in Figure 7.15. It depends on the blockage  $\varphi$ , which is the ratio of the area of feasible, actual obstructions under the canopy divided by the cross sectional area under the canopy, both areas being normal to the wind direction.  $\varphi$  = 0 represents an empty canopy, and  $\varphi$  = 1 represents the canopy fully blocked with contents to the down wind eaves only (this is not a closed building).
- (3) The overall force coefficients,  $c_{\rm f}$ , and net pressure coefficients  $c_{\rm p,net}$ , given in Tables 7.6 to 7.8 for  $\varphi$  = 0 and  $\varphi$  = 1 take account of the combined effect of wind acting on both the upper and lower surfaces of the canopies for all wind directions. Intermediate values may be found by linear interpolation.
- (4) Downwind of the position of maximum blockage,  $c_{p,net}$  values for  $\varphi = 0$  should be used.
- (5) The overall force coefficient represents the resulting force. The net pressure coefficient represents the maximum local pressure for all wind directions. It should be used in the design of roofing elements and fixings.

- (6) Each canopy must be able to support the load cases as defined below:
- for a monopitch canopy (Table 7.6) the center of pressure should be taken at d/4 from the windward edge (d = alongwind dimension, Figure 7.16)
- for a duopitch canopy (Table 7.7) the center of pressure should be taken at the center of each slope (Figure 7.17). In addition, a duopitch canopy should be able to support one pitch with the maximum or minimum load, the other pitch being unloaded.
- for a multibay duopitch canopy each load on a bay may be calculated by applying the reduction factors  $\psi_{mc}$  given in Table 7.8 to the  $c_{p,net}$  values given in Table 7.7.

For canopies with double skins, the rules in 7.2.10 (4) should be used.

- (7) Friction forces should be considered (see 7.5).
- (8) The reference height  $z_e$  should be taken as h as shown in Figures 7.16 and 7.17.

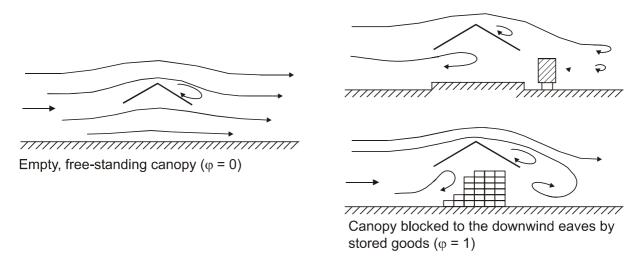
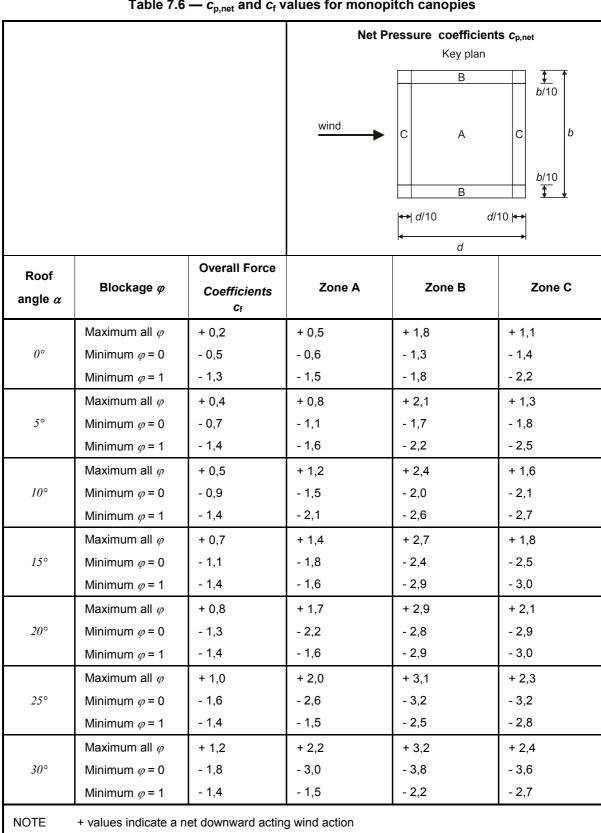


Figure 7.15 — Airflow over canopy roofs



- values represent a net upward acting wind action

Table 7.6 —  $c_{p,net}$  and  $c_f$  values for monopitch canopies

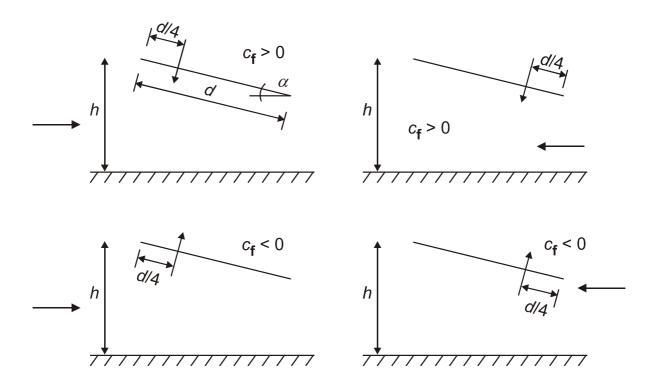


Figure 7.16 — Location of the centre of force for monopitch canopies

Table 7.7 —  $c_{p,net}$  and  $c_f$  values for duopitch canopies Net pressure coefficients cp,net Key plan *b*/10 С D lc Α Α b b/10 В \$ **↔** d/10 **←** d/10 |↔ Roof Overall **Force** Blockage  $\varphi$ angle  $\alpha$ d Coefficient Zone A Zone C Zone D Zone B [°]  $\boldsymbol{c}_{\text{f}}$ Maximum all  $\varphi$ +0,7+ 0,8 + 1,6 +0,6+ 1,7 - 20 Minimum  $\varphi = 0$ - 0,7 - 0.9 - 1,3 - 1.6 - 0,6 - 1,3 - 1,5 - 2,4 - 2,4 - 0,6 Minimum  $\varphi = 1$ Maximum all  $\varphi$ + 0,5 + 0,6 + 1,5 + 1,4 + 0,7 - 15 - 0,6 Minimum  $\varphi = 0$ - 0,6 - 0,8 - 1,3 - 1,6 - 2,7 - 2,6 - 0,6 - 1,4 - 1,6 Minimum  $\varphi = 1$ Maximum all  $\varphi$ + 0,4 + 0,6 + 1,4 +0.8+ 1,1 - 10 Minimum  $\varphi = 0$ - 0,6 - 0,8 - 1,3 - 1,5 - 0,6 - 1,4 - 1,6 - 2,7 - 2,6 - 0,6 Minimum  $\varphi = 1$ Maximum all  $\varphi$ + 0,3 + 1,5 + 0,5 + 0,8 + 0,8 - 5 Minimum  $\varphi = 0$ - 0,5 - 0,7 - 1,3 - 1,6 - 0,6 Minimum  $\varphi = 1$ - 1,3 - 1,5 - 2,4 - 2,4 - 0,6 Maximum all  $\varphi$ +0,3+ 0,6 + 1,8 + 1,3 +0,4+ 5 Minimum  $\varphi = 0$ - 0,6 - 0,6 - 1,4 - 1,4 - 1,1 - 1,3 - 1,3 - 2,0 - 1,8 - 1,5 Minimum  $\varphi = 1$ Maximum all  $\varphi$ + 0,4 + 0,7 + 1,8 + 1,4 + 0,4 + 10 - 0,7 Minimum  $\varphi = 0$ - 0,7 - 1,5 - 1,4 - 1,4 Minimum  $\varphi = 1$ - 1,3 - 1,3 - 2,0 - 1,8 - 1,8 Maximum all  $\varphi$ + 0,4 + 0,9 + 1,9 + 1,4 + 0,4 + 15 Minimum  $\varphi = 0$ - 0,8 - 0,9 - 1,7 - 1,4 - 1,8 - 1,3 - 1,3 - 2,2 - 1,6 - 2,1 Minimum  $\varphi = 1$ Maximum all  $\varphi$ + 0,6 + 1,1 + 1,9 + 1,5 +0,4+ 20 Minimum  $\varphi = 0$ - 0,9 - 1,2 - 1,8 - 1,4 - 2,0

Minimum  $\varphi = 1$ 

- 1,3

- 1,4

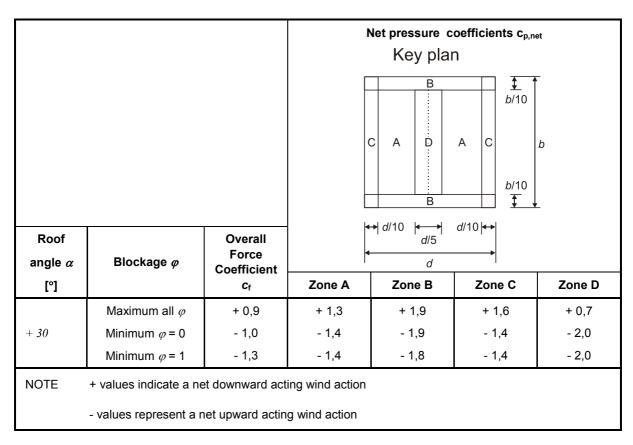
- 2,2

- 1,6

-2,1

	Maximum all $\varphi$	+ 0,7	+ 1,2	+ 1,9	+ 1,6	+ 0,5
+ 25	Minimum $\varphi = 0$	- 1,0	- 1,4	- 1,9	- 1,4	- 2,0
	Minimum $\varphi$ = 1	- 1,3	- 1,4	- 2,0	- 1,5	- 2,0

Table 7.7 — continue



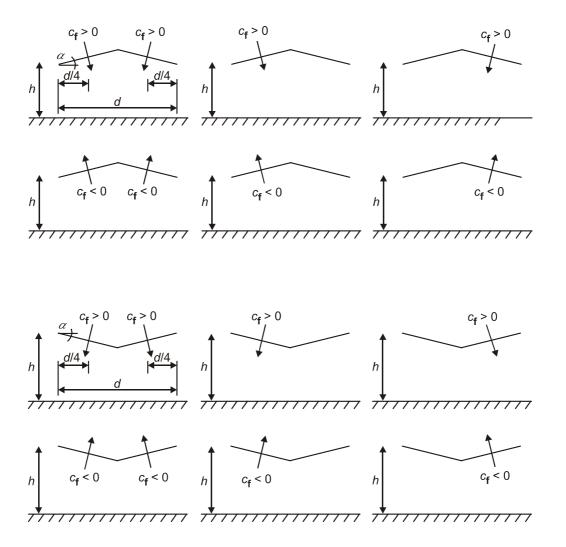


Figure 7.17 — Arrangements of loads obtained from force coefficients for duopitch canopies

(9) Loads on each slope of multibay canopies, as shown in Figure 7.18, are determined by applying the reduction factors  $\psi_{mc}$  given in Table 7.8 to the overall force, and net pressure coefficients for isolated duo-pitch canopies.

Table 7.8 — Reduction factors  $\psi_{mc}$  for multibay canopies

		$\psi_{ m mc}$ factors for all $arphi$					
Вау	Location	on maximum (downward) force and pressure coefficients	on minimum (upward) force and pressure coefficients				
1	End bay	1,0	0,8				
2	second bay	0,9	0,7				
3	third and subsequent bays	0,7	0,7				

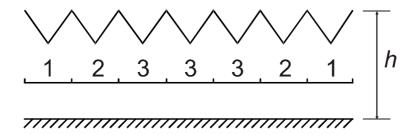


Figure 7.18 — Multibay canopies

## 7.4 Free-standing walls, parapets, fences and signboards

(1) The values of the resulting pressure coefficients  $c_{\rm p,net}$  for free-standing walls and parapets depend on the solidity ratio  $\varphi$ . For solid walls the solidity  $\varphi$  should be taken as 1, and for walls which are 80 % solid (i.e. have 20 % openings)  $\varphi$  = 0,8. Porous walls and fences with a solidity ratio  $\varphi \le$  0,8 should be treated as plane lattices in accordance with 7.11.

NOTE For parapets and noise barriers of bridges see Section 8.

### 7.4.1 Free-standing walls and parapets

(1) For free-standing walls and parapets resulting pressure coefficients  $c_{p,net}$  should be specified for the zones A, B, C and D as shown in Figure 7.19.

NOTE Values of the resulting pressure coefficients  $c_{p,net}$  for free-standing walls and parapets may be given in the National Annex. Recommended values are given in Table 7.9 for two different solidity ratio, see 7.4 (1). The reference area in both cases is the gross area. Linear interpolation may be used for solidity ratio between 0,8 and 1.

Table 7.9 — Recommended	pressure coefficients c <sub>p.net</sub>	for free-standing	walls and parapets

Solidity	Zone		Α	В	С	D
φ = 1	Without return corners	<i>ℓ/h</i> ≤ 3	2,3	1,4	1,2	1,2
		ℓ/ <b>h</b> = 5	2,9	1,8	1,4	1,2
		<i>ℓ/h</i> ≥ 10	3,4	2,1	1,7	1,2
	with return corners of length $\geq h^{a, b}$		±2,1	±1,8	±1,4	±1,2
φ = 0,8			±1,2	±1,2	±1,2	±1,2

<sup>&</sup>lt;sup>a</sup> Linear interpolation may be used for return corner lengths between 0,0 and *h* 

(2) The reference height for free standing walls should be taken as  $z_e = h$ , see Figure 7.19. The reference height for parapets in buildings should be taken as  $z_e = (h + h_p)$ , see Figure 7.6.

<sup>&</sup>lt;sup>b</sup> Mixing of positive and negative values is not allowed.

# for $\ell > 4 h$ **■**0 **■** 0,3 *h* **■**2 h **■** 4 h C D for $\ell \le 4 h$ **■**0 **■** 0,3 *h* **4**2 h **4** 4 h C for $\ell \leq 2 h$ **4**0 **4** 0,3 *h* **∢**2 h (b) Key to wind angle Without return corner With return corner

(a) Keys to zone (z<sub>e</sub>=h)

Figure 7.19 — Key to zones of free-standing walls and parapets

### 7.4.2 Shelter factors for walls and fences

(1) If there are other walls or fences upwind that are equal in height or taller than the wall or fence of height, h, under consideration, then an additional shelter factor can be used with the net pressure coefficients for walls and lattice fences. The value of the shelter factor  $\psi_s$  depends on the spacing between the walls or fences x, and the solidity  $\varphi$ , of the upwind (sheltering) wall or fence. Values of  $\psi_s$  are given in Figure 7.20.

The resulting net pressure coefficient on the sheltered wall,  $c_{p,net,s}$ , is given by Expression (7.7):

$$c_{\text{p.net.s}} = \psi_{\text{s}} \cdot c_{\text{p.net}}$$
 (7.7)

(2) The shelter factor should not be applied in the end zones within a distance of *h* measured from the free end of the wall.

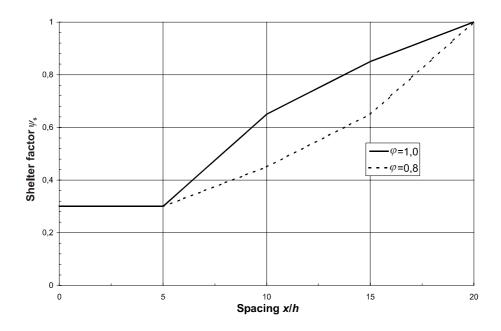


Figure 7.20 — Shelter factor  $\psi_s$  for walls and fences for  $\varphi$ -values between 0,8 and 1,0

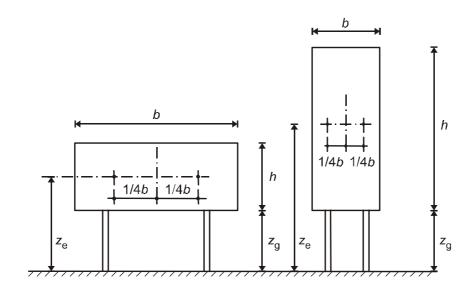
### 7.4.3 Signboards

(1) For signboards separated from the ground by a height  $z_g$  grater than h/4 (see Figure 7.21), the force coefficients are given by Expression (7.8):

$$c_f = 1,80$$
 (7.8)

- (2) Signboards separated from the ground by a height  $z_g$  less than h/4 and with b/h > 1 should be treated as boundary walls, (see 7.4.1). When  $z_g$  is less than h/4 and  $b/h \le 1$  Expression (7.8) is applicable.
- (3) The resultant force normal to the signboard should be taken to act at the height of the center of the signboard, with an horizontal eccentricity e given by Expression (7.9):

$$\mathbf{e} = \pm 0.25 \cdot \mathbf{b} \tag{7.9}$$



NOTE 1 reference height:  $z_e = z_g + h/2$ 

NOTE 2 reference area:  $A_{ref} = b \cdot h$ 

Figure 7.21 — Key for signboards

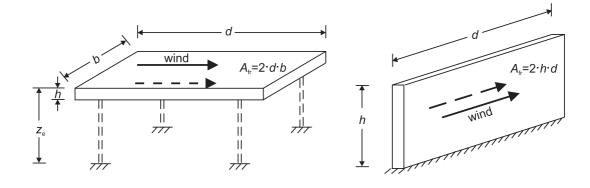
Divergence or stall flutter instabilities should be checked.

## 7.5 Friction coefficients

- (1) Friction should be considered for the cases defined in 5.3 (3).
- (2) The friction coefficients  $c_{fr}$ , for walls and roof surfaces given in Table 7.10, should be used
- (3) The reference area  $A_{\rm fr}$  is given in Figure 7.22. Friction forces should be applied on the part of the external surfaces parallel to the wind, located beyond a distance from the upwind eaves or corners, equal to the smallest value of  $2 \cdot b$  or  $4 \cdot h$ .
- (4) The reference height  $z_e$  should be taken equal to the structure height above ground or building height h, see Figure 7.22

Table 7.10 — Frictional coefficients  $c_{\rm fr}$  for walls, parapets and roof surfaces

Surface	Friction coefficient c <sub>fr</sub>		
Smooth	0.01		
(i.e. steel, smooth concrete)	0,01		
Rough	0,02		
(i.e. rough concrete, tar-boards)			
very rough	0,04		
(i.e. ripples, ribs, folds)			



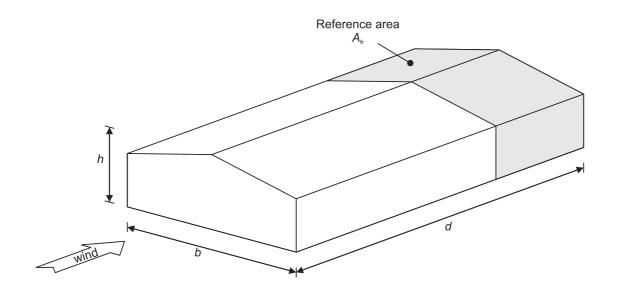


Figure 7.22 — Reference area for friction

# 7.6 Structural elements with rectangular sections

(1) The force coefficient  $c_f$  of structural elements of rectangular section with the wind blowing normally to a face should be determined by Expression (7.10):

$$\mathbf{c}_{\mathbf{f}} = \mathbf{c}_{\mathbf{f},0} \cdot \boldsymbol{\psi}_{\mathbf{f}} \cdot \boldsymbol{\psi}_{\lambda} \tag{7.10}$$

where:

- $c_{\rm f,0}$  is the force coefficient of rectangular sections with sharp corners and without free-end flow as given by Figure 7.23.
- $\psi_{\rm f}$  is the reduction factor for square sections with rounded corners.  $\psi_{\rm f}$  depends on Reynolds number, see Note 1.
- $\psi_{\lambda}$  is the end-effect factor for elements with free-end flow as defined in 7.13.

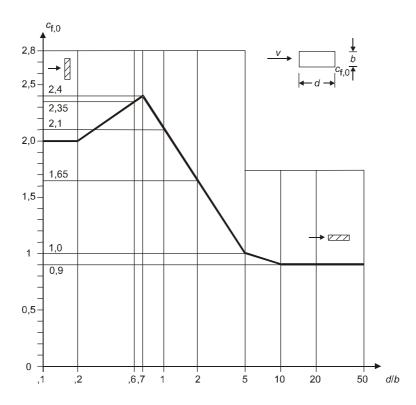


Figure 7.23 — Force coefficients  $c_{f,0}$  of rectangular sections with sharp corners and without free end flow

NOTE 1 The values of  $\psi_r$  may be given in the National Annex. Recommended approximate upper bound values of  $\psi_r$  are given in Figure 7.24. Figure 7.24 are obtained under low-turbulent conditions. These coefficients are assumed to be safe.

NOTE 2 Figure 7.24 may also be used for buildings with h/d > 5.0

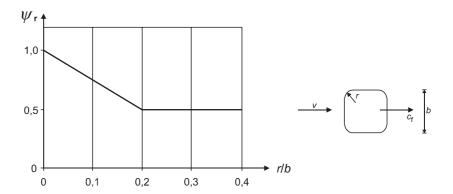


Figure 7.24 — Reduction factor  $\psi_r$  for a square cross-section with rounded corners

(2) The reference area  $A_{ref}$  should be determined by Expression (7.11)

$$A_{\text{ref}} = \ell \cdot b \tag{7.11}$$

where:

 $\ell$  is the length of the structural element being considered.

The reference height  $z_e$  is equal to the maximum height above ground of the section being considered.

(3) For plate-like sections (d/b < 0.2) lift forces at certain wind angles of attack may give rise to higher values of  $c_f$  up to an increase of 25 %.

# 7.7 Structural elements with sharp edged section

(1) The force coefficient  $c_f$  of structural elements with sharp edged section (e.g. elements with cross-sections such as those shown in Figure 7.25) should be determined using Expression (7.12).

$$\mathbf{c}_{\mathsf{f}} = \mathbf{c}_{\mathsf{f},0} \cdot \boldsymbol{\psi}_{\lambda} \tag{7.12}$$

 $\psi_{\lambda}$  is the end-effect factor (see 7.13)

NOTE 1 The National Annex may specify  $c_{f,0}$ . For all elements without free-end flow the recommended value is 2,0. This value is based on measurements under low-turbulent conditions. It is assumed to be a safe value.

NOTE 2 Expression (7.12) and Figure 7.25 may also be used for building with h/d > 5.0

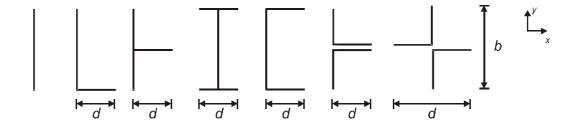


Figure 7.25 — Sharp edged structural sections

(2) The reference areas (see Figure 7.25), should be taken as follows:

in x – direction : 
$$A_{\text{ref},x} = \ell \cdot b$$
  
in y – direction :  $A_{\text{ref},y} = \ell \cdot d$  (7.13)

where:

- $\ell$  is the length of the structural element being considered.
- (3) In all cases the reference height  $z_e$  should be taken as equal to the maximum height above ground of the section being considered.

# 7.8 Structural elements with regular polygonal section

(1) The force coefficient  $c_f$  of structural elements with regular polygonal section with 5 or more sides should be determined using Expression (7.14).

$$\mathbf{c}_{\mathsf{f}} = \mathbf{c}_{\mathsf{f},0} \cdot \boldsymbol{\psi}_{\lambda} \tag{7.14}$$

where:

- $\psi_{\lambda}$  is the end-effect factor as defined in 7.13.
- $c_{\rm f,0}$  is the force coefficient of structural elements without free-end flow.

NOTE The values of  $c_{f,0}$  may be given in the National Annex. Recommended conservative values based on measurements under low-turbulent conditions are given in Table 7.11.

Table 7.11 — Force coefficient  $c_{\rm f,0}$  for regular polygonal sections

Number of sides	Sections	Finish of surface and of corners	Reynolds number Re <sup>(1)</sup>	C <sub>f,0</sub>
5	Pentagon	all	All	1,80
6	Hexagon	all	All	1,60
8	Octagon	surface smooth	$Re \le 2,4 \cdot 10^5$	1,45
		r/b < 0,075 (2)	Re ≥ 3·10 <sup>5</sup>	1,30
		surface smooth	Re ≤ 2·10 <sup>5</sup>	1,30
		$r/b \ge 0.075$ (2)	Re ≥ 7·10 <sup>5</sup>	1,10
10	Decagon	all	All	1,30
12	Dodecagon	surface smooth (3) corners rounded	2 · 10 <sup>5</sup> < Re < 1,2·10 <sup>6</sup>	0,90
		all atheres	Re < 4·10 <sup>5</sup>	1,30
		all others	Re > 4·10 <sup>5</sup>	1,10
16-18	Hexdecago n		Re < 2·10 <sup>5</sup>	treat as a circular
		surface smooth (3) corners rounded	Re < 2·10	cylinder, see (7.9)
		233.3.3333	$2 \cdot 10^5 \le Re < 1, 2 \cdot 10^6$	0,70

Reynolds number with  $v = v_m$  and  $v_m$  given in 4.3, Re, is defined in 7.9

r = corner radius, b = diameter of circumscribed circumference, see Figure 7.26

From wind tunnel tests on sectional models with galvanised steel surface and a section with b = 0.3 m and corner radius of  $0.06 \cdot b$ 

(2) For buildings where h/d > 5,  $c_{f,0}$  may be determined from Expression (7.14) and the information contained in Table 7.11 and Figure 7.25.

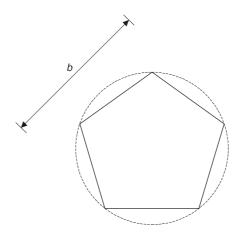


Figure 7.26 — Regular polygonal section

(3) The reference area  $A_{ref}$  is should be obtained from Expression (7.15).

$$A_{\text{ref}} = \ell \cdot b \tag{7.15}$$

where:

- $\ell$  is the length of the structural element being considered.
- b is the diameter of circumscribed circumference, see Figure 7.26.
- (4) The reference height  $z_e$  is equal to the maximum height above ground of the section being considered.

# 7.9 Circular cylinders

## 7.9.1 External pressure coefficients

(1) Pressure coefficients of sections depend upon the Reynolds numbers Re defined by Expression (7.16).

$$Re = \frac{b \cdot v(z_e)}{v} \tag{7.16}$$

where:

- b is the diameter
- $\nu$  is the kinematic viscosity of the air ( $\nu = 15.10^{-6} \,\text{m}^2/\text{s}$ )
- $v(z_e)$  is the peak wind velocity defined in Note 2 of Figure 7.27at height  $z_e$

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(2) The external pressure coefficients  $c_{pe}$  of circular cylinders should be determined from Expression (7.17).

$$c_{\rm pe} = c_{\rm p,0} \cdot \psi_{\lambda\alpha} \tag{7.17}$$

where:

 $c_{\text{p,0}}$  is the external pressure coefficient without free-end flow (see (3))

 $\psi_{\lambda\alpha}$  is the end-effect factor (see (4))

- (3) The external pressure coefficient  $c_{p,0}$  is given in Figure 7.27 for various Reynolds numbers as a function of angle  $\alpha$ .
- (4) The end-effect factor  $\psi_{\lambda\alpha}$  is given by Expression (7.18).

$$\psi_{\lambda\alpha} = 1 \qquad \text{for} \qquad 0^{\circ} \le \alpha \le \alpha_{\min}$$

$$\psi_{\lambda\alpha} = \psi_{\lambda} + (1 - \psi_{\lambda}) \cdot \cos\left(\frac{\pi}{2} \cdot \left(\frac{\alpha - \alpha_{\min}}{\alpha_{A} - \alpha_{\min}}\right)\right) \qquad \text{for} \qquad \alpha_{\min} < \alpha < \alpha_{A}$$

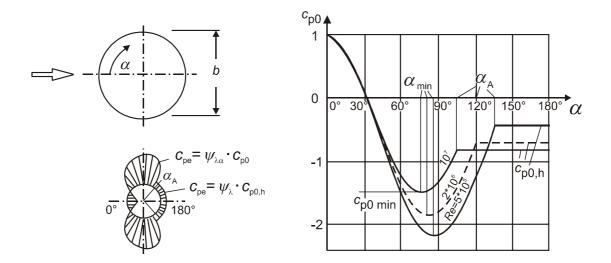
$$\psi_{\lambda\alpha} = \psi_{\lambda} \qquad \text{for} \qquad \alpha_{A} \le \alpha \le 180^{\circ}$$

$$(7.18)$$

where:

 $\alpha_{\rm A}$  is the position of the flow separation (see Figure 7.27)

 $\psi_{\lambda}$  is the end-effect factor (see 7.13)



NOTE 1 Intermediate values may be interpolated linearly

NOTE 2 Typical values in the above Figure are shown in Table 7.12. Figure and Table are based on the Reynolds number with  $V=\sqrt{\frac{2\cdot q_{\rm p}}{\rho}}$  and  $q_{\rm p}$  given in 4.5

NOTE 3 The above Figure is based on an equivalent roughness k/b less than  $5 \cdot 10^{-4}$ . Typical values of roughness height k are given in Table 7.13.

Figure 7.27 —Pressure distribution for circular cylinders for different Reynolds number ranges and without end-effects

Table 7.12 — Typical values for the pressure distribution for circular cylinders for different Reynolds number ranges and without end-effects

Re	$lpha_{min}$	C <sub>p0,min</sub>	$lpha_{A}$	C <sub>p0,h</sub>
5·10 <sup>5</sup>	85	-2,2	135	-0,4
2·10 <sup>6</sup>	80	-1,9	120	-0,7
10 <sup>7</sup>	75	-1,5	105	-0,8

where:

 $lpha_{\min}$  is the position of the minimum pressure in [°]

 $c_{\mbox{\scriptsize p0,min}}$  is the value of the minimum pressure coefficient

 $\alpha_{A}$  is the position of the flow separation in [°]

 $c_{\rm p0,h}$  is the base pressure coefficient

(5) The reference area  $A_{ref}$  should be determined from Expression (7.19):

$$A_{\text{ref}} = \ell \cdot b \tag{7.19}$$

(6) The reference height  $z_e$  is equal to the maximum height above ground of the section being considered.

## 7.9.2 Force coefficients

(1) The force coefficient  $c_f$  for a finite circular cylinder should be determined from Expression (7.20).

$$c_{\rm f} = c_{\rm f,0} \cdot \psi_{\lambda} \tag{7.20}$$

where:

 $c_{\rm f,0}$  is the force coefficient of cylinders without free-end flow (see Figure 7.28)

 $\psi_{\lambda}$  is the end-effect factor (see 7.13)

NOTE 1 Figure 7.28 may also be used for building with h/d > 5.0

NOTE 2 Figure 7.28 is based on the Reynolds number with  $v = \sqrt{\frac{2 \cdot q_p}{\rho}}$  and  $q_p$  given in 4.5

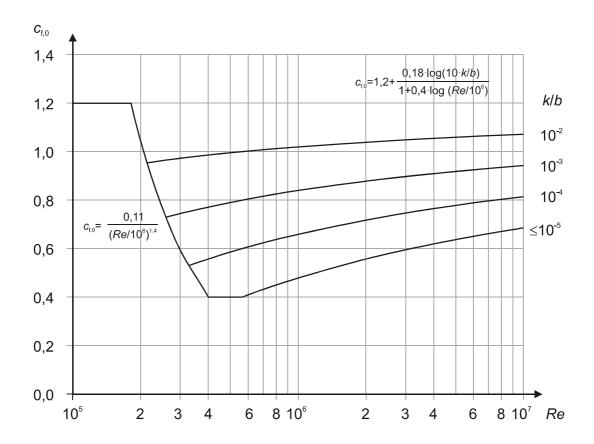


Figure 7.28 — Force coefficient  $c_{f,0}$  for circular cylinders without free-end flow and for different equivalent roughness k/b

- (2) Values of equivalent surface roughness k are given in Table 7.13.
- (3) For stranded cables  $c_{\rm f,0}$  is equal to 1,2 for all values of the Reynolds number Re.

Table 7.13 — Equivalent surface roughness k

Type of surface	Equivalent roughness <i>k</i>	Type of surface	Equivalent roughness <i>k</i>
	mm		mm
glass	0,0015	smooth concrete	0,2
polished metal	0,002	planed wood	0,5
fine paint	0,006	rough concrete	1,0
spray paint	0,02	rough sawn wood	2,0
bright steel	0,05	rust	2,0
cast iron	0,2	brickwork	3,0
galvanised steel	0,2		

(4) The reference area  $A_{ref}$  should be obtained by Expression (7.21).

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$$A_{\text{ref}} = \ell \cdot b \tag{7.21}$$

where:

- $\ell$  is the length of the structural element being considered.
- (5) The reference height  $z_e$  is equal to the maximum height above ground of the section being considered.
- (6) For cylinders near a plane surface with a distance ratio  $z_g/b < 1,5$  (see Figure 7.29) special advice is necessary.

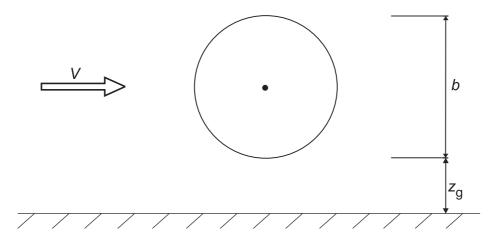


Figure 7.29 — Cylinder near a plane surface

# 7.9.3 Force coefficients for vertical cylinders in a row arrangement

For vertical circular cylinders in a row arrangement, the force coefficient  $c_{f,0}$  depends on the wind direction related to the row axis and the ratio of distance a and the diameter b as defined in Table 7.14. The force coefficient,  $c_{f,}$  for each cylinder may be obtained by Expression (7.22):

$$\mathbf{C}_{\mathbf{f}} = \mathbf{C}_{\mathbf{f},0} \cdot \boldsymbol{\psi}_{\lambda} \cdot \boldsymbol{\kappa} \tag{7.22}$$

where:

 $c_{\rm f,0}$  is the force coefficient of cylinders without free-end flow, (see 7.9.2)

 $\psi_{\lambda}$  is the end-effect factor (see 7.13)

 $\kappa$  is the factor given in Table 7.14 (for the most unfavourable wind direction)

a/b	ĸ	<u>a</u> a →
a/b < 3,5	1,15	
3,5 < a/b < 30	$\kappa = \frac{210 - \frac{a}{b}}{180}$	
a/b > 30	1,00	<u></u> b ←
a: distance		
b: diameter		

Table 7.14 — Factor  $\kappa$  for vertical cylinders in a row arrangement

# 7.10 Spheres

(1) The alongwind force coefficient  $c_{f,x}$  of spheres should be determined as a function of the Reynolds number Re (see 7.9.1) and the equivalent roughness k/b (see Table 7.13).

NOTE 1 The values of  $c_{\rm f,x}$  may be given in the National Annex. Recommended values based on measurements in low turbulent flow are given in Figure 7.30. Figure 7.30 is based on the Reynolds number with  $v=\sqrt{\frac{2\cdot q_{\rm p}}{\rho}}$  and  $q_{\rm p}$  given in 4.5

NOTE 2 The values in Figure 7.30 are limited to values  $z_g > b/2$ , where  $z_g$  is the distance of the sphere from a plain surface, b is the diameter (see Figure 7.31). For  $z_g < b/2$  the force coefficient  $c_{f,x}$  is be multiplied by the factor 1,6.

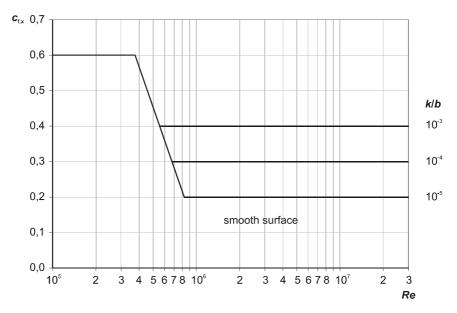


Figure 7.30 — Alongwind force coefficient of a sphere

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(2) The vertical force coefficient  $c_{f,z}$  of spheres is given by Expression (7.23).

$$c_{f,z} = 0$$
 for  $z_g > \frac{b}{2}$  (7.23) 
$$c_{f,z} = +0.60$$
 for  $z_g < \frac{b}{2}$ 

(3) In both cases the reference area  $A_{ref}$  should be obtained by Expression (7.24).

$$A_{\text{ref}} = \pi \cdot \frac{b^2}{4} \tag{7.24}$$

(4) The reference height should be taken as:

$$z_{\rm e} = z_{\rm g} + \frac{b}{2}$$

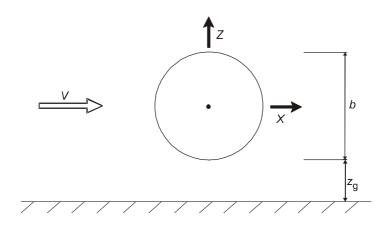


Figure 7.31 — Sphere near a plain surface

# 7.11 Lattice structures and scaffoldings

(1) The force coefficient,  $c_f$ , of lattice structures and scaffoldings should be obtained by Expression (7.25).

$$c_{\rm f} = c_{\rm f,0} \cdot \psi_{\lambda} \tag{7.25}$$

where:

 $c_{f,0}$  is the force coefficient of lattice structures and scaffoldings without end-effects. It is given by Figures 7.33 to 7.35 as a function of solidity ratio  $\varphi$  (7.11 (2)) and Reynolds number Re.

Re is the Reynolds number using the average member diameter  $b_i$  see Note 1

 $\psi_{\lambda}$  is the end-effect factor (see 7.13) as a function of the slenderness of the structure,  $\lambda$ , calculated with  $\ell$  and width b = d, see Figure 7.32.

NOTE 1 Figures 7.33 to 7.35 are based on the Reynolds number with  $v = \sqrt{\frac{2 \cdot q_p}{\rho}}$  and  $q_p$  given in 4.5.

NOTE 2 The National Annex may give a reduction factor for scaffolding without air tightness devices and affected by solid building obstruction. A recommended value is given in prEN 12811.

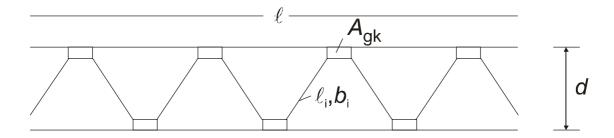


Figure 7.32 — Lattice structure or scaffolding

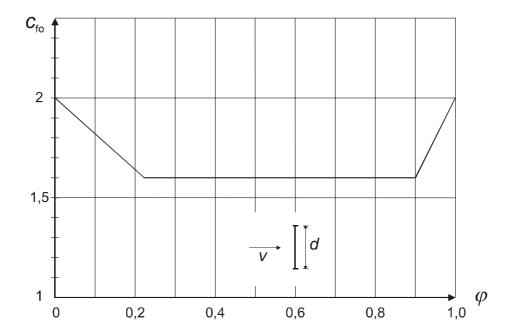


Figure 7.33 — Force coefficient  $c_{\rm f,0}$  for a plane lattice structure with angle members as a function of solidity ratio  $\varphi$ 

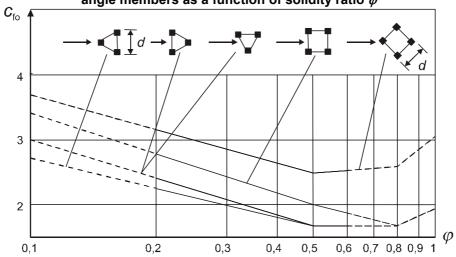


Figure 7.34 —Force coefficient  $c_{\rm f,0}$  for a spatial lattice structure with angle members as a function of solidity ratio  $\varphi$ 

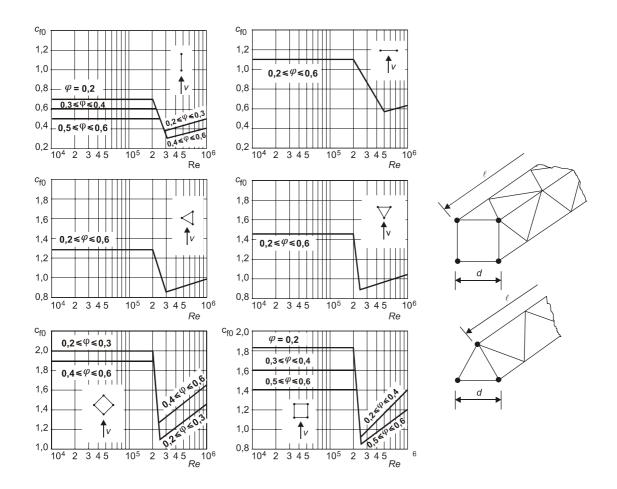


Figure 7.35 — Force coefficient  $c_{\rm f,0}$  for plane and spatial lattice structure with members of circular cross-section

(2) The solidity ratio,  $\varphi$ , is defined by Expression (7.26).

$$\varphi = \frac{A}{A_c} \tag{7.26}$$

where:

A is the sum of the projected area of the members and gusset plates of the face projected normal to the face:  $A = \sum_i b_i \cdot \ell_i + \sum_k A_{gk}$ 

- $A_{c}$  is the the area enclosed by the boundaries of the face projected normal to the face =  $d \ell$
- $\ell$  is the length of the lattice
- d is the width of the lattice
- $b_i$ ,  $\ell_i$  is the width and length of the individual member i (see Figure 7.32), projected normal to the face
- $A_{gk}$  is the area of the gusset plate k
- (3) The reference area  $A_{ref}$  should be determined by Expression (7.27)

$$A_{\text{ref}} = A \tag{7.27}$$

(4) The reference height  $z_{\rm e}$  is equal to the maximum height of the element above ground.

# 7.12 Flags

- (1) Force coefficients  $c_{\rm f}$  and reference areas  $A_{\rm ref}$  for flags are given in Table 7.15.
- (2) The reference height  $z_{\rm e}$  is equal to the height of the flag above ground.

Table 7.15 — Force coefficients  $c_{\rm f}$  for flags

Flags	$A_{ref}$	C <sub>f</sub>
Fixed Flags	$h \cdot \ell$	1,8
a) Free Flags  h	$m{h} \cdot \ell$	
b)   Force in the plane	0,5 · h · ℓ	$0.02 + 0.7 \cdot \frac{m_{\rm f}}{\rho \cdot h} \cdot \left(\frac{A_{\rm ref}}{h^2}\right)^{-1.25}$
where: $m_{\rm f}$ mass per unit area of the flag $\rho$ air density (7.1) $z_{\rm e}$ height of the flag above ground		
NOTE The equation for free flags includes dynamic forces from the flag flutter effect		

# 7.13 Effective slenderness $\lambda$ and end-effect factor $\psi_{\lambda}$

(1) Where relevant, the end-effect factor  $\psi_{\lambda}$  should be determined as a function of slenderness ratio  $\lambda$ .

NOTE The force coefficients,  $c_{f,0}$ , given in 7.6 to 7.12 are based on measurements on structures without free-end flow away from the ground. The end-effect factor takes into account the reduced resistance of the structure due to the windflow around the end (end-effect). Figure 7.36 and Table 7.16 are based on measurements in low turbulent flow. Values, taking the effect of turbulence into account may be specified in the National Annex.

(2) The effective slenderness  $\lambda$  should be defined depending on the dimensions of the structure and its position.

NOTE The National Annex may give values for  $\lambda$  and  $\psi_{\lambda}$ . Recommended values for  $\lambda$  are given in Table 7.16 and indicative values for  $\psi_{\lambda}$  are given in Figure 7.36 for different solidity ratio  $\varphi$ .

Table 7.16 — Recommended values of  $\lambda$  for cylinders, polygonal sections, rectangular sections, sharp edged structural sections and lattice structures

No.	Position of the structure,	Effective slenderness $\lambda$
NO.	wind normal to the plane of the page	Effective stenderness $\lambda$
1	$ \begin{array}{c cccc} \hline b & \downarrow & \downarrow & \downarrow \\ \hline \ell & \downarrow & \downarrow & \downarrow \\ \hline z_g \ge b & z_g \ge 2b \\ \hline \text{for } b \le \ell \end{array} $	For polygonal, rectangular and sharp edged sections and lattice structures: for $\ell \geq 50$ m, $\lambda = 1,4$ $\ell/b$ or $\lambda = 70$ , whichever is smaller
2	$b = b_1 \le 1,5b$	for $\ell$ <15 m, $\lambda$ =2 $\ell/b$ or $\lambda$ = 70, whichever is smaller For circular cylinders: for $\ell \geq 50$ , $\lambda$ =0,7 $\ell/b$ or $\lambda$ =70, whichever is smaller for $\ell$ <15 m, $\lambda$ = $\ell/b$ or $\lambda$ =70,
3	$\frac{\frac{\ell}{2}}{\frac{b}{2}}$	whichever is smaller For intermediate values of ℓ, linear interpolation should be used
4	$b_1 \ge 2.5b$ $b \downarrow b$ $\downarrow b$ $\downarrow b$ $\downarrow c$ $\downarrow b$ $\downarrow c$ $\downarrow$	for $\ell \geq 50$ m, $\lambda = 0.7$ $\ell/b$ or $\lambda = 70$ , whichever is larger for $\ell < 15$ m, $\lambda = \ell/b$ or $\lambda = 70$ , whichever is larger For intermediate values of $\ell$ , linear interpolation should be used

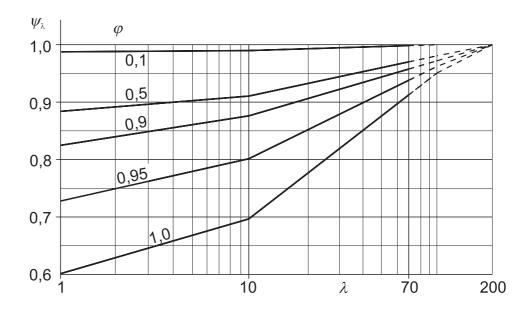


Figure 7.36 — Indicative values of the end-effect factor  $\psi_\lambda$  as a function of solidity ratio  $\varphi$  versus slenderness  $\lambda$ 

(3) The solidity ratio  $\varphi$  (see Figure 7.37) is given by Expression (7.28).

$$\varphi = \frac{A}{A_{c}} \tag{7.28}$$

where:

A is the sum of the projected areas of the members

 $A_{\rm c}$  is the overall envelope area  $A_{\rm c}$  =  $\ell \cdot b$ 

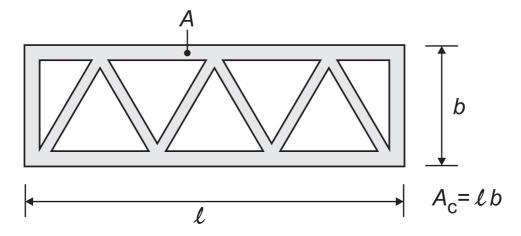


Figure 7.37 — Definition of solidity ratio  $\varphi$ 

# 8 Wind actions on bridges

## 8.1 General

- (1) This section only applies to bridges of constant depth and with cross-sections as shown in Figure 8.1 consisting of a single deck with one or more spans.
  - NOTE 1 Wind actions for other types of bridges (e.g. arch bridges, bridges with suspension cables or cable stayed, roofed bridges, moving bridges and bridges with multiple or significantly curved decks) may be defined in the National Annex.
  - NOTE 2 The angle of the wind direction to the deck axis in the vertical and horisontal planes may be defined in the National Annex.

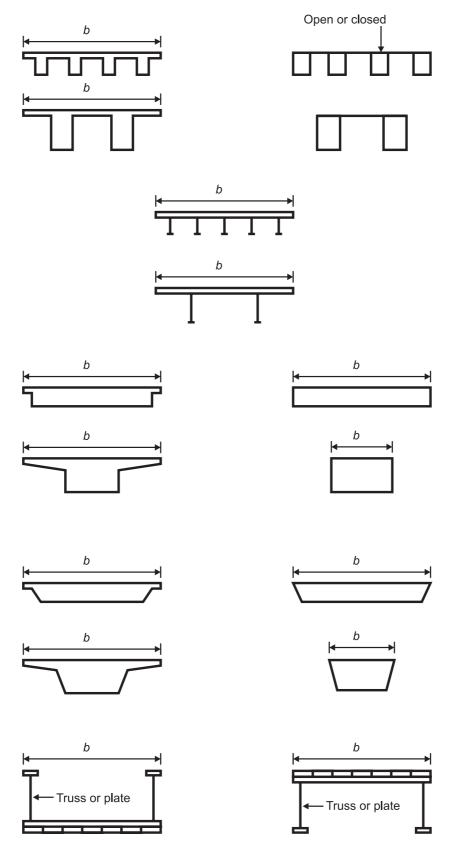


Figure 8.1 – Examples of cross-sections of normal construction decks

(2) Wind forces exerted on decks are dealt with in 8.2 and 8.3. Those exerted on piers are dealt with in 8.4. The forces exerted on various parts of a bridge due to wind blowing in the same direction should be considered as simultaneous if they are unfavourable.

(3) Wind actions on bridges produce forces in the x, y and z directions as shown in Figure 8.2,

where:

x-direction is the direction parallel to the deck width, perpendicular to the span

*y*-direction is the direction along the span

z-direction is the direction perpendicular to the deck

The forces produced in the x- and y-directions are due to wind blowing in different directions and normally are not simultaneous. The forces produced in the z-direction can result from the wind blowing in a wide range of directions; if they are unfavourable and significant, they should be taken into account as simultaneous with the forces produced in any other direction.

NOTE The notation used for bridges differs from that defined in 1.6. The following notations are used for bridges:

- L length in y-direction
- b width in x-direction
- d depth in z-direction

In Figure 8.2 the values to be given to *L*, *b* and *d* in various cases are, where relevant, more precisely defined in further clauses. When Sections 5 to 7 are referred to, the notations for *b* and *d* need to be readjusted.

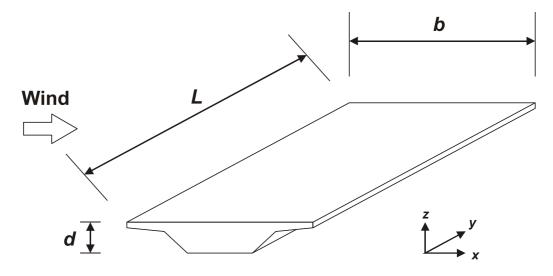


Figure 8.2 — Directions of wind actions on bridges

(4) Where road traffic is considered to be simultaneous with the wind (see A2.2.1 and A2.2.2 in Annex A2 to EN 1990) the combination value  $\psi_0 F_{wk}$  of the wind action on the bridge and on the vehicles should be limited to a value  $F_w^*$  determined by substituting a value  $v_{b,0}^*$  for the fundamental value of the basic velocity  $v_{b,0}$ .

NOTE The National Annex may give a value for  $v_{\rm b,0}^{\star}$  . The recommended value is 23 m/s.

(5) Where railway traffic is considered to be simultaneous with the wind (see A2.2.1 and A2.2.4 in Annex A2 to EN 1990) the combination value  $\psi_0 F_{wk}$  of the wind action on the bridge and on the trains should be limited to a value  $F_{w}^{"}$  determined by substituting a value  $v_{b,0}^{"}$  for the fundamental value of the basic velocity  $v_{b,0}$ .

NOTE The value of  $v_{b,0}^{**}$  may be defined in the National Annex. The recommended value of  $v_{b,0}^{**}$  is 25 m/s.

# 8.2 Choice of the response calculation procedure

- (1) It should be assessed whether a dynamic response procedure is needed for bridges.
  - NOTE 1 The National Annex may give criteria and procedures.
  - NOTE 2 If a dynamic response procedure is not needed,  $c_s c_d$  may be taken equal to 1,0.
  - NOTE 3 For normal road and railway bridge decks of less than 40 m span a dynamic response procedure is generally not needed. For the purpose of this categorization, normal bridges may be considered to include bridges constructed in steel, concrete, aluminium or timber, including composite construction, and whose shape of cross sections is generally covered by Figure 8.1.

## 8.3 Force coefficients

(1) Force coeffcients for parapets and gantries on bridges should be determined were relevant.

NOTE The National Annex may give force coefficients for parapets and gantries on bridges. It is recommended to use Section 7.4.

#### 8.3.1 Force coefficients in x-direction (general method)

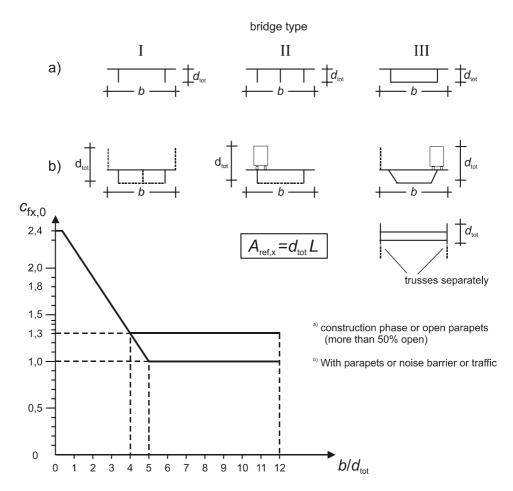
(1) Force coefficients for wind actions on bridge decks in the x-direction are given by :

$$\boldsymbol{c}_{\mathrm{f,x}} = \boldsymbol{c}_{\mathrm{fx,0}} \tag{8.1}$$

where:

 $c_{fx,0}$  is the force coefficient without free-end flow (see 7.13).

- NOTE 1 A bridge has usually no free-end flow because the flow is deviated only along two sides (over and under the bridge deck).
- NOTE 2 For normal bridges  $c_{fx,0}$  may be taken equal to 1,3. Alternatively,  $c_{fx,0}$  may be taken from Figure 8.3.
- NOTE 3 Where the angle of inclination of the wind exceeds 10°, the drag coefficient may be derived from special studies. This angle of inclination may be due to the slope of the terrain in the on-coming wind direction.



Where two generally similar decks are at the same level and separated transversally by a gap not exceeding significantly 1 m, the wind force on the windward structure may be calculated as if it were a single structure. In other cases special consideration may have to be given to wind-structure interaction.

Figure 8.3 — Force coefficient for bridges,  $c_{fx,0}$ 

(2) Where the windward face is inclined to the vertical (see Figure 8.4), the drag coefficient  $c_{fx,0}$  may be reduced by 0,5 % per degree of inclination,  $\alpha_1$  from the vertical, limited to a maximum reduction of 30 %.

NOTE This reduction is not applicable to  $F_W$ , defined in 8.3.2, unless otherwise specified in the National Annex.

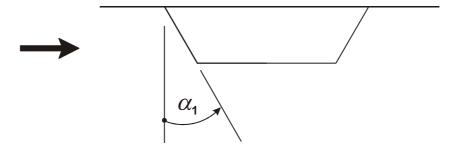


Figure 8.4 — Bridge with inclined windward face

- (3) Where a bridge deck is sloped transversely,  $c_{fx,0}$  should be increased by 3% per degree of inclination, but not more than 25 %.
- (4) Reference areas  $A_{ref,x}$  for load combinations without traffic load should be defined as:
- (a) for decks with plain (web) beams, the sum of (see Figure 8.5 and Table 8.1):

- 1) the face area of the front main girder
- 2) the face area of those parts of the other main girders projecting under (underlooking) this first one
- 3) the face area of the part of one cornice or footway or ballasted track projecting over the front main girder
- 4) the face area of solid restraints or noise barriers, where relevant, over the area described in 3) or, in the absence of such equipment, 0,3 m for each open parapet or barrier.
- b) for decks with trussed girders, the sum of :
  - 1) the face area of one cornice or footway or ballasted track
  - 2) those solid parts of all main truss girders in normal projected elevation situated above or underneath the area as described in 1).
  - 3) the face area of solid restraints or noise barriers, if relevant, over the area described in 1) or, in the absence of such equipment, 0,3 m for each open parapet or barrier.

However, the total reference area should not exceed that obtained from considering an equivalent plain (web) beam of the same overall depth, including all projecting parts.

c) for decks with several main girders during construction, prior to the placement of the carriageway slab : the face area of two main girders.

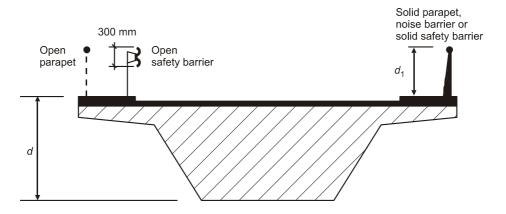


Figure 8.5 — Depth to be used for  $A_{ref,x}$ 

Table 8.1 — Depth to be used for  $A_{ref,x}$ 

Road restraint system	on one side	on both sides
Open parapet or open safety barrier	d + 0,3 m	d + 0,6 m
Solid parapet or solid safety barrier	d + d <sub>1</sub>	d + 2d <sub>1</sub>
Open parapet and open safety barrier	d + 0,6 m	d + 1,2 m

- (5) Reference areas  $A_{\text{ref},x}$  for load combinations with traffic load are as specified in (4), with the following modification. Instead of the areas described above in a) 3) and 4) and b) 3), the following should be taken into account where they are larger:
- a) for road bridges, a height of 2 m from the level of the carriageway, on the most unfavourable length, independently of the location of the vertical traffic loads,

- b) for railway bridges, a height of 4 m from the top of the rails, on the total length of the bridge.
- (6) The reference height,  $z_e$ , may be taken as the distance from the lowest ground level to the centre of the bridge deck structure, disregarding other parts (e.g. parapets) of the reference areas.
- (7) Wind pressure effects of passing vehicles are outside the scope of this Part. Wind effects induced by passing trains see EN 1991-2..

# 8.3.2 Force in x-direction – Simplified Method

(1) Where it has been assessed that a dynamic response procedure is not necessary, the wind force in the *x*-direction may be obtained using Expression (8.2):

$$F_{W} = \frac{1}{2} \cdot \rho \cdot V_{b}^{2} \cdot C \cdot A_{ref,x}$$
 (8.2)

where:

 $v_b$  is the basic wind speed (see 4.2 (2))

is the wind load factor.  $C = c_e \cdot c_{f,x}$ , where  $c_e$  is the exposure factor given in 4.5 and  $c_{f,x}$  is given in 8.3.1(1)

 $A_{\text{ref},x}$  is the reference area given in 8.3.1

 $\rho$  is the density of air (see 4.5)

NOTE C-values may be defined in the National Annex. Recommended values are given in Table 8.2.

Table 8.2 — Recommended values of the force factor C for bridges

b/d <sub>tot</sub>	z <sub>e</sub> ≤ 20 m	z <sub>e</sub> = 50 m
≤ 0,5	5,7	7,1
≥ 4,0	3,1	3,8

This table is based on the following assumptions:

- terrain category II according to Table 4.1
- force coefficient c<sub>f,x</sub> according to 8.3.1 (1)
- $-c_0=1,0$
- $-k_{l}=1.0$

For intermediate values of  $b/d_{tot}$ , and of  $z_e$  linear interpolation may be used

# 8.3.3 Wind forces on bridge decks in z-direction

(1) Force coefficients  $c_{f,z}$  should be defined for wind action on the bridge decks in the z-direction, both upwards and downwards (lift force coefficients).  $c_{f,z}$  should not be used to calculate vertical vibrations of the bridge deck.

NOTE 1 The National Annex may give values for  $c_{f,z}$ . In the absence of wind tunnel tests the recommended value may be taken equal to  $\pm 0.9$ . This value takes globally into account the influence of a possible transverse slope of the deck, of the slope of terrain and of fluctuations of the angle of the wind direction with the deck due to turbulence.

As an alternative  $c_{f,z}$  may be taken from Figure 8.6. In using it:

the depth dtot may be limited to the depth of the deck structure, disregarding the traffic and any bridge equipment

for flat, horizontal terrain the angle  $\alpha$  of the wind with the horizontal may be taken as  $\pm$  5° due to turbulence. This is also valid for hilly terrain when the bridge deck is at least 30 m above ground.

NOTE 2 This force may have significant effects only if the force is of the same order as the dead load.

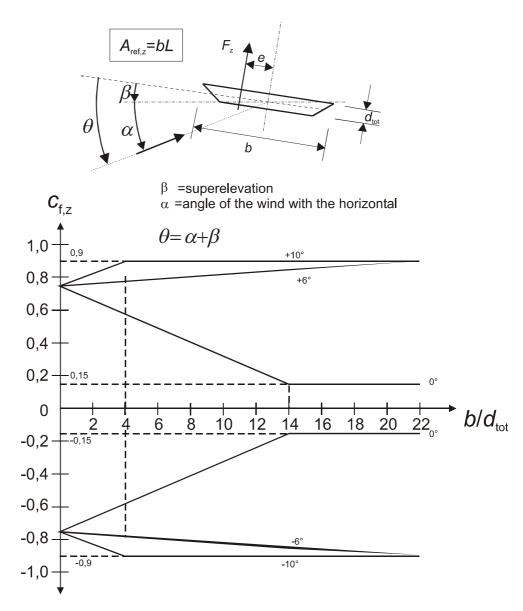


Figure 8.6 — Force coefficient  $c_{\rm f,z}$  for bridges with transversal slope and wind inclination

(2) The reference area  $A_{ref,z}$  is equal to the plan area (see Figure 8.2):

$$A_{\text{ref},z} = b \cdot L \tag{8.3}$$

- (3) No end-effect factor should be taken into account.
- (4) The reference height is the same as for  $c_{f,x}$  (see 8.3.1(6)).

(5) If not otherwise specified the eccentricity of the force in the x-direction may be set to e = b/4.

# 8.3.4 Wind forces on bridge decks in y-direction

(1) If necessary, the longitudinal wind forces in y-direction should be taken into account.

NOTE The National Annex may give the values. The recommended values are:

- for plated bridges, 25 % of the wind forces in x-direction,
- for truss bridges, 50 % of the wind forces in x-direction.

# 8.4 Bridge piers

#### 8.4.1 Wind directions and design situations

- (1) The wind actions on bridge decks and their supporting piers should be calculated by identifying the most unfavourable direction of the wind on the whole structure for the effect under consideration.
- (2) Separate calculations of wind actions should be made for transient design situations during construction phases when no horizontal transmission or redistribution of wind actions by the deck is possible. If during such phases a pier may bear cantilevering deck parts or scaffoldings, a possible asymmetry of wind actions on such elements should be taken into account.

NOTE Execution transient situations are usually more critical for piers and for some types of decks subject to particular execution methods than the persistent ones. For characteristic values during transient design situations see EN 1991-1-6. For scaffoldings, see 7.11.

## 8.4.2 Wind effects on piers

- (1) Wind effects on piers should be calculated by using the general format defined in this Eurocode. For overall loads the provisions of Clauses 7.6, 7.8 or 7.9.2 should be used.
  - NOTE 1 Simplified rules may be given in the National Annex.
  - NOTE 2 The National Annex may give procedures for the treatment of asymmetric loading. The recommended procedure is to completely remove the design wind load from those parts of the structure where its action will produce a beneficial effect (see 7.1.2 (1)).

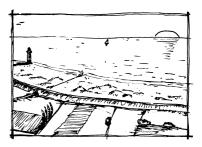
# Annex A (informative)

# **Terrain effects**

# A.1 Illustrations of the upper roughness of each terrain category

# Terrain category 0

Sea, coastal area exposed to the open sea



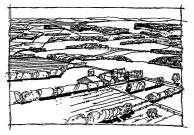
## Terrain category I

Lakes or area with negligible vegetation and without obstacles



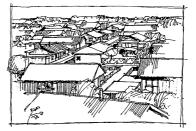
# Terrain category II

Area with low vegetation such as grass and isolated obstacles (trees, buildings) with separations of at least 20 obstacle heights



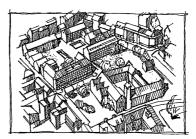
# Terrain category III

Area with regular cover of vegetation or buildings or with isolated obstacles with separations of maximum 20 obstacle heights (such as villages, suburban terrain, permanent forest)



# **Terrain category IV**

Area in which at least 15 % of the surface is covered with buildings and their average height exceeds 15 m



# A.2 Transition between roughness categories 0, I, II, III and IV

(1) The transition between different roughness categories has to be considered when calculating  $q_0$  and  $c_s c_d$ .

NOTE The procedure to be used may be given in the National Annex. Two recommended procedures, Procedure 1 and Procedure 2, are given below.

#### Procedure 1

If the structure is situated near a change of terrain roughness at a distance:

- less than 2 km from the smoother category 0
- less than 1 km from the smoother categories I to III

the smoother terrain category in the upwind direction should be used

Small areas (less than 10 % of the area under consideration) with deviating roughness can be ignored.

#### Procedure 2

- a) Determine the roughness categories for the upstream terrain in the angular sectors to be considered.
- b) For every angular sector, determine the distance x from the building to the upstream roughness changes
- c) If the distance *x* from the building to a terrain with lower roughness length is smaller than the values given in Table A.1, then the lower value for the roughness length should be used for the angular sector considered. If this distance *x* is larger than the value in Table A.2, the higher value for the roughness length should be used.

Small areas (less than 10 % of the area under consideration) with deviating roughness can be ignored.

Where no distance x is given in Table A.1 or for heights exceeding 50 m, the smaller roughness length should be used.

For intermediate values of height z, linear interpolation may be used.

A building in a certain terrain category may be calculated in a lower terrain category if it is situated within the distance limits defined in Table A.1

# Table A.1 — Distance x

Height z	I to II	I to III
5 m	0,50 km	5,00 km
7 m	1,00 km	10,00 km
10 m	2,00 km	20,00 km
15 m	5,00 km	
20 m	12,00 km	
30 m	20,00 km	
50 m	50,00 km	

Height z	II to III	II to IV
5 m	0,30 km	2,00 km
7 m	0,50 km	3,50 km
10 m	1,00 km	7,00 km
15 m	3,00 km	20,00 km
20 m	7,00 km	
30 m	10,00 km	
50 m	30,00 km	

Height z	III to IV
5 m	0,20 km
7 m	0,35 km
10 m	0,70 km
15 m	2,00 km
20 m	4,50 km
30 m	7,00 km
50 m	20,00 km

# A.3 Numerical calculation of orography coefficients

(1) At isolated hills and ridges or cliffs and escarpments different wind velocities occur dependent on the upstream slope  $\Phi = H/L_{II}$  in the wind direction, where the height H and the length  $L_{II}$  are defined in Figure A. 1.

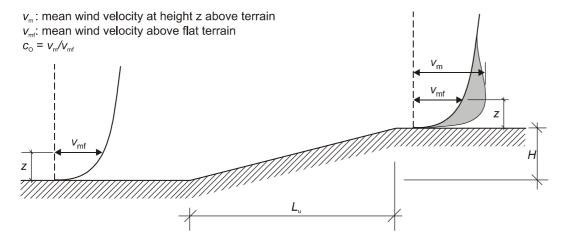


Figure A.1 — Illustration of increase of wind velocities over orography

(2) The largest increase of the wind velocities occurs near the top of the slope and is determined from the orography factor  $c_0$ , see Figure A.1. The slope has no significant effect on the standard deviation of the turbulence defined in 4.4 (1).

NOTE The turbulence intensity will decrease with increasing wind velocity and equal value for the standard deviation

- (3) The orography factor,  $c_0(z) = v_m/v_{mf}$  accounts for the increase of mean wind speed over isolated hills and escarpments (not undulating and mountainous regions). It is related to the wind velocity at the base of the hill or escarpment. The effects of orography should be taken into account in the following situations:
- − For sites on upwind slopes of hills and ridges: where 0,05 <  $\Phi$  ≤ 0,3 and |x| ≤  $L_u$  / 2
- − For sites on downwind slopes of hills and ridges: where Φ < 0.3 and  $x < L_d/2$  where Φ ≥ 0.3 and x < 1.6 H
- − For sites on upwind slopes of cliffs and escarpments: where 0,05 <  $\Phi$  ≤ 0,3 and |x| ≤  $L_u$  / 2
- For sites on downwind slopes of cliffs and escarpments: where  $\Phi$  < 0,3 and x < 1,5  $L_e$  where  $\Phi$  ≥ 0,3 and x < 5 H

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It is defined by:

$$c_0 = 1$$
 for  $\phi < 0.05$  (A.1)

$$c_0 = 1 + 2 \cdot s \cdot \Phi$$
 for  $0.05 < \Phi < 0.3$  (A.2)

$$c_0 = 1 + 0.6 \cdot s$$
 for  $\Phi > 0.3$  (A.3)

#### where:

- s is the orographic location factor, to be obtained from Figure A.2 or Figure A.3 scaled to the length of the effective upwind slope length,  $L_e$
- $\Phi$  is the upwind slope  $H/L_u$  in the wind direction (see Figure A.2 and Figure A.3)
- L<sub>e</sub> is the effective length of the upwind slope, defined in Table A.2
- $L_{\rm u}$  is the actual length of the upwind slope in the wind direction
- $L_{\rm d}$  is the actual length of the downwind slope in the wind direction
- *H* is the effective height of the feature
- x is the horizontal distance of the site from the top of the crest
- z is the vertical distance from the ground level of the site

Table A.2 — Values of the effective length  $L_{\rm e}$ .

Type of slope ( $\Phi = H/L_u$ )		
<b>Shallow</b> (0,05 < <i>Ф</i> < 0,3)	<b>Steep</b> ( <i>Ф</i> > 0,3)	
$L_{\rm e} = L_{\rm u}$	$L_{\rm e} = H/0,3$	

NOTE The calculated graphs in Figures A.2 and A.3 exceed the area of application as defined above. The consideration of orographic effects beyond these boundaries is optional.

(4) In valleys,  $c_0(z)$  may be set to 1,0 if no speed up due to funnelling effects is to be expected. For structures situated within, or for bridges spanning steep-sided valleys care should be taken to account for any increase of wind speed caused by funnelling.

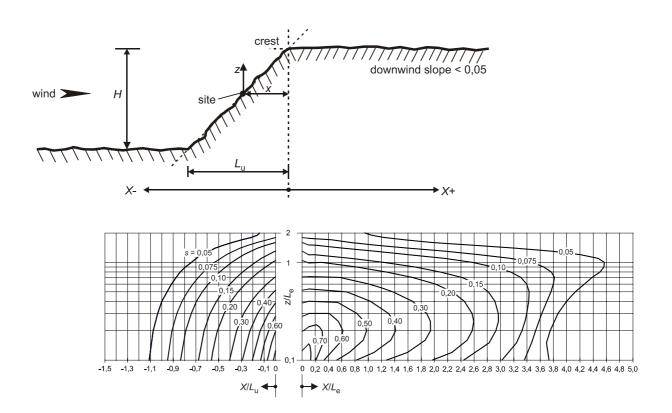


Figure A.2 — Factor s for cliffs and escarpments

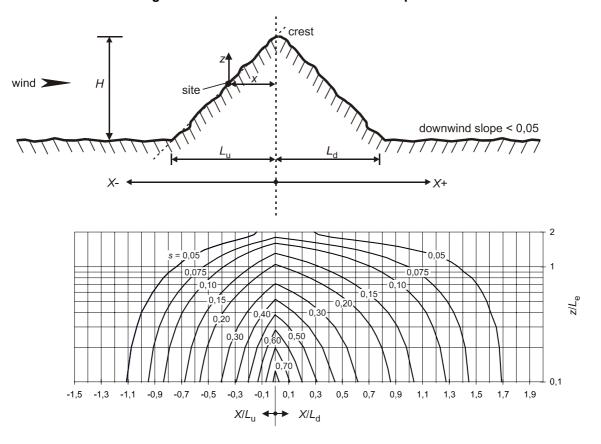


Figure A.3 — Factor s for hills and ridges

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(5) Expressions A.4 to A.7 and A.11 may be used to compute the value of orographic location factor, s. As those expressions are empirical, it is most important that values of the parameters used must be restricted to the stated ranges, otherwise invalid values will be generated.

# a) upwind section for all orography (Figures A.2 and A.3):

For the ranges

$$-1.5 \le \frac{X}{L_{11}} \le 0$$
 and  $0 \le \frac{z}{L_{a}} \le 2.0$ 

take:

$$s = A \cdot e^{\left(B \frac{X}{L_u}\right)} \tag{A.4}$$

where

$$A = 0.1552 \cdot \left(\frac{z}{L_{e}}\right)^{4} - 0.8575 \cdot \left(\frac{z}{L_{e}}\right)^{3} + 1.8133 \cdot \left(\frac{z}{L_{e}}\right)^{2} - 1.9115 \cdot \left(\frac{z}{L_{e}}\right) + 1.0124$$
(A.5)

and

$$B = 0.3542 \cdot \left(\frac{z}{L_{\rm e}}\right)^2 - 1.0577 \cdot \left(\frac{z}{L_{\rm e}}\right) + 2.6456 \tag{A.6}$$

when

$$\frac{X}{L_{11}} < -1.5 \text{ or } \frac{z}{L_{e}} > 2$$

take:

s = 0

# b) downwind section for cliffs and escarpments (Figure A.2):

For the ranges

$$0.1 \le \frac{X}{L_e} \le 3.5$$
 and  $0.1 \le \frac{z}{L_e} \le 2.0$ 

take:

$$s = A \cdot \left( \log \left[ \frac{X}{L_0} \right] \right)^2 + B \cdot \left( \log \left[ \frac{X}{L_0} \right] \right) + C$$
 (A.7)

where

$$A = -1,3420 \cdot \left( \log \left[ \frac{z}{L_a} \right] \right)^3 - 0,8222 \cdot \left( \log \left[ \frac{z}{L_a} \right] \right)^2 + 0,4609 \cdot \log \left[ \frac{z}{L_a} \right] - 0,0791$$
 (A.8)

$$B = -1,0196 \cdot \left( \log \left[ \frac{z}{L_e} \right] \right)^3 - 0,8910 \cdot \left( \log \left[ \frac{z}{L_e} \right] \right)^2 + 0,5343 \cdot \log \left[ \frac{z}{L_e} \right] - 0,1156$$
 (A.9)

and

$$C = 0.8030 \cdot \left( \log \left[ \frac{z}{L_e} \right] \right)^3 + 0.4236 \cdot \left( \log \left[ \frac{z}{L_e} \right] \right)^2 - 0.5738 \cdot \log \left[ \frac{z}{L_e} \right] + 0.1606$$
 (A.10)

For the range

$$0 \le \frac{X}{L_{\rm e}} \le 0.1 ,$$

interpolate between values for

$$\frac{X}{L_e} = 0$$
 (s = A in Expression A.5) and  $\frac{X}{L_e} = 0.1$ .

when:  $\frac{z}{L_e}$  < 0,1 use the values for  $\frac{z}{L_e}$  = 0,1.

when:  $\frac{z}{L_d} > 3.5$  or  $\frac{z}{L_e} > 2.0$  take the value s = 0

# c) downwind section for hills and ridges (Figure A.3):

For the ranges

$$0 \le \frac{X}{L_d} \le 2.0$$
 and  $0 \le \frac{z}{L_e} \le 2.0$ 

take:

$$s = A \cdot e^{\left(B \cdot \frac{X}{L_d}\right)} \tag{A.11}$$

where:

$$A = 0.1552 \cdot \left(\frac{z}{L_{e}}\right)^{4} - 0.8575 \cdot \left(\frac{z}{L_{e}}\right)^{3} + 1.8133 \cdot \left(\frac{z}{L_{e}}\right)^{2} - 1.9115 \cdot \left(\frac{z}{L_{e}}\right) + 1.0124$$
(A.12)

and

$$B = -0.3056 \cdot \left(\frac{z}{L_e}\right)^2 + 1.0212 \cdot \left(\frac{z}{L_e}\right) - 1.7637 \tag{A.13}$$

when

$$\frac{X}{L_{\rm d}} > 2.0 \text{ or } \frac{z}{L_{\rm e}} > 2.0$$

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take:

s = 0

NOTE Expressions A.5 and A.12 are identical.

# A.4 Neighbouring structures

(1) If a building is more than twice as high as the average height  $h_{\text{ave}}$  of the neighbouring structures then, as a first approximation, the design of any of those nearby structures may be based on the peak velocity pressure at height  $z_n$  ( $z_e = z_n$ ) above ground (Expression A.14), see Figure A.4.

$$x \le r:$$

$$z_{n} = \frac{1}{2} \cdot r$$

$$r < x < 2 \cdot r:$$

$$z_{n} = \frac{1}{2} \left( r - \left(1 - \frac{2 \cdot h_{low}}{r}\right) \cdot (x - r) \right)$$

$$x \ge 2 \cdot r:$$

$$z_{n} = h_{low}$$
(A.14)

in which the radius r is:

$$r = h_{\text{high}}$$
 if  $h_{\text{high}} \le 2 \cdot d_{\text{large}}$   $r = 2 \cdot d_{\text{large}}$  if  $h_{\text{high}} > 2 \cdot d_{\text{large}}$ 

The structural height  $h_{low}$ , the radius r, the distance x and the dimensions  $d_{small}$  and  $d_{large}$  are illustrated in Figure A.4 Increased wind velocities can be disregarded when  $h_{low}$  is more than half the height  $h_{high}$  of the high building, i.e.  $z_n = h_{low}$ .

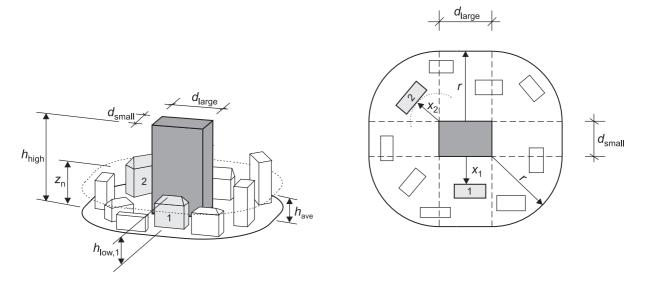


Figure A.4 — Influence of a high rise building, on two different nearby structures (1 and 2)

# A.5 Displacement height

(1) For buildings in terrain category IV, closely spaced buildings and other obstructions causes the wind to behave as if the ground level was raised to a displacement height,  $h_{\rm dis}$ .  $h_{\rm dis}$  may be determined by Expression (A.15), see Figure A.5. The profile of peak velocity pressure over height (see Figure 4.2) may be lifted by a height  $h_{\rm dis}$ .

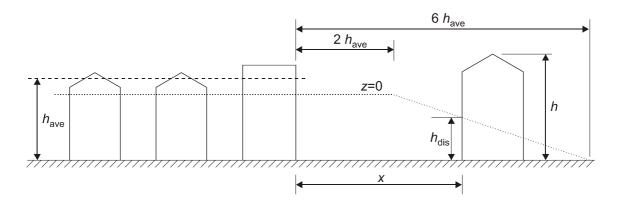


Figure A.5 — Obstruction height and upwind spacing

$$x \le 2 \cdot h_{\text{ave}}$$
  $h_{\text{dis}}$  is the lesser of  $0.8 \cdot h_{\text{ave}}$  or  $0.6 \cdot h$   $2 \cdot h_{\text{ave}} < x < 6 \cdot h_{\text{ave}}$   $h_{\text{dis}}$  is the lesser of  $1.2 \cdot h_{\text{ave}} - 0.2 \cdot x$  or  $0.6 \cdot h$  (A.15)  $x \ge 6 \cdot h_{\text{ave}}$   $h_{\text{dis}} = 0$ 

In the absence of more accurate information the obstruction height may be taken as  $h_{ave}$  = 15 m for terrain category IV.

These rules are direction dependent, the values of  $h_{\text{ave}}$  and x should be established for each 30° sector as described in 4.3.2.

# Annex B

(informative)

# Procedure 1 for determining the structural factor c<sub>s</sub>c<sub>d</sub>

#### **B.1 Wind turbulence**

(1) The turbulent length scale L(z) represents the average gust size for natural winds. For heights z below 200 m the turbulent length scale may be calculated using Expression (B.1):

$$L(z) = L_{t} \cdot \left(\frac{z}{z_{t}}\right)^{\alpha} \qquad \text{for} \qquad z \ge z_{\min}$$

$$L(z) = L(z_{\min}) \qquad \text{for} \qquad z < z_{\min}$$
(B.1)

with a reference height of  $z_t$  = 200 m, a reference length scale of  $L_t$  = 300 m, and with  $\alpha$  = 0,67 + 0,05 ln( $z_0$ ), where the roughness length  $z_0$  is in m. The minimum height  $z_{min}$  is given in Table 4.1.

(2) The wind distribution over frequencies is expressed by the non-dimensional power spectral density function  $S_L(z,n)$ , which should be determined using Expression (B.2):

$$S_{L}(z,n) = \frac{n \cdot S_{v}(z,n)}{\sigma_{v}^{2}} = \frac{6.8 \cdot f_{L}(z,n)}{(1+10.2 \cdot f_{L}(z,n))^{5/3}}$$
(B.2)

where  $S_v(z,n)$  is the one-sided variance spectrum, and

 $f_{\rm L}(z,n) = \frac{n \cdot L(z)}{v_{\rm m}(z)}$  is a non-dimensional frequency determined by the frequency  $n = n_{\rm 1,x}$ , the natural

frequency of the structure in Hz, by the mean velocity  $v_m(z)$  and the turbulence length scale L(z) defined in (B. 1). The power spectral density function is illustrated in Figure B.1.

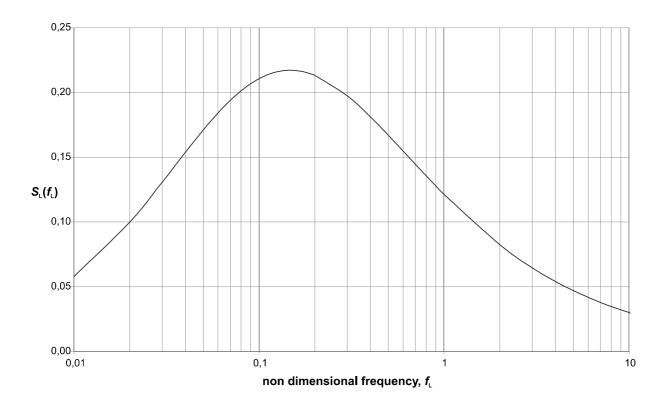


Figure B.1 —Power spectral density function  $S_L(f_L)$ 

# B.2 Structural factor $c_{s}c_{d}$

- (1) The structural factor  $c_{\rm S}c_{\rm d}$  is defined in 6.3.1.
- (2) The background factor  $B^2$  allowing for the lack of full correlation of the pressure on the structure surface may be calculated using Expression (B.3):

$$B^{2} = \frac{1}{1 + 0.9 \cdot \left(\frac{b+h}{L(z_{e})}\right)^{0.63}}$$
 (B.3)

where:

- b, h is the width and height of the structure, see Figure 6.1.
- $L(z_e)$  is the turbulent length scale given in B. 1 (1) at reference height  $z_e$  defined in Figure 6.1. It is on the safe side to use  $B^2 = 1$ .
- (3) The peak factor  $k_p$ , defined as the ratio of the maximum value of the fluctuating part of the response to its standard deviation, should be obtained from Expression (B.4) and is shown in Figure B.2.

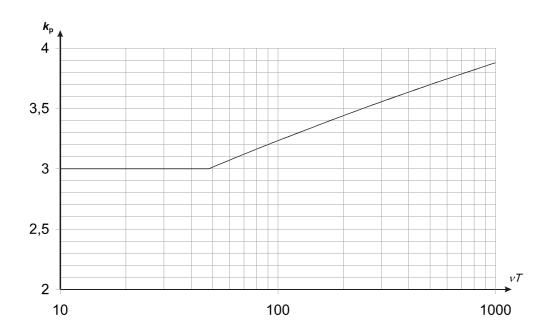


Figure B.2 —Peak factor

$$k_{\rm p} = \sqrt{2 \cdot \ln(\nu \cdot T)} + \frac{0.6}{\sqrt{2 \cdot \ln(\nu \cdot T)}}$$
 or  $k_{\rm p}$ = 3 whichever is larger (B.4)

where:

 $\nu$  is the up-crossing frequency given in (4)

T is the averaging time for the mean wind velocity, T = 600 seconds.

(4) The up-crossing frequency  $\nu$  should be obtained from Expression (B.5):

$$v = n_{1,x} \sqrt{\frac{R^2}{B^2 + R^2}}$$
 ;  $v \ge 0.08 \ Hz$  (B.5)

where  $n_{1,x}$  is the natural frequency of the structure, which may be determined using Annex F. The limit of  $v \ge 0.08$  Hz corresponds to a peak factor of 3,0.

(5) The resonance response factor  $R^2$  allowing for turbulence in resonance with the considered vibration mode of the structure should be determined using Expression (B.6):

$$R^{2} = \frac{\pi^{2}}{2 \cdot \delta} \cdot S_{L}(z_{e}, n_{1,x}) \cdot R_{h}(\eta_{h}) \cdot R_{b}(\eta_{b})$$
(B.6)

where:

 $\delta$  is the total logarithmic decrement of damping given in F.5

 $S_L$  is the non-dimensional power spectral density function given in B. 1 (2)

 $R_h$ ,  $R_b$  is the aerodynamic admittance functions given in (6).

(6) The aerodynamic admittance functions  $R_h$  and  $R_b$  for a fundamental mode shape may be approximated using Expressions (B.7) and (B.8):

$$R_{h} = \frac{1}{\eta_{h}} - \frac{1}{2 \cdot {\eta_{h}}^{2}} (1 - e^{-2 \cdot \eta_{h}}); \qquad R_{h} = 1 \quad \text{for} \quad \eta_{h} = 0$$
 (B.7)

$$R_{b} = \frac{1}{\eta_{b}} - \frac{1}{2 \cdot {\eta_{b}}^{2}} (1 - e^{-2 \cdot \eta_{b}}); \qquad R_{b} = 1 \quad \text{for} \quad \eta_{b} = 0$$
(B.8)

with: 
$$\eta_{\rm h} = \frac{4.6 \cdot h}{L(z_{\rm e})} \cdot f_{\rm L}(z_{\rm e}, n_{\rm 1,x})$$
 and  $\eta_{\rm b} = \frac{4.6 \cdot b}{L(z_{\rm e})} \cdot f_{\rm L}(z_{\rm e}, n_{\rm 1,x})$ 

NOTE For mode shapes with internal node points more detailed calculations should be used.

# **B.3 Number of loads for dynamic response**

(1) Figure B.3 shows the number of times  $N_g$ , that the value  $\Delta S$  of an effect of the wind is reached or exceeded during a period of 50 years.  $\Delta S$  is expressed as a percentage of the value  $S_k$ , where  $S_k$  is the effect due to a 50 years return period wind action.

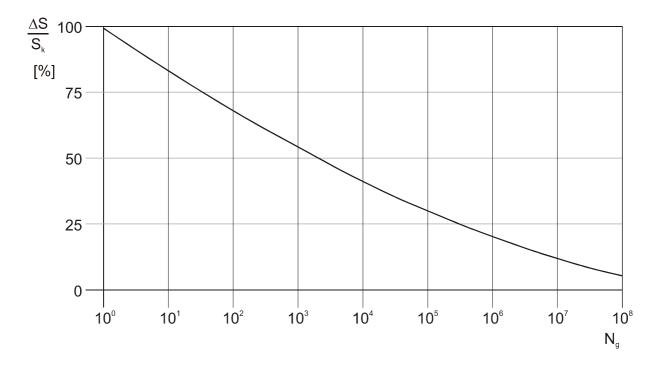


Figure B.3 — Number of gust loads  $N_g$  for an effect  $\Delta S/S_k$  during a 50 years period

The relationship between  $\Delta S/S_k$  and  $N_g$  is given by Expression B.9.

$$\frac{\Delta S}{S_{\nu}} = 0.7 \cdot (\log(N_{\rm g}))^2 - 17.4 \cdot \log(N_{\rm g}) + 100$$
(B.9)

# B.4 Service displacement and accelerations for serviceability assessments of a vertical structure

- (1) The maximum along-wind displacement is determined from the equivalent static wind force defined in 5.3.
- (2) The standard deviation  $\sigma_{a,x}$  of the characteristic along-wind acceleration of the structural point at height *z* should be obtained using Expression (B.10):

$$\sigma_{a,x}(z) = \frac{c_f \cdot \rho \cdot b \cdot I_v(z_e) \cdot V_m^2(z_e)}{m_{1,x}} \cdot R \cdot K_x \cdot \Phi_{1,x}(z)$$
(B.10)

where:

c<sub>f</sub> is the force coefficient, see Section 7

 $\rho$  is the air density, see 4.5 (1)

b is the width of the structure, defined in Figure 6.1

 $I_v(z_e)$  is the turbulence intensity at the height  $z = z_e$  above ground, see Figure 6.1 and 4.4

 $v_{\rm m}(z_{\rm e})$  is the mean wind velocity for  $z=z_{\rm e}$ , see 4.3.1 (1)

R is the square root of resonant response, see B. 2 (5)

 $K_x$  is the non-dimensional coefficient, given by Expression (B.11)

 $m_{1.x}$  is the along wind fundamental equivalent mass, see F.4 (1)

 $n_{1,x}$  is the fundamental frequency of along wind vibration of the structure; approximations are given in Annex F

- $\Phi_{1,x}(z)$  is the fundamental along wind modal shape, as a first approximation the expressions given in Annex F may be used
- (3) The non dimensional coefficient,  $K_x$ , is defined by:

$$K_{x} = \frac{\int_{0}^{h} v_{m}^{2}(z) \Phi_{1,x}(z) dz}{v_{m}^{2}(z_{e}) \cdot \int_{0}^{h} \Phi_{1,x}^{2}(z) dz}$$
(B.11)

where:

*h* is the height of the structure (see Figure 6.1).

NOTE Assuming  $\Phi_{1,x}(z) = (z/h)^{\zeta}$  (see Annex F) and  $c_0(z) = 1$  (flat terrain, see 4.3.3), Expression (B.11) can be approximated by Expression (B.12). This approximation is shown in Figure B.4

$$K_{x} = \frac{\left(2 \cdot \zeta + 1\right) \cdot \left\{ \left(\zeta + 1\right) \cdot \left[ \ln\left(\frac{z_{e}}{z_{0}}\right) + 0.5\right] - 1 \right\}}{\left(\zeta + 1\right)^{2} \cdot \ln\left(\frac{z_{e}}{z_{0}}\right)}$$
(B.12)

where:

 $z_0$  is the roughness length (Table 4.1)

 $\zeta$  is the exponent of the mode shape (see Annex F)

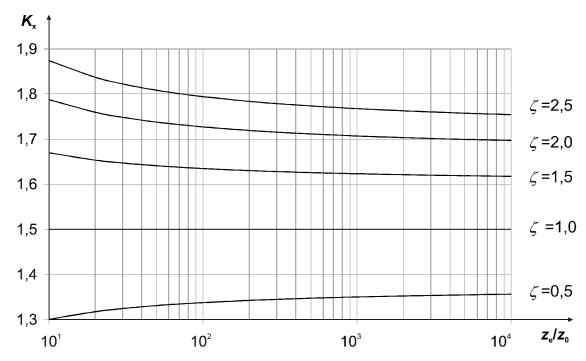


Figure B.4 — Approximation of the non dimensional coefficient,  $K_x$  according to Expression (B.12)

(4) The characteristic peak accelerations are obtained by multiplying the standard deviation in (2) by the peak factor in B. 2 (3) using the natural frequency as upcrossing frequency, i.e.  $\nu = n_{1,x}$ .

# Annex C

(informative)

# Procedure 2 for determining the structural factor $c_{\rm s}c_{\rm d}$

#### C.1 Wind turbulence

(1) The turbulence should be considered in accordance with B.1.

#### C.2 Structural factor

- (1) The structural factor  $c_s c_d$  is defined in 6.3.1.
- (2) The background factor  $B^2$  allowing for the lack of full correlation of the pressure on the structure surface may be calculated using Expression (C.1):

$$B^{2} = \frac{1}{1 + \frac{3}{2} \cdot \sqrt{\left(\frac{b}{L(z_{e})}\right)^{2} + \left(\frac{h}{L(z_{e})}\right)^{2} + \left(\frac{b}{L(z_{e})} \cdot \frac{h}{L(z_{e})}\right)^{2}}}$$
(C.1)

where:

- *b,h* is the width and height of the structure, see Figure 6.1
- $L(z_e)$  is the turbulent length scale given in B.1. (1) at reference height  $z_e$  defined in Figure 6.1.

It is on the safe side to use  $B^2 = 1$ .

- (3) The peak factor  $k_p$ , should be obtained from B. 2 (3).
- (4) The resonance response factor  $R^2$  allowing for turbulence in resonance with the considered vibration mode of the structure should be determined using Expression (C.2):

$$R^{2} = \frac{\pi^{2}}{2 \cdot \delta} \cdot S_{L}(z_{e}, n_{1,x}) \cdot K_{s}(n_{1,x})$$
 (C.2)

where:

- $\delta$  is the total logarithmic decrement of damping given in Annex F
- $S_L$  is the wind power spectral density function given in B. 1 (2)
- $n_{1,X}$  is the natural frequency of the structure, which may be determined using Annex F
- $K_{s}$  is the size reduction function given in (5).

(5) The size reduction function  $K_s$  may be approximated by Expression (C.3):

$$K_{s}(n) = \frac{1}{1 + \sqrt{(G_{y} \cdot \phi_{y})^{2} + (G_{z} \cdot \phi_{z})^{2} + \left(\frac{2}{\pi} \cdot G_{y} \cdot \phi_{y} \cdot G_{z} \cdot \phi_{z}\right)^{2}}}$$
(C.3)

$$\phi_{y} = \frac{c_{y} \cdot b \cdot n}{v_{m}(z_{e})} \qquad \qquad \phi_{z} = \frac{c_{z} \cdot h \cdot n}{v_{m}(z_{e})}$$

The constants  $G_y$  and  $G_z$  depend on the mode shape variation along the horizontal *y*-axis and vertical *z*-axis, respectively. The decay constants  $c_y$  and  $c_z$  are both equal to 11,5.

(6) The constant G introduced in (5) and the constant K used to calculate accelerations, are shown in Table C.1.

Table C.1 — G and K as a function of mode shape

Mode shape	Uniform	Linear	Parabolic	Sinusoidal
G:	1/2	3/8	5/18	4/ π²
K:	1	3/2	5/3	<b>4</b> /π

NOTE 1 For buildings with a uniform horizontal mode shape variation and a linear vertical mode shape variation  $\Phi(y,z) = z/h$ ,  $G_V = 1/2$ ,  $G_Z = 3/8$ ,  $K_V = 1$  and  $K_Z = 3/2$ .

NOTE 2 For chimneys with a uniform horizontal mode shape variation and a parabolic vertical mode shape variation  $\Phi(y,z) = z^2/h^2$ ,  $G_V = 1/2$ ,  $G_Z = 5/18$ ,  $K_V = 1$  and  $K_Z = 5/3$ .

NOTE 3 For bridges with a sinusoidal horizontal mode shape variation  $\Phi(y,z) = \sin(\pi \cdot y/b)$ ,  $G_y = 4/\pi^2$ ,  $G_z = 1/2$ ,  $K_y = 4/\pi$  and  $K_z = 1$ .

#### C.3 Number of loads for dynamic response

(1) The number of loads should be obtained from B. 3.

#### C.4 Service displacement and accelerations for serviceability assessments

- (1) The maximum along-wind displacement is the static displacement determined from the equivalent static wind force defined in 5.2.
- (2) The standard deviation  $\sigma_{a,x}$  of the characteristic along-wind acceleration of the structural point with coordinates (y,z) is approximately given by Expression (C.4):

$$\sigma_{a,x}(y,z) = c_f \cdot \rho \cdot I_v(z_e) \cdot v_m^2(z_e) \cdot R \cdot \frac{K_y \cdot K_z \cdot \Phi(y,z)}{\mu_{ref} \cdot \Phi_{max}}$$
(C.4)

where:

c<sub>f</sub> is the force coefficient, see Section 7

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 $\rho$  is the air density, see 4.5

 $I_{v}(z_{e})$  is the turbulence intensity at height  $z_{e}$  above ground, see 4.4 (1)

 $v_{\rm m}(z_{\rm e})$  is the characteristic mean wind velocity at height  $z_{\rm e}$ , above ground, see 4.3.1 (1)

R is the square root of the resonant response, see C.2 (4)

 $K_y, K_z$  is the constants given in C.2 (6)

 $\mu_{\text{ref}}$  is the reference mass per unit area, see F.5 (3)

 $\Phi(y,z)$  is the mode shape

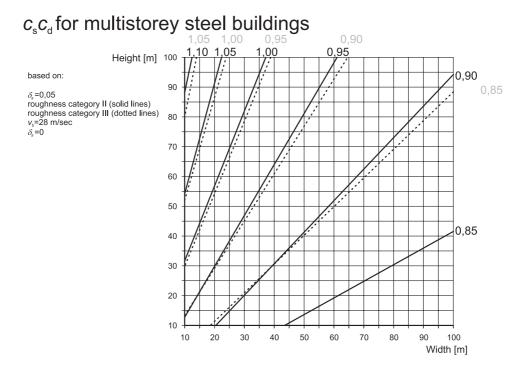
 $\Phi_{\max}$  is the mode shape value at the point with maximum amplitude

(3) The characteristic peak accelerations are obtained by multiplying the standard deviation in (2) by the peak factor in B. 2 (3) using the natural frequency as upcrossing frequency, i.e.  $v = n_{1,x}$ .

# **Annex D** (informative)

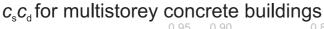
# $c_{\rm s}c_{\rm d}$ values for different types of structures

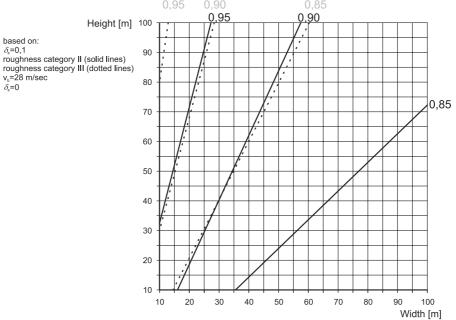
(1) The natural frequencies and mode shapes of the structures presented in this annex are derived from linear analysis or estimated using the expressions given in Annex F.



NOTE For values exceeding 1,1 the detailed procedure given in 6.3 may be applied (approved minimum value of  $c_s c_d = 0.85$ )

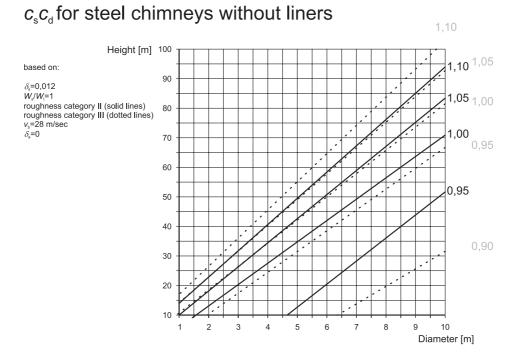
Figure D.1 —  $c_s c_d$  for multistorey steel buildings with rectangular ground plan and vertical external walls, with regular distribution of stiffness and mass (frequency according to Expression (F.2)).





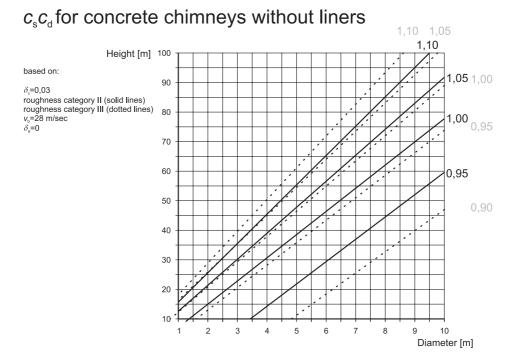
NOTE For values exceeding 1,1 the detailed procedure given in 6.3 may be applied (approved minimum value of  $c_s c_d = 0.85$ )

Figure D.2 —  $c_{\rm s}c_{\rm d}$  for multistorey concrete buildings with rectangular ground plan and vertical external walls, with regular distribution of stiffness and mass (frequency according to Expression (F.2)).



NOTE For values exceeding 1,1 the detailed procedure given in 6.3 may be applied (approved minimum value of  $c_s c_d = 0.85$ )

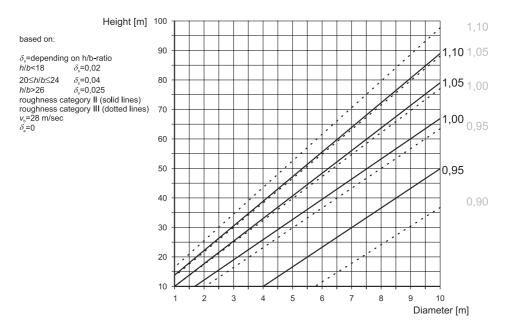
Figure D.3 —  $c_s c_d$  for steel chimneys without liners (frequency according to Expression (F.3), with  $\varepsilon_1$ =1000 and  $W_s/W_t$ =1,0).



NOTE For values exceeding 1,1 the detailed procedure given in 6.3 may be applied (approved minimum value of  $c_s c_d = 0.85$ )

Figure D.4 —  $c_s c_d$  for concrete chimneys without liners (frequency according to Expression (F.3), with  $\varepsilon_1$ =700 and  $W_s/W_t$ =1,0).

# $c_{\rm s}c_{\rm d}$ for steel chimneys with liners



NOTE For values exceeding 1,1 the detailed procedure given in 6.3 may be applied (approved minimum value of  $c_s c_d = 0.85$ )

Figure D.5 —  $c_s c_d$  for steel chimneys with liners and different values of  $\delta_s$  according to Table F.2 (frequency according to Expression (F.3), with  $\varepsilon_1$ =1000 and  $W_s/W_t$ =0,5).

# Annex E

(informative)

### Vortex shedding and aeroelastic instabilities

### E.1 Vortex shedding

#### E.1.1 General

- (1) Vortex-shedding occurs when vortices are shed alternately from opposite sides of the structure. This gives rise to a fluctuating load perpendicular to the wind direction. Structural vibrations may occur if the frequency of vortex-shedding is the same as a natural frequency of the structure. This condition occurs when the wind velocity is equal to the critical wind velocity defined in E.1.3.1. Typically, the critical wind velocity is a frequent wind velocity indicating that fatigue, and thereby the number of load cycles, may become relevant.
- (2) The response induced by vortex shedding is composed of broad-banded response that occurs whether or not the structure is moving, and narrow-banded response originating from motion-induced wind load.
  - NOTE 1 Broad-banded response is normally most important for reinforced concrete structures and heavy steel structures.
  - NOTE 2 Narrow-banded response is normally most important for light steel structures.

#### E.1.2 Criteria for vortex shedding

- (1) The effect of vortex shedding should be investigated when the ratio of the largest to the smallest crosswind dimension of the structure, both taken in the plane perpendicular to the wind, exceeds 6.
- (2) The effect of vortex shedding need not be investigated when

$$v_{\text{crit}i} > 1,25 \cdot v_{\text{m}}$$
 (E.1)

where:

 $v_{\text{crit,i}}$  is the critical wind velocity for mode *i*, as defined in E.1.3.1

 $v_{\rm m}$  is the characteristic 10 minutes mean wind velocity specified in 4.3.1 (1) at the cross section where vortex shedding occurs (see Figure E.3).

#### E.1.3 Basic parameters for vortex shedding

#### E.1.3.1 Critical wind velocity $v_{crit.i}$

(1) The critical wind velocity for bending vibration mode *i* is defined as the wind velocity at which the frequency of vortex shedding equals a natural frequency of the structure or a structural element and is given in Expression (E.2).

$$v_{\text{crit,i}} = \frac{b \cdot n_{i,y}}{St} \tag{E.2}$$

where:

- b is the reference width of the cross-section at which resonant vortex shedding occurs and where the modal deflection is maximum for the structure or structural part considered; for circular cylinders the reference width is the outer diameter
- $n_{i,y}$  is the natural frequency of the considered flexural mode i of cross-wind vibration; approximations for  $n_{1,y}$  are given in F.2
- St Strouhal number as defined in E.1.3.2.

(2) The critical wind velocity for ovalling vibration mode i of cylindrical shells is defined as the wind velocity at which two times of the frequency of vortex shedding equals a natural frequency of the ovalling mode i of the cylindrical shell and is given in Expression (E.3).

$$v_{\text{crit,i}} = \frac{b \cdot n_{i,0}}{2 \cdot St} \tag{E.3}$$

where:

- b is the outer shell diameter
- St is the Strouhal number as defined in E.1.3.2
- $n_{i,o}$  is the natural frequency of the ovalling mode *i* of the shell

NOTE 1 For shells without stiffening rings  $n_0$  is given in F.2 (3)

NOTE 2 Procedures to calculate ovalling vibrations are not covered in Annex E.

#### E.1.3.2 Strouhal number St

The Strouhal number St for different cross-sections may be taken from Table E.1

Table E.1 — Strouhal numbers St for different cross-sections

Cross-section	St			
for all De gurphage		0,18		
for all Re-numbers				
$ \begin{array}{c c} d \\ \hline 0,5 \le d/b \le 10 \end{array} $		from Figure E.1		
d d	d/b = 1	0,11		
b	<i>d/b</i> = 1,5	0,10		
linear interpolation	d/b = 2	0,14		
→ d + d + d + d + d + d + d + d + d + d	d/b = 1	0,13		
linear interpolation	d/b = 2	0,08		
→ d → b	<i>d/b</i> = 1	0,16		
linear interpolation	<i>d/b</i> = 2	0,12		
<del> </del> d	d/b = 1,3	0,11		
$\begin{array}{c} \\ \\ \\ \\ \end{array}$	<i>d/b</i> = 2,0	0,07		
linear interpolation				
NOTE Extrapolations for Strouhal numbers as function of <i>d/b</i> are not allowed.				

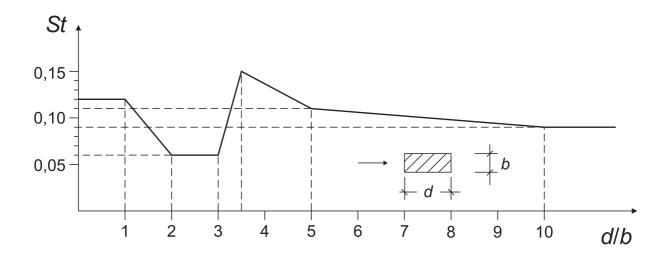


Figure E.1 — Strouhal number (St) for rectangular cross-sections with sharp corners

#### E.1.3.3 Scruton number Sc

(1) The susceptibility of vibrations depends on the structural damping and the ratio of structural mass to fluid mass. This is expressed by the Scruton number Sc, which is given in Expression (E.4).

$$Sc = \frac{2 \cdot \delta_{s} \cdot m_{i,e}}{\rho \cdot b^{2}}$$
 (E.4)

where:

 $\delta_{\rm s}$  is the structural damping expressed by the logarithmic decrement.

ho is the air density under vortex shedding conditions.

 $m_{i,e}$  is the equivalent mass  $m_e$  per unit length for mode i as defined in F.4 (1)

b is the reference width of the cross-section at which resonant vortex shedding occurs

NOTE The value of the air density  $\rho$  may be given in the National Annex. The recommended value is 1,25 kg/m<sup>3</sup>.

#### E.1.3.4 Reynolds number Re

(1) The vortex shedding action on a circular cylinder depends on the Reynolds number Re at the critical wind velocity  $v_{crit.}$ . The Reynolds number is given in Expression (E.5).

$$Re(v_{crit,i}) = \frac{b \cdot v_{crit,i}}{v}$$
 (E.5)

where:

b is the outer diameter of the circular cylinder

 $\nu$  is the kinematic viscosity of the air ( $\nu \approx 15 \cdot 10^{-6} \,\mathrm{m}^2/\mathrm{s}$ )

 $v_{\text{crit,i}}$  is the critical wind velocity, see E.1.3.1

#### E.1.4 Vortex shedding action

(1) The effect of vibrations induced by vortex shedding should be calculated from the effect of the inertia force per unit length  $F_w(s)$ , acting perpendicular to the wind direction at location s on the structure and given in Expression (E.6)

$$F_{\mathbf{w}}(\mathbf{s}) = m(\mathbf{s}) \cdot (2 \cdot \pi \cdot n_{\mathbf{i},\mathbf{v}})^{2} \cdot \Phi_{\mathbf{i},\mathbf{v}}(\mathbf{s}) \cdot \mathbf{y}_{\mathsf{F},\mathsf{max}} \tag{E.6}$$

where:

m(s) is the vibrating mass of the structure per unit length [kg/m]

 $n_{i,y}$  is the natural frequency of the structure

 $\Phi_{i,v}(s)$  is the mode shape of the structure normalised to 1 at the point with the maximum displacement

 $y_{\rm E,max}$  is the maximum displacement over time of the point with  $\Phi_{\rm LV}(s)$  equal to 1, see E.1.5

#### E.1.5 Calculation of the cross wind amplitude

#### E.1.5.1 General

- (1) Two different approaches for calculating the vortex excited cross-wind amplitudes are given in E.1.5.2 and E.1.5.3.
  - NOTE 1 The choice of calculation approach or alternative calculation procedures may be specified in the National Annex.
  - NOTE 2 A direct comparison of the approaches proposed in E.1.5.2 and E.1.5.3 is not possible because some of the input parameters are chosen for different environmental conditions. The National Annex may define the range of application for each of the approaches proposed.
  - NOTE 3 Mixing of the approaches E.1.5.2 and E.1.5.3 is not allowed, except if it is specifically stated in the text.
- (2) The approach given in E.1.5.2 can be used for various kind of structures and mode shapes. It includes turbulence and roughness effects and it may be used for normal climatic conditions.
- (3) The approach given in E.1.5.3 may be used to calculate the response for vibrations in the first mode of cantilevered structures with a regular distribution of cross wind dimensions along the main axis of the structure. Typically structures covered are chimneys or masts. It cannot be applied for grouped or in-line arrangements and for coupled cylinders. This approach allows for the consideration of different turbulence intensities, which may differ

due to meteorological conditions. For regions where it is likely that it may become very cold and stratified flow conditions may occur (e.g. in coastal areas in Northern Europe), approach E.1.5.3 may be used.

NOTE The National Annex may give the regions where very cold and stratified flow conditions may occur. For these regions the approach 2 in E.1.5.3 is more appropriate, and the National Annex may define appropriate input parameters (like  $K_a$  or turbulence intensity) which should be used in this approach.

#### E.1.5.2 Approach 1 for the calculation of the cross wind amplitudes

#### E.1.5.2.1 Calculation of displacements

The largest displacement  $y_{F,max}$  can be calculated using Expression (E.7).

$$\frac{y_{\rm F,max}}{b} = \frac{1}{{\rm S}t^2} \cdot \frac{1}{{\rm S}c} \cdot K \cdot K_{\rm W} \cdot c_{\rm lat} \tag{E.7}$$

where:

St is the Strouhal number given in Table E.1

Sc is the Scruton number given in E.1.3.3

 $K_{\rm W}$  is the effective correlation length factor given in E.1.5.2.4

K is the mode shape factor given in E.1.5.2.5

 $c_{\text{lat}}$  is the lateral force coefficient given in Table E.2

NOTE The aeroelastic forces are taken into account by the effective correlation length factor  $K_W$ .

#### E.1.5.2.2 Lateral force coefficient $c_{lat}$

(1) The basic value,  $c_{lat,0}$ , of the lateral force coefficient is given in Table E.2.

Table E.2 — Basic value of the lateral force coefficient  $c_{\mathrm{lat,0}}$  for different cross-sections

Cross-section		C <sub>lat,0</sub>
b		from Figure E.2
for all Re-numbers		
b		1,1
$0.5 \le d/b \le 10$		
d +	<i>d/b</i> = 1	0,8
b	<i>d/b</i> = 1,5	1,2
linear interpolation	<i>d/b</i> = 2	0,3
b	<i>d/b</i> = 1	1,6
linear interpolation	<i>d/b</i> = 2	2,3
d	d/b = 1	1,4
linear interpolation	d/b = 2	1,1
J d J		
<del>\                                    </del>	<i>d/b</i> = 1,3	0,8
linear interpolation	<i>d/b</i> = 2,0	1,0

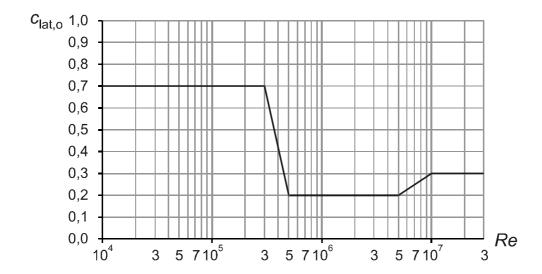


Figure E.2 — Basic value of the lateral force coefficient  $c_{\text{lat,0}}$  versus Reynolds number  $Re(v_{\text{crit,i}})$  for circular cylinders, see E.1.3.4

(2) The lateral force coefficient,  $c_{lat}$ , is given in Table E.3.

Table E.3 — Lateral force coefficient  $c_{lat}$  versus critical wind velocity ratio,  $v_{crit,i}/v_{m,Lj}$ :

Critical wind velocity ratio	C <sub>lat</sub>
$\frac{v_{crit,i}}{v_{m,Lj}} \leq 0.83$	$c_{\text{lat}} = c_{\text{lat},0}$
$0.83 \le \frac{v_{\text{crit,i}}}{v_{\text{m,Lj}}} < 1.25$	$c_{\text{lat}} = \left(3 - 2.4 \cdot \frac{v_{\text{crit,i}}}{v_{\text{m,Lj}}}\right) \cdot c_{\text{lat,0}}$
$1,25 \le \frac{v_{\text{crit,i}}}{v_{\text{m,L}_j}}$	$c_{\text{lat}} = 0$

#### where:

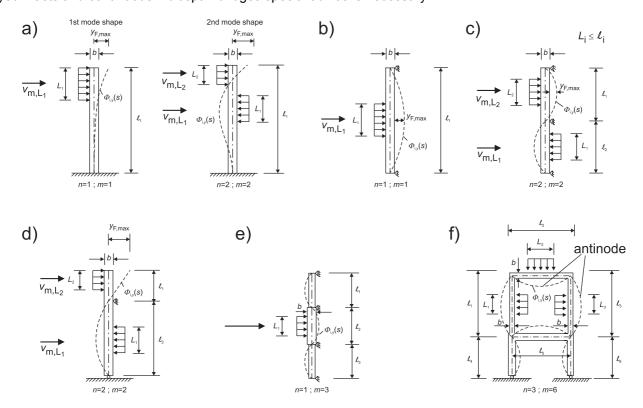
 $c_{\text{lat,0}}$  basic value of  $c_{\text{lat}}$  as given in Table E.2 and, for circular cylinders, in Figure E.2

 $v_{crit,i}$  critical wind velocity (see Expression (E.1))

 $v_{\text{m,Lj}}$  mean wind velocity (see 4.2) in the centre of the effective correlation length as defined in Figure E.3

#### E.1.5.2.3 Correlation length L

(1) The correlation length  $L_j$ , should be positioned in the range of antinodes. Examples are given in Figure E.3. For guyed masts and continuous multispan bridges special advice is necessary.



NOTE If more than one correlation length is shown, it is safe to use them simultaneously, and the highest value of  $c_{lat}$  should be used.

Figure E.3 — Examples for application of the correlation length  $L_j$  (j = 1, 2, 3)

Table E.4 — Effective correlation length  $L_i$  as a function of vibration amplitude  $y_F(s_i)$ 

$y_{F}(s_{j})/b$	L <sub>j</sub> / b	
< 0,1	6	
0,1 to 0,6	$4,8+12 \cdot \frac{y_{F}(s_{j})}{b}$	
> 0,6	12	

#### E.1.5.2.4 Effective correlation length factor $K_W$

(1) The effective correlation length factor,  $K_W$ , is given in Expression (E.8).

$$K_{W} = \frac{\sum_{j=1}^{n} \int_{L_{1}} |\Phi_{i,y}(s)| ds}{\sum_{j=1}^{m} \int_{\ell_{1}} |\Phi_{i,y}(s)| ds} \le 0.6$$
(E.8)

where:

 $\Phi_{i,y}$  is the mode shape i (see F.3).

L<sub>i</sub> is the correlation length

- $\ell_j$  is the length of the structure between two nodes (see Figure E.3); for cantilevered structures it is equal to the height of the structure
- *n* is the number of regions where vortex excitation occurs at the same time (see Figure E.3)
- m is the number of antinodes of the vibrating structure in the considered mode shape  $\Phi_{i,y}$
- s is the coordinate defined in Table E.5.
- (2) For some simple structures vibrating in the fundamental cross-wind mode and with the exciting force indicated in Table E.5 the effective correlation length factor  $K_W$  can be approximated by the expressions given in Table E.5.

Table E.5 — Correlation length factor  $K_{\mathrm{W}}$  and mode shape factor K for some simple structures

Structure	mode shape	K <sub>W</sub>	κ
	$\Phi_{i,y}(s)$		
	see F.3 with $\zeta = 2.0$ $n = 1 \; ; m = 1$	$3 \cdot \frac{L_{j} / b}{\lambda} \cdot \left[ 1 - \frac{L_{j} / b}{\lambda} + \frac{1}{3} \cdot \left( \frac{L_{j} / b}{\lambda} \right)^{2} \right]$	0,13
$ \begin{array}{c c}  & \stackrel{L}{\downarrow} \\  & \stackrel{S}{\downarrow} & \stackrel{F}{\downarrow} \\  & \stackrel{D}{\downarrow} & \stackrel{D}{\downarrow} \\  & \stackrel{D}{\downarrow} & \stackrel{D}{\downarrow} & \stackrel{D}{\downarrow} \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow \\  & \downarrow & \downarrow & \downarrow & \downarrow \\  & \downarrow &$	see Table F.1 n = 1;m = 1	$\cos\left[\frac{\pi}{2}\cdot\left(1-\frac{L_{j}/b}{\lambda}\right)\right]$	0,10
$ \begin{array}{c c}  & & & \\  & & & &$	see Table F.1 n = 1; m = 1	$\frac{L_{j}/b}{\lambda} + \frac{1}{\pi} \cdot \sin \left[ \pi \cdot \left( 1 - \frac{L_{j}/b}{\lambda} \right) \right]$	0,11
$F_2$ $F_2$ $F_3$	modal analysis  n = 3  m = 3	$\frac{\sum_{i=1}^{n} \int_{L_{j}}  \mathcal{\Phi}_{i,y}(s)  ds}{\sum_{j=1}^{m} \int_{\ell_{j}}  \mathcal{\Phi}_{i,y}(s)  ds}$	0,10

NOTE 1 The mode shape,  $\Phi_{i,y}(s)$ , is taken from F.3. The parameters n and m are defined in Expression (E.7) and in Figure E.3

NOTE 2  $\lambda = \ell/b$ 

#### E.1.5.2.5 Mode shape factor

(1) The mode shape factor K is given in Expression (E.9).

$$K = \frac{\sum_{j=1}^{m} \int_{\ell_{j}} |\mathcal{D}_{i,y}(s)| ds}{4 \cdot \pi \cdot \sum_{j=1}^{m} \int_{\ell_{j}} \mathcal{D}_{i,y}^{2}(s) ds}$$
(E.9)

where:

m is defined in E.1.5.2.4 (1)

 $\Phi_{i,v}(s)$  is the cross-wind mode shape i (see F.3)

 $\ell_{\rm i}$  is the length of the structure between two nodes (see Figure E.3)

(2) For some simple structures vibrating in the fundamental cross-wind mode the mode shape factor is given in Table E.5.

#### E.1.5.2.6 Number of load cycles

(1) The number of load cycles N caused by vortex excited oscillation is given by Expression (E.10).

$$N = 2 \cdot T \cdot n_{y} \cdot \varepsilon_{0} \cdot \left(\frac{v_{crit}}{v_{0}}\right)^{2} \cdot \exp\left(-\left(\frac{v_{crit}}{v_{0}}\right)^{2}\right)$$
 (E.10)

where:

 $n_v$  is the natural frequency of cross-wind mode [Hz]. Approximations for  $n_v$  are given in Annex F

 $v_{\text{crit}}$  is the critical wind velocity [m/s] given in E.1.3.1

 $v_0$  is  $\sqrt{2}$  times the modal value of the Weibull probability distribution assumed for the wind velocity [m/s], see Note 2

T is the life time in seconds, which is equal to 3,2 10<sup>7</sup> multiplied by the expected lifetime in years

 $\varepsilon_0$  is the bandwidth factor describing the band of wind velocities with vortex-induced vibrations, see Note 3

NOTE 1 The National Annex may specify the minimum value of N. The recommended value is  $N \ge 10^4$ .

NOTE 2 The value  $v_0$  can be taken as 20 % of the characteristic mean wind velocity as specified in 4.3.1 (1) at the height of the cross section where vortex shedding occurs.

NOTE 3 The bandwidth factor  $\varepsilon_0$  is in the range 0,1 – 0,3. It may be taken as  $\varepsilon_0$  = 0,3.

#### E.1.5.2.7 Vortex resonance of vertical cylinders in a row or grouped arrangement

(1) For circular cylinders in a row or grouped arrangement with or without coupling (see Figure E.4) vortex excited vibrations may occur.

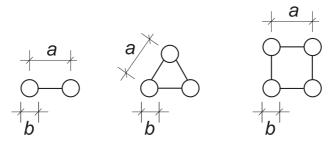


Figure E.4 — In-line and grouped arrangements of cylinders

(2) The maximum deflections of oscillation can be estimated by Expression (E.6) and the calculation procedure given in E.1.5.2 with the modifications given by Expressions (E.11) and (E. 12).

For in-line, free standing circular cylinders without coupling:

$$c_{\text{lat}} = 1,5 \cdot c_{\text{lat(single)}} \qquad \qquad \text{for} \qquad 1 \leq \frac{a}{b} \leq 10$$
 
$$c_{\text{lat}} = c_{\text{lat(single)}} \qquad \qquad \text{for} \qquad \frac{a}{b} \geq 15$$
 
$$\text{linear interpolation} \qquad \qquad \text{for} \qquad 10 < \frac{a}{b} \leq 15$$
 
$$St = 0,1 + 0,085 \cdot \log \left(\frac{a}{b}\right) \qquad \qquad \text{for} \qquad 1 \leq \frac{a}{b} \leq 9$$
 
$$St = 0,18 \qquad \qquad \text{for} \qquad \frac{a}{b} > 9$$

where:

 $c_{\text{lat (single)}} = c_{\text{lat}}$  as given in Table E.3

For coupled cylinders:

$$c_{\text{lat}} = K_{\text{iv}} \cdot c_{\text{lat(single)}}$$
 for  $1,0 \le a/b \le 3,0$  (E.12)

where:

 $K_{iv}$  is the interference factor for vortex shedding (Table E.8)

St is the Strouhal number, given in Table E.8

Sc is the Scruton number, given in Table E.8

For coupled cylinders with a/d > 3.0 specialist advice is recommended.

NOTE The factor  $1.5 \cdot c_{lat}$  for circular cylinders without coupling is a rough approximation. It is expected to be conservative.

#### E.1.5.3 Approach 2, for the calculation of the cross wind amplitudes

(1) The characteristic maximum displacement at the point with the largest movement is given in Expression (E.13).

$$y_{\text{max}} = \sigma_{y} \cdot k_{p} \tag{E.13}$$

where:

 $\sigma_{\rm v}$  is the standard deviation of the displacement, see (2)

 $k_{\rm p}$  is the peak factor, see (6)

(2) The standard deviation  $\sigma_y$  of the displacement related to the width b at the point with the largest deflection ( $\Phi$  = 1) can be calculated by using Expression (E.14).

$$\frac{\sigma_{y}}{b} = \frac{1}{St^{2}} \cdot \frac{C_{c}}{\sqrt{\frac{Sc}{4 \cdot \pi} - K_{a} \cdot \left(1 - \left(\frac{\sigma_{y}}{b \cdot a_{L}}\right)^{2}\right)}} \cdot \sqrt{\frac{\rho \cdot b^{2}}{m_{e}}} \cdot \sqrt{\frac{b}{h}}$$
(E.14)

where:

- C<sub>c</sub> is the aerodynamic constant dependent on the cross-sectional shape, and for a circular cylinder also dependent on the Reynolds number Re as defined in E.1.3.4 (1); given in Table E.6.
- $K_a$  is the aerodynamic damping parameter as given in E.1.5.3 (4)
- $a_L$  is the normalised limiting amplitude giving the deflection of structures with very low damping; given in Table E.6
- St is the Strouhal number given in E.1.6.2
- $\rho$  is the air density under vortex shedding conditions, see Note 1
- $m_{\rm e}$  is the effective mass per unit length; given in F.4 (1)
- *h,b* is the height and width of structure. For structures with varying width, the width at the point with largest displacements is used.
  - NOTE 1 The value of the air density  $\rho$  may be given in the National Annex. The recommended value is 1,25 kg/m<sup>3</sup>.
  - NOTE 2 The aerodynamic constant C<sub>c</sub> depends on the lift force acting on a non-moving structure.
  - NOTE 3 The motion-induced wind loads are taken into account by  $K_a$  and  $a_L$ .
- (3) The solution to Expression (E.14) is given in Expression (E.15).

$$\left(\frac{\sigma_{y}}{b}\right)^{2} = c_{1} + \sqrt{c_{1}^{2} + c_{2}}$$
 (E.15)

where the constants  $c_1$  and  $c_2$  are given by:

$$c_1 = \frac{a_L^2}{2} \cdot \left( 1 - \frac{Sc}{4 \cdot \pi \cdot K_a} \right); \qquad c_2 = \frac{\rho \cdot b^2}{m_e} \cdot \frac{a_L^2}{K_a} \cdot \frac{C_c^2}{St^4} \cdot \frac{b}{h}$$
 (E.16)

(4) The aerodynamic damping constant  $K_a$  decreases with increasing turbulence intensity. For a turbulence intensity of 0 %, the aerodynamic damping constant may be taken as  $K_a = K_{a,max}$ , which is given in Table E.6.

NOTE Using  $K_{a,max}$  for turbulence intensities larger 0 % gives conservative predictions of displacements. More detailed information on the influence of the turbulence intensity on  $K_a$  may be specified in the National Annex.

(5) For a circular cylinder and a square cross-section the constants  $C_c$ ,  $K_{a,max}$  and  $a_L$  are given in Table E.6.

Table E.6 — Constants for determination of the effect of vortex shedding

Constant	Circular cylinder Re ≤ 10 <sup>5</sup>	Circular cylinder Re = 5·10 <sup>5</sup>	Circular cylinder Re ≥ 10 <sup>6</sup>	Square cross-section
C <sub>c</sub>	0,02	0,005	0,01	0,04
K <sub>a,max</sub>	2	0,5	1	6
a <sub>L</sub>	0,4	0,4	0,4	0,4

NOTE: For circular cylinders the constants  $C_c$  and  $K_{a,max}$  are assumed to vary linearly with the logarithm of the Reynolds number for  $10^5 < Re < 5.10^5$  and for  $5.10^5 < Re < 10^6$ , respectively.

(6) The peak factor  $k_p$  should be determined.

NOTE The National Annex may specify the peak factor. Expression (E.17) gives the recommended value.

$$k_{p} = \sqrt{2} \cdot \left(1 + \frac{1,2}{\tan\left(0.75 \cdot \frac{Sc}{(4 \cdot \pi \cdot K_{a})}\right)}\right)$$
 (E.17)

(7) The number of load cycles may be obtained from E.1.5.2.6 using a bandwidth factor of  $\varepsilon_0$  = 0,15.

#### E.1.6 Measures against vortex induced vibrations

- (1) The vortex-induced amplitudes may be reduced by means of aerodynamic devices (only under special conditions, e.g. Scruton numbers larger than 8) or damping devices supplied to the structure. The drag coefficient  $c_f$  for a structure with circular cross section and aerodynamic devices based on the basic diameter b, may increase up to a value of 1,4. Both applications require special advice.
- (2) For more information see codes for special structures.

#### E.2 Galloping

#### E.2.1 General

- (1) Galloping is a self-induced vibration of a flexible structure in cross wind bending mode. Non circular cross sections including L-, I-, U- and T-sections are prone to galloping. Ice may cause a stable cross section to become unstable.
- (2) Galloping oscillation starts at a special onset wind velocity  $v_{CG}$  and normally the amplitudes increase rapidly with increasing wind velocity.

#### E.2.2 Onset wind velocity

(1) The onset wind velocity of galloping,  $v_{CG}$ , is given in Expression (E.18).

$$v_{\rm CG} = \frac{2 \cdot Sc}{a_{\rm C}} \cdot n_{\rm 1,y} \cdot b \tag{E.18}$$

where:

Sc is the Scruton number as defined in E.1.3.3 (1)

 $n_{1,y}$  is the cross-wind fundamental frequency of the structure; approximations of  $n_{1,y}$  are given in F.2

- b is the width as defined in Table E.7
- $a_{\rm G}$  is the factor of galloping instability (Table E.7); if no factor of galloping instability is known,  $a_{\rm G}$  = 10 may be used.
- (2) It should be ensured that :

$$V_{\rm CG} > 1,25 \cdot V_{\rm m} \tag{E.19}$$

where:

- $v_{\rm m}$  is the mean wind velocity as defined in Expression (4.3) and calculated at the height, where galloping process is expected, likely to be the point of maximum amplitude of oscillation.
- (3) If the critical vortex shedding velocity  $v_{crit}$  is close to the onset wind velocity of galloping  $v_{CG}$ :

$$0.7 < \frac{V_{\text{CG}}}{V_{\text{crit}}} < 1.5$$
 (E.20)

interaction effects between vortex shedding and galloping are likely to occur. In this case specialist advice is recommended.

Table E.7 — Factor of galloping instability  $a_{\rm G}$ 

Cross-section		Factor of galloping instability a <sub>G</sub>	Cross-section		Factor of galloping instability a <sub>G</sub>
t t = 0,06 b  →   ←		10		b	1,0
ICE (ice on cables)		1,0	** \( \ell \) \( \text{\lambda} \) \( \lambda	/3 <u></u>	4
	d/b=2	2	* b * * d	d/b=2	0,7
linear interpolation	<i>d/b</i> =1,5	1,7	* d * *	d/b=2,7	5
	<i>d/b</i> =1	1,2	* d *	d/b=5	7
<del></del>	d/b=2/3	1	+ d +	d/b=3	7,5
b b d +	d/b=1/2	0,7	*d*	d/b=3/4	3,2
linear interpolation	d/b=1/3	0,4	<b>↓ † b † d d d</b>	d/b=2	1
NOTE Extrapolations for the factor $a_{G}$ as function of d/b are not allowed.					

#### E.2.3 Classical galloping of coupled cylinders

- (1) For coupled cylinders (Figure E.4) classical galloping may occur.
- (2) The onset velocity for classical galloping of coupled cylinders,  $v_{CG}$ , may be estimated by Expression (E.21)

$$v_{\text{CG}} = \frac{2 \cdot Sc}{a_{\text{G}}} \cdot n_{1,x} \cdot b \tag{E.21}$$

where Sc,  $a_{\rm G}$  and b are given in Table E.8 and  $n_{\rm 1,y}$  is the natural frequency of the bending mode (see F.2).

(3) It should be ensured that:

$$V_{CG} > 1,25 \cdot V_{m}(z) \tag{E.22}$$

where:

 $v_m(z)$  is the mean wind velocity as defined in Expression (4.3), calculated at the height z, where the galloping excitation is expected, that is likely to be the point of maximum amplitude of oscillation

Table E.8 — Data for the estimation of cross-wind response of coupled cylinders at in-line and grouped arrangements

Coupled cylinders         Scruton number $Sc = \frac{2 \cdot \delta_{x} \cdot \Sigma_{m_{xy}}}{\rho \cdot b^{2}}$ (compare with Expression (E.4)) $alb = 1$ $alb \ge 2$ $alb \le 1,5$ $alb \ge 2,5$ $Alb = 1$ $Alb \ge 2$ $alb \le 1,5$ $alb \ge 2,5$ $Alb = 1$ $Alb \ge 2$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1,5$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1,5$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1,5$ $Alb \ge 1,5$ $Alb \ge 2,5$ $Alb = 1,5$ $Alb \ge 1,5$ $Alb \ge 1,5$ $Alb \ge 1,5$ $Alb = 1,5$ $Alb \ge 1,5$ $Alb \ge 1,5$ $Alb \ge 1,5$ $Alb \ge 1,5$ $Alb = 1,5$ $Alb \ge $		dirangements				
		Scruton number $Sc = \frac{2 \cdot \delta_s \cdot \Sigma_{m_{i,y}}}{\rho \cdot b^2}$ (compare with Expression (				
$K_{iv} = 1.5$ $K_{iv} = 1.5$ $A_{iv} = 1.5$ $A_{iv} = 3.0$ $A_{i$	.,	a/b = 1	a/b ≥ 2	<i>alb</i> ≤ 1,5	a/b ≥ 2,5	
$K_{iv} = 4.8$ $K_{iv} = 3.0$ $A_{iv} = 3.0$ $A_{i$	1 1 0—0 1 <del>1, 1</del>	K <sub>iv</sub> = 1,5	K <sub>iv</sub> = 1,5	a <sub>G</sub> = 1,5	a <sub>G</sub> = 3,0	
$K_{iv} = 4.8$ $K_{iv} = 3.0$ $A_{iv} = 3.0$ $A_{i$	* * * * * * * * * * * * * * * * * * * *	K <sub>iv</sub> = 4,8	K <sub>iv</sub> = 3,0	a <sub>G</sub> = 6,0	a <sub>G</sub> = 3,0	
15 10 10 5	1	K <sub>iv</sub> = 4,8	K <sub>iv</sub> = 3,0	a <sub>G</sub> = 1,0	a <sub>G</sub> = 2,0	
15 10 i=3 i=2		linear interpolation				
Reciprocal Strouhal numbers of coupled cylinders with in-line and grouped arrangements		15 10 Reciprocal Strouha	0 1	i=3 i=2 2 3	a b	

### E.3 Interference galloping of two or more free standing cylinders

- (1) Interference galloping is a self-excited oscillation which may occur if two or more cylinders are arranged close together without being connected with each other.
- (2) If the angle of wind attack is in the range of the critical wind direction  $\mathcal{B}_k$  and if a/b < 3 (see Figure E.5), the critical wind velocity,  $v_{\text{CIG}}$ , may be estimated by

$$v_{\text{CIG}} = 3.5 \cdot n_{1,y} \cdot b \sqrt{\frac{\frac{a}{b} \cdot Sc}{a_{\text{IG}}}}$$
 (E.23)

where:

Sc is the Scruton number as defined in E.1.3.3 (1)

 $a_{IG}$  is the combined stability parameter  $a_{IG} = 3.0$ 

 $n_{1,y}$  is the fundamental frequency of cross-wind mode. Approximations are given in F.2

a is the spacing

b is the diameter

NOTE The National Annex may give additional guidance on a<sub>IG</sub>.

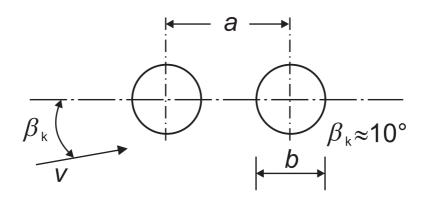


Figure E.5 — Geometric parameters for interference galloping

(3) Interference galloping can be avoided by coupling the free-standing cylinders. In that case classical galloping may occur (see E.2.3).

#### E.4 Divergence and Flutter

#### E.4.1 General

- (1) Divergence and flutter are instabilities that occur for flexible plate-like structures, such as signboards or suspension-bridge decks, above a certain threshold or critical wind velocity. The instability is caused by the deflection of the structure modifying the aerodynamics to alter the loading.
- (2) Divergence and flutter should be avoided.
- (3) The procedures given below provide a means of assessing the susceptibility of a structure in terms of simple structural criteria. If these criteria are not satisfied, specialist advice is recommended

#### E.4.2 Criteria for plate-like structures

To be prone to either divergence or flutter, the structure satisfies all of the three criteria given below. The criteria should be checked in the order given (easiest first) and if any one of the criteria is not met, the structure will not be prone to either divergence or flutter.

- The structure, or a substantial part of it, has an elongated cross-section (like a flat plate) with b/d less than 0,25 (see Figure E.6).
- The torsional axis is parallel to the plane of the plate and normal to the wind direction, and the centre of torsion is at least d/4 downwind of the windward edge of the plate, where b is the inwind depth of the plate measured normal to the torsional axis. This includes the common cases of torsional centre at geometrical centre, i.e. centrally supported signboard or canopy, and torsional centre at downwind edge, i.e. cantilevered canopy.
- The lowest natural frequency corresponds to a torsional mode, or else the lowest torsional natural frequency is less than 2 times the lowest translational natural frequency.

#### E.4.3 Divergency velocity

(1) The critical wind velocity for divergence is given in Expression (E.24)

$$v_{\text{div}} = \left[ \frac{2 \cdot k_{\Theta}}{\rho \cdot d^2 \cdot \frac{dc_{\text{M}}}{d\Theta}} \right]^{\frac{1}{2}}$$
 (E.24)

where:

 $k_{\Theta}$  is the torsional stiffness

 $c_{\rm M}$  is the aerodynamic moment coefficient, given in Expression (E.25):

$$c_{\rm M} = \frac{M}{\frac{1}{2} \cdot \rho \cdot v^2 \cdot d^2} \tag{E.25}$$

 $dc_{\text{M}}/d\Theta$  is the rate of change of aerodynamic moment coefficient with respect to rotation about the torsional centre,  $\Theta$  is expressed in radians.

 $\rho$  is the density of air given in 4.5

d is the in wind depth (chord) of the structure (see Figure E.6)

- b width as defined in Figure E.6
- (2) Values of  $dc_{\text{M}}/d\Theta$  measured about the geometric centre of various rectangular sections are given in Figure E.6.
- (3) It should be ensured that:

$$V_{\rm div} > 2 \cdot V_{\rm m}(Z_{\rm e}) \tag{E.26}$$

where:

 $v_{\rm m}(z_{\rm e})$  mean wind velocity as defined in Expression (4.3) at height  $z_{\rm e}$  (defined in Figure 6.1)

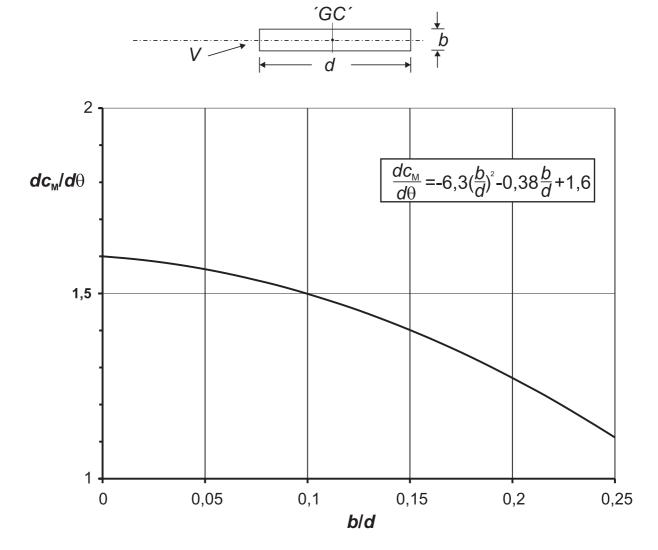


Figure E.6 — Rate of change of aerodynamic moment coefficient,  $dc_{\rm M}/d\Theta$ , with respect to geometric centre "GC" for rectangular section

# Annex F (informative)

## **Dynamic characteristics of structures**

#### F.1General

- (1) Calculation procedures recommended in this section assume that structures possess linear elastic behaviour and classical normal modes. Dynamic structural properties are therefore characterised by:
- natural frequencies
- modal shapes
- equivalent masses
- logarithmic decrements of damping.
- (2) Natural frequencies, modal shapes, equivalent masses and logarithmic decrements of damping should be evaluated, theoretically or experimentally, by applying the methods of structural dynamics.
- (3) Fundamental dynamic properties can be evaluated in approximate terms, using simplified analytical, semiempirical or empirical equations, provided they are adequately proved: Some of these equations are given in F.2 to F.5.

#### F.2Fundamental frequency

(1) For cantilevers with one mass at the end a simplified expression to calculate the fundamental flexural frequency  $n_1$  of structures is given by Expression (F.1):

$$n_1 = \frac{1}{2 \cdot \pi} \cdot \sqrt{\frac{g}{x_1}} \tag{F.1}$$

where:

- g is the acceleration of gravity = 9,81 m/s<sup>2</sup>
- x<sub>1</sub> is the maximum displacement due to self weight applied in the vibration direction in m
- (2) The fundamental flexural frequency  $n_1$  of multi-storey buildings with a height larger than 50 m can be estimated using Expression (F.2):

$$n_1 = \frac{46}{h} \text{ [Hz]} \tag{F.2}$$

where:

*h* is the height of the structure in m

The same expression may give some guidance for single-storey buildings and towers.

(3) The fundamental flexural frequency  $n_1$ , of chimneys can be estimated by Expression (F.3):

$$n_1 = \frac{\varepsilon_1 \cdot b}{h_{\text{eff}}^2} \cdot \sqrt{\frac{W_s}{W_t}} \quad [Hz]$$
 (F.3)

with:

$$h_{\text{eff}} = h_1 + \frac{h_2}{3}$$
 (F.4)

where:

b is the top diameter of the chimney [m],

 $h_{\text{eff}}$  is the effective height of the chimney [m],  $h_1$  and  $h_2$  are given in Figure F.1,

 $W_{\rm s}$  is the weight of structural parts contributing to the stiffness of the chimney,

 $W_{\rm t}$  is the total weight of the chimney,

 $\varepsilon_1$  is equal to 1000 for steel chimneys, and 700 for concrete and masonry chimneys.

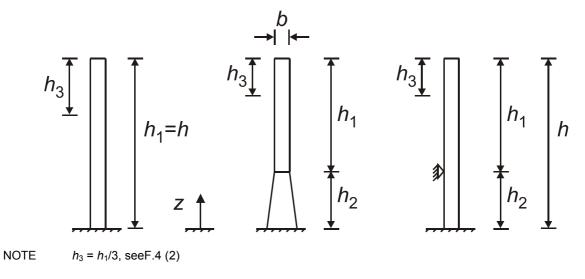


Figure F.1 — Geometric parameters for chimneys

(4) The fundamental ovalling frequency  $n_{1,0}$  of a long cylindrical shell without stiffening rings may be calculated using Expression (F.5).

$$n_{1,0} = 0.492 \cdot \sqrt{\frac{t^3 \cdot E}{\mu_s \cdot (1 - v^2) \cdot b^4}}$$
 (F.5)

where:

E is Young's modulus in [N/m<sup>2</sup>]

t is the shell thickness in [m]

ν is Poisson ratio

 $\mu_{\rm s}$  is the mass of the shell per unit area in [kg/m<sup>2</sup>]

b is the diameter of the shell in [m]

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Expression (F.5) gives the lowest natural frequency of the shell. Stiffness rings increase  $n_0$ .

(5) The fundamental vertical bending frequency  $n_{1,B}$  of a plate or box girder bridge may be approximately derived from Expression (F.6).

$$n_{1,B} = \frac{K^2}{2 \cdot \pi \cdot L^2} \cdot \sqrt{\frac{EI_b}{m}}$$
 (F.6)

where:

L is the length of the main span in m

E is Youngs Modulus in N/m<sup>2</sup>

I<sub>b</sub> is the second moment of area of cross-section for vertical bending at mid-span in m<sup>4</sup>

m is the mass per unit length of the full cross-section ad midspan (for dead and super-imposed dead loads) in kg/m

K is a dimensionless factor depending on span arrangement defined below.

a) For single span bridges:

 $K = \pi$  if simply supported or

K = 3.9 if propped cantilevered or

K = 4.7 if encastre

b) For two-span continuous bridges:

K is obtained from Figure F.2, using the curve for two-span bridges, where

 $L_1$  is the length of the side span and  $L > L_1$ .

c) For three-span continuous bridges:

*K* is obtained from Figure F.2, using the appropriate curve for three-span bridges, where

 $L_1$  is the length of the longest side span

 $L_2$  is the length of the other side span and  $L > L_1 > L_2$ 

This also applies to three-span bridges with a cantilevered/suspended main span.

If  $L_1 > L$  then K may be obtained from the curve for two span bridges, neglecting the shortest side span and treating the largest side span as the main span of an equivalent two-span bridge.

d) For symmetrical four-span continuous bridges (i.e. bridges symmetrical about the central support):

*K* may be obtained from the curve for two-span bridges in Figure F.2 treating each half of the bridge as an equivalent two-span bridge.

e) For unsymmetrical four-span continuous bridges and continuous bridges with more than four spans:

K may be obtained from Figure F.2 using the appropriate curve for three-span bridges, choosing the main span as the greatest internal span.

NOTE 1 If the value of  $\sqrt{\frac{EI_b}{m}}$  at the support exceeds twice the value at mid-span, or is less than 80 % of the mid-span value, then the Expression (F.6) should not be used unless very approximate values are sufficient.

NOTE 2 A consistent set should be used to give  $n_{1,B}$  in cycles per second.

- (6) The fundamental torsional frequency of plate girder bridges is equal to the fundamental bending frequency calculated from Expression (F.6), provided the average longitudinal bending inertia per unit width is not less than 100 times the average transverse bending inertia per unit length.
- (7) The fundamental torsional frequency of a box girder bridge may be approximately derived from Expression (F.7):

$$n_{1,T} = n_{1,B} \cdot \sqrt{P_1 \cdot (P_2 + P_3)}$$
 (F.7)

with:

$$P_1 = \frac{m \cdot b^2}{I_0} \tag{F.8}$$

$$P_2 = \frac{\sum r_i^2 \cdot I_j}{b^2 \cdot I_p} \tag{F.9}$$

$$P_3 = \frac{L^2 \cdot \sum J_j}{2 \cdot K_2 \cdot b^2 \cdot I_2 \cdot (1 + \nu)}$$
 (F.10)

where:

 $n_{1,B}$  is the fundamental bending frequency in Hz

b is the total width of the bridge

*m* is the mass per unit length defined in F.2 (5)

ν is Poisson's ratio of girder material

- $r_i$  is the distance of individual box centre-line from centre-line of bridge
- $I_{\rm j}$  is the second moment of mass per unit length of individual box for vertical bending at mid-span, including an associated effective width of deck
- $I_p$  is the second moment of mass per unit length of cross-section at mid-span. It is described by Expression (F.11).

$$I_{p} = \frac{m_{d} \cdot b^{2}}{12} + \sum (I_{pj} + m_{j} \cdot r_{j}^{2})$$
 (F.11)

where:

 $m_{\rm d}$  is the mass per unit length of the deck only, at mid-span

 $I_{pj}$  is the mass moment of inertia of individual box at mid-span

 $m_{\rm j}$  is the mass per unit length of individual box only, at mid-span, without associated portion of deck

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 $J_{\rm j}$  is the torsion constant of individual box at mid-span. It is described by Expression (F.12).

$$J_{j} = \frac{4 \cdot A_{j}^{2}}{\oint \frac{ds}{t}}$$
 (F.12)

where:

A<sub>j</sub> is the enclosed cell area at mid-span

 $\oint \frac{ds}{t}$  is the integral around box perimeter of the ratio length/thickness for each portion of box wall at mid-span

NOTE Slight loss of accuracy may occur if the proposed Expression (F.12) is applied to multibox bridges whose plan aspect ratio (=span/width) exceeds 6.

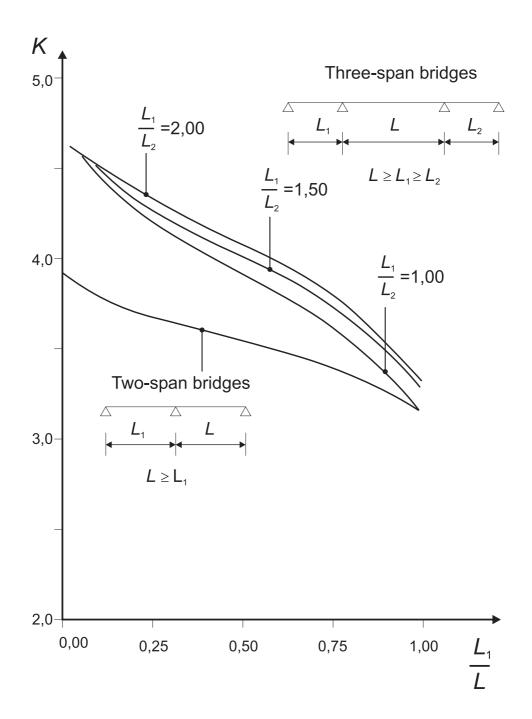


Figure F.2 — Factor K used for the derivation of fundamental bending frequency

## F.3Fundamental mode shape

(1) The fundamental flexural mode  $\Phi_1(z)$  of buildings, towers and chimneys cantilevered from the ground may be estimated using Expression (F.13), see Figure F.3.

$$\Phi_{1}(z) = \left(\frac{z}{h}\right)^{\zeta}$$
 (F.13)

where:

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- $\zeta$  = 0,6 for slender frame structures with non load-sharing walling or cladding
- $\zeta$  = 1,0 for buildings with a central core plus peripheral columns or larger columns plus shear bracings
- $\zeta$  = 1,5 for slender cantilever buildings and buildings supported by central reinforced concrete cores
- $\zeta$  = 2,0 for towers and chimneys
- $\zeta$  = 2,5 for lattice steel towers

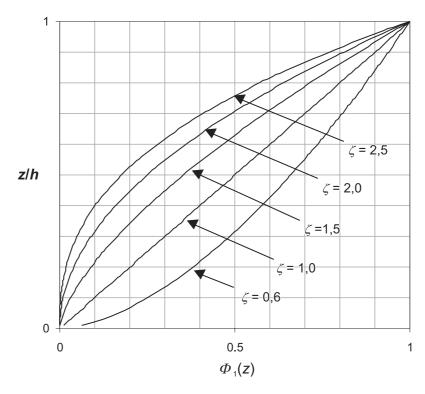


Figure F.3— Fundamental flexural mode shape for buildings, towers and chimneys cantilevered from the ground

(2) The fundamental flexural vertical mode  $\Phi_1(s)$  of bridges may be estimated as shown in Table F.1.

Table F.1 — Fundamental flexural vertical mode shape for simple supported and clamped structures and structural elements

Scheme	Mode shape	$\Phi_1(s)$
$ \begin{array}{c c}                                    $	$\Phi_1(s) = \frac{1}{4} 1$	$\sin\!\left(\pi\cdotrac{s}{\ell} ight)$
	$\frac{\Phi_1(s)}{\frac{1}{1}}$	$\frac{1}{2} \cdot \left[ 1 - \cos \left( 2 \cdot \pi \cdot \frac{s}{\ell} \right) \right]$

#### F.4Equivalent mass

(1) The equivalent mass per unit length  $m_e$  of the fundamental mode is given by Expression (F.14).

$$m_{\rm e} = \frac{\int\limits_0^\ell m(\mathbf{s}) \cdot \Phi_1^2(\mathbf{s}) \, \mathrm{d}\mathbf{s}}{\int\limits_0^\ell \Phi_1^2(\mathbf{s}) \, \mathrm{d}\mathbf{s}}$$
 (F.14)

where:

*m* is the mass per unit length

is the height or span of the structure or the structural element

i = 1 is the mode number

- (2) For cantilevered structures with a varying mass distribution  $m_e$  may be approximated by the average value of m over the upper third of the structure  $h_3$  (see Figure F.1).
- (3) For structures supported at both ends of span  $\ell$  with a varying distribution of the mass per unit length  $m_e$  may be approximated by the average value of m over a length of  $\ell/3$  centred at the point in the structure in which  $\mathcal{D}(s)$  is maximum (see Table F.1).

#### F.5Logarithmic decrement of damping

(1) The logarithmic decrement of damping  $\delta_s$  for fundamental bending mode may be estimated by Expression (F.15).

$$\delta = \delta_{s} + \delta_{a} + \delta_{d} \tag{F.15}$$

where:

- $\delta_{\rm s}$  is the logarithmic decrement of structural damping
- $\delta_{a}$  is the logarithmic decrement of aerodynamic damping for the fundamental mode
- $\delta_{\rm d}$  is the logarithmic decrement of damping due to special devices (tuned mass dampers, sloshing tanks etc.)
- (2) Approximate values of logarithmic decrement of structural damping,  $\delta_s$ , are given in Table F.2.
- (3) The logarithmic decrement of aerodynamic damping  $\delta_a$ , for the fundamental bending mode of alongwind vibrations may be estimated by Expression (F.16).

$$\delta_{\rm a} = \frac{c_{\rm f} \cdot \rho \cdot V_{\rm m}(z_{\rm e})}{2 \cdot n_{\rm l} \cdot \mu_{\rm e}} \tag{F.16}$$

where:

- c<sub>f</sub> is the force coefficient for wind action in the wind direction stated in Section 7.
- $\mu_{e}$  is the equivalent mass per unit area of the structure which for rectangular areas given by Expression (F.17).

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$$\mu_{e} = \frac{\int_{0}^{h} \int_{0}^{b} \mu(y,z) \cdot \Phi_{1}^{2}(y,z) \, dydz}{\int_{0}^{h} \int_{0}^{b} \Phi_{1}^{2}(y,z) \, dydz}$$
(F.17)

where

 $\mu(y,z)$  is the mass per unit area of the structure

 $\Phi_1(y,z)$  is the mode shape.

The mass per unit area of the structure at the point of the largest amplitude of the mode shape is normally a good approximation to  $\mu_e$ .

(4) In most cases the modal deflections  $\Phi(y,z)$  are constant for each height z and instead of Expression (F.16) the logarithmic decrement of aerodynamic damping  $\delta_a$ , for alongwind vibrations may be estimated by Expression (F.18).

$$\delta_{a} = \frac{c_{f} \cdot \rho \cdot b \cdot v_{m}(z_{e})}{2 \cdot n_{1} \cdot m_{e}}$$
 (F.18)

(5) If special dissipative devices are added to the structure,  $\delta_d$  should be calculated by suitable theoretical or experimental techniques.

Table F.2 —Approximate values of logarithmic decrement of structural damping in the fundamental mode,  $\delta$ 

Structural type $\delta_{\!\scriptscriptstyle S}$ structural damping,						
reinforced concrete building	0,10					
steel buildings			0,05			
mixed structures concrete	e + steel		0,08			
reinforced concrete tower	s and chimneys		0,03			
unlined welded steel stack	ks without external thermal ins	ulation	0,012			
unlined welded steel stack	k with external thermal insulation	on	0,020			
		<i>h/b</i> < 18	0,020			
steel stack with one liner insulation <sup>a</sup>	with external thermal	20≤h/b<24	0,040			
		<i>h</i> / <i>b</i> ≥ 26	0,014			
		h/b <18	0,020			
steel stack with two or mo thermal insulation <sup>a</sup>	ore liners with external	20≤h/b<24	0,040			
thornal modiation		<i>h</i> / <i>b</i> ≥ 26	0,025			
steel stack with internal be	steel stack with internal brick liner 0,070					
steel stack with internal gunite 0,030						
coupled stacks without liner 0,015						
guyed steel stack without	0,04					
	welded		0,02			
steel bridges + lattice steel towers	high resistance bolts		0,03			
	ordinary bolts		0,05			
composite bridges			0,04			
concrete bridges	prestressed without cracks		0,04			
concrete bridges	with cracks		0,10			
Timber bridges			0,06 - 0,12			
Bridges, aluminium alloys 0,02						
Bridges, glass or fibre reinforced plastic 0,04 - 0,08						
cables	0,006					
spiral cables 0,020						
NOTE 1 The values for timber and plastic composites are indicative only. In cases where aerodynamic effects are found to be significant in the design, more refinded figures are needed through specialist advice (agreed if appropriate with the competent Authority.						
NOTE 2 For cable supported bridges the values given in Table F.2 need to be factored by 0,75						
<sup>a</sup> For intermediate values of <i>h/b</i> , linear interpolation may be used						

# **Bibliography**

ISO 2394 General principles on reliability for structures

ISO 3898 General principles on reliability for structures

ISO 8930 General principles on reliability for structures - List of equivalent terms

ISO FDIS12494